# **Beam Cooling**

### **Beam Cooling**

Introduction

- **1. Electron Cooling**
- 2. Laser Cooling
- 3. Stochastic Cooling

Cooling

#### reduction of momentum (energy) spread due to cooling





M. Steck GSI Helmholtzzentrum Darmstadt

reduction of beam size (emittance)

due to cooling

## **Beam Cooling**

Beam cooling is synonymous for a reduction of beam temperature.

Temperature is equivalent to terms as phase space volume, emittance and momentum spread.

Beam Cooling processes are not following Liouville's Theorem: `in a system where the particle motion is controlled by external conservative forces the phase space density is conserved'

(This neglect interactions between beam particles.)

Beam cooling techniques are non-Liouvillean processes which violate the assumption of a conservative force.

e.g. interaction of the beam particles with other particles (electrons, photons, matter)

### **Beam Temperature**

Where does the beam temperature originate from? The beam particles are generated in a 'hot' source



#### at rest (source)

at low energy

#### at high energy

In a standard accelerator the beam temperature is not reduced (thermal motion is superimposed the average motion after acceleration) but: many processes can heat up the beam

e.g. heating by mismatch, space charge, intrabeam scattering, internal targets, residual gas, external noise

## **Adiabatic Shrinking**



after acceleration from  $p_1$  to  $p_2$ :  $x_2' < x_1'$ 

adiabatic shrinking of emittance:  $\epsilon_2 = x_2 \cdot x_2' < \epsilon_1 = x_1 \cdot x_1'$ 

 $\epsilon_1\beta_1\gamma_1 = \epsilon_2\beta_2\gamma_2$  (normalized emittance) momentum:  $p_{1,2} = m_0c\beta_{1,2}\gamma_{1,2}$   $\epsilon_2 = \epsilon_1 \times \beta_1\gamma_1/\beta_2\gamma_2 = \epsilon_1 \times p_1/p_2$ (reduction of emittance due to acceleration)

### **6D Particle Coordinates**

#### **Particle coordinates**



(transverse: vertical)

$$y, y' = \frac{dy}{ds} \approx \frac{p_y}{p_0} < 1$$

the motion in the longitudinal  $(z,\Delta p/p)$ and the transverse phase plane (x,x')(y,y')are decoupled and the phase space areas are conserved independently

### **Beam Temperature Definition**

Longitudinal beam temperature

$$\frac{1}{2}k_B T_{\parallel} = \frac{1}{2}mv_{\parallel}^2 = \frac{1}{2}mc^2\beta^2(\frac{\delta p_{\parallel}}{p})^2$$

Transverse beam temperature

$$\frac{1}{2}k_B T_{\perp} = \frac{1}{2}mv_{\perp}^2 = \frac{1}{2}mc^2\beta^2\gamma^2\theta_{\perp}^2 \qquad \theta_{\perp} = \frac{v_{\perp}}{\beta c}, \quad \theta_{\perp}(s) = \sqrt{\frac{\epsilon}{\beta_{\perp}(s)}}$$

Distribution function  $f(v_{\perp}, v_{\parallel}) \propto \exp(-\frac{mv_{\perp}^2}{2k_B T_{\perp}} - \frac{mv_{\parallel}^2}{2k_B T_{\parallel}})$ 

Particle beams can be anisotropic:  $k_B T_{||} \neq k_B T_{\perp}$ 

e.g. due to laser cooling or the distribution of the electron (cooling) beam

Don't confuse: beam energy  $\leftrightarrow$  beam temperature (e.g. a beam of energy 100 GeV can have a temperature of 1 eV)

### **Benefits of Beam Cooling**

- Improved beam quality
  - Precision experiments
  - Luminosity increase
- Compensation of heating
  - Experiments with internal target
  - Colliding beams
- Intensity increase by accumulation
  - Weak beams from the source can be enhanced
  - Secondary beams (antiprotons, rare isotopes)



### **Non-destructive Diagnostics**

transverse

Profile of transverse distribution from ionization of the residual gas



#### horizontal beam profile



Cooling of the beam after injection into ESR

#### **Non-destructive Diagnostics**

#### longitudinal



Cooling

#### reduction of momentum (energy) spread due to cooling

reduction of beam size (emittance) due to cooling





## **Cooling Force**

#### Generic (simplest case of a) cooling force:

$$F_{x,y,s} = -\alpha_{x,y,s} v_{x,y,s}$$

 $v_{x,y,s}$  velocity in the rest frame of the beam

non conservative, cannot be described by a Hamiltonian

For a 2D subspace distribution function f(z, z', t)

$$\begin{split} F_z &= -\alpha_z v_z \quad z = x, y, s \quad v_z = v_0 \cdot z' \\ \frac{df(z, z', t)}{dt} &= -\lambda_z f(z, z', t) \quad \lambda_z \quad \text{cooling (damping) rate} \end{split}$$

in a circular accelerator:

Transverse (emittance) cooling rate

Longitudinal (momentum spread) cooling rate

$$\epsilon_{x,y}(t_0 + t) = \epsilon_{x,y}(t_0) \ e^{-\lambda_{x,y}t}$$
$$\frac{\delta p_{\parallel}}{p_0}(t_0 + t) = \frac{\delta p_{\parallel}}{p_0}(t_0) \ e^{-\lambda_{\parallel}t}$$



superposition of a cold intense electron beam with the same velocity (in the lab system) momentum transfer by Coulomb collisions, cooling force results from energy loss in the co-moving gas of free electrons







# **Electron Cooling Time**

first estimate:   
(Budker 1967) 
$$\tau = \frac{3}{8\sqrt{2\pi}n_eQ^2r_er_icL_C}(\frac{k_BT_e}{m_ec^2} + \frac{k_BT_i}{m_ic^2})^{3/2}$$

for large relative velocities

cooling time 
$$\tau_z \propto \frac{A}{Q^2} \frac{1}{n_e \eta} \beta^3 \gamma^5 \theta_z^3 \begin{cases} \theta_{x,y} = \frac{v_{x,y}}{\gamma \beta c} \\ \theta_{\parallel} = \frac{v_{\parallel}}{\gamma \beta c} \end{cases}$$
  
cooling rate ( $\tau^{-1}$ ):

- slow for hot beams  $\propto \theta^{-3}$
- decreases with energy  $\propto \gamma^{-2}$  ( $\beta \cdot \gamma \cdot \theta$  is conserved)
- linear dependence on electron beam intensity  $n_e$  and cooler length  $\eta = L_{ec}/C$
- favorable for highly charged ions Q<sup>2</sup>/A
- independent of hadron beam intensity

#### for small relative velocities

cooling rate is constant and maximum at small relative velocity  $F \propto v_{rel} \Rightarrow \tau = \Delta t = p_{rel}/F = constant$ 

### **Longitudinal Cooling**

#### Xe<sup>54+</sup> 350 MeV/u

#### I<sub>e</sub>= 100 mA







#### measurement time 20 s

I<sub>e</sub>= 500 mA

#### protons 400 MeV (Q=1)



#### measurement time 650 s

M. Steck GSI Helmholtzzentrum Darmstadt

#### I<sub>e</sub>= 250 mA

### **Electron Beam Properties**

#### electron beam temperature

is determined by the thermal cathode temperature k<sub>B</sub>T<sub>cat</sub>

transverse temperature  $k_B T_{\perp} = k_B T_{cat}$ 

can be reduced by transverse magnetic expansion with ( $\propto B_c/B_{qun}$ )

longitudinal temperature  $k_B T_{\parallel} = (k_B T_{cat})^2 / 4E_0 << k_B T_{\perp}$ 

**lower limit** :  $k_B T_{\parallel} \ge 2e \frac{n_c^{1/3}}{4\pi\epsilon_0}$ 

typical temperature values:

 $\label{eq:k_BT_l} \begin{array}{ll} \approx 100 \ meV \mbox{ (1100 K)} \\ \mbox{with magnetic expansion} & k_BT_{\perp} \approx 1 \ meV \\ \mbox{longitudinal} & k_BT_{\parallel} \approx 0.1 \mbox{ - 1 meV} \end{array}$ 

### **Electron Beam Properties**

#### constant electron beam radius



# Electron Motion in the Longitudinal Magnetic Field



another important consequence:

for interaction times which are long compared to the cyclotron period the ions do not sense the transverse electron temperature  $\Rightarrow$  magnetized cooling ( $T_{eff} \approx T_{\parallel} \ll T_{\perp}$ )

## **Optimized Electron Cooling**

#### minimize relative velocity between ions and electrons

electron beam space charge:

transverse electric field + longitudinal B-field  $\Rightarrow$  azimuthal drift

$$v_{azi} = r\omega_{azi} = r\frac{2\pi r_e n_e c^2}{\gamma \omega_c}$$

 $\Rightarrow$  electron and ion beam should be well centered

Favorable for optimum cooling (small transverse relative velocity):

- parallel adjustment of ion and electron beam
- high parallelism of magnetic field lines  $B_{\perp}/B_{\parallel}$  in cooling section
- large beta function (small ion beam divergence) in cooling section

#### Electron Cooled Beams in Equilibrium with Intrabeam Scattering (IBS)



### Accumulation of Heavy lons by Electron Cooling

3

2.5

2

1.5

1

2

3

Time [s]

0.5

Ion Current [mA]



fast accumulation by repeated multiturn injection with electron cooling





Au<sup>65+</sup> 11.4 MeV/u

4

-5

6

limitations: space charge tune shift recombination (REC)

### **Accumulation of Secondary Particles**

basic idea: confine stored beam to a fraction of the circumference, inject into gap and apply cooling to merge the two beam components  $\Rightarrow$  fast increase of intensity (for secondary beams)



simulation of longitudinal stacking with barrier buckets and electron cooling experimental verification at ESR



# Some Technical Aspects of Electron Cooling Systems

cold electron beam: thermal cathode at about 1000-1200 degrees C high electron current: up to about 1 A small current losses at full energy:  $\leq 10^{-4}$  relative to electron current ultrahigh vacuum operation: 10<sup>-11</sup> mbar range continuous longitudinal magnetic field from electron gun to collector straight magnetic field (parallel field lines):  $\langle B_{\parallel}/B_{\parallel} \rangle \leq 10^{-5} - 10^{-4}$ stable accelerating voltage (electron energy): variations  $\delta U/U \approx 10^{-6} - 10^{-5}$ control of space charge compensation (capture of residual gas ions in the negative potential of the electron beam)

#### First Experimental Proof: NAP-M Experiment (1974)



NAP-M : "Antiproton Storage Ring – Model" INP Novosibirsk, 1974 – 1984

> First electron cooler "EPOChA" ("Electron beam for cooling of antiprotons", Rus.)





### **Electron Cooling Systems**

#### Low Energy: 35 keV SIS/GSI



Medium Energy: 300 keV ESR/GSI



#### High Energy: 4.3 MeV Recycler/FNAL



## **Bunched Beam Electron Cooling**

Electron cooling with electrostatic acceleration is limited in energy (5-10 MeV). A bunched electron beam offers the extension of the electron cooling method to higher energy (linear rf accelerator to increase the electron energy).



#### Low-Energy RHIC electron Cooler (LEReC) at BNL

- LEReC is the first electron cooler based on the RF acceleration of electron beam .
- State of the art electron accelerator which uses photocathode high-current gun, high-power laser and several RF cavities.
- Electron beam parameters suitable for cooling were successfully generated and transported to the cooling sections in RHIC.
- First electron cooling of hadron beams using a bunched electron beam was demonstrated on April 5, 2019.
- Both longitudinal and transverse cooling was achieved.
- Cooling of ion bunches in two separate RHIC rings (Yellow and Blue) using single electron beam was demonstrated.







## 2. Laser Cooling

#### fast ions interact with laser light



the directed excitation and isotropic emission result in a transfer of velocity v<sub>r</sub>



#### drawbacks: only longitudinal cooling extremely small cooling range

### **Laser Cooling**

a single laser does not provide cooling (only acceleration or deceleration)



capture range of laser is limited  $\Rightarrow$  frequency sweep (snowplow)

ions studied so far: <sup>7</sup>Li<sup>1+</sup>, <sup>9</sup>Be<sup>1+</sup>, <sup>24</sup>Mg<sup>1+</sup>, <sup>12</sup>C<sup>3+</sup>

in future: laser cooling of Li-like heavy ions at relativistic energies at SIS100 large relativistic energy  $\Rightarrow$  large excitation energy in particle rest frame

### Laser Cooling of C<sup>3+</sup>



## **3. Stochastic Cooling**

First cooling method which was successfully used for beam preparation



S. van der Meer, D. Möhl, L. Thorndahl et al. (1925 – 2011) (1936 - 2012)

Conditions:

Betatron motion phase advance (pick-up to kicker):  $(n + \frac{1}{2}) \pi$ 

Signal travel time = time of flight of particle (between pick-up and kicker)

Sampling of sub-ensemble of total beam

Principle of transverse cooling: measurement of deviation from ideal orbit is used for correction kick (feedback)

### **Stochastic Cooling**

single particle betatron motion along storage ring without and with correction kick



### **Stochastic Cooling**



### **Stochastic Cooling**

#### some refinements of cooling rate formula

noise: thermal or electronic noise adds to beam signal

**mixing:** change of relative longitudinal position of particles due to momentum spread

$$\begin{array}{l} \text{cooling rate } \lambda = \tau^{-1} = \displaystyle \frac{2W}{N} \underbrace{(2g - g^2(M + U))}_{\text{cooling heating}} & \text{M mixing factor} \\ \text{U noise to signal ratio} \\ \\ \hline \\ \text{maximum of cooling rate} \\ \lambda_{max} = \displaystyle \frac{2W}{N} \frac{1}{M + U} & \displaystyle \frac{d\lambda}{dg} = 0 \Rightarrow g = \displaystyle \frac{1}{M + U} \end{array}$$

#### further refinement (wanted $\leftrightarrow$ unwanted mixing):

with wanted mixing M = M (kicker to pick-up)  $\lambda = \tau^{-1} = \frac{2W}{N}(2g(1 - \tilde{M}^2) - g^2(M + U))$ and unwanted mixing M (pick-up to kicker)

# Mixing



### **Longitudinal Stochastic Cooling**

#### 1) Palmer cooling

pick-up in dispersive section detects horizontal position  $\Rightarrow$  acceleration/deceleration kick corrects momentum deviation

#### 2) Notch filter cooling

filter creates notches at the harmonics of the nominal revolution frequency

 $\Rightarrow$  particles are forced to circulate at the nominal frequency



#### 3) ToF cooling

simplified scheme without notches allows efficient pre-cooling

# Antiproton Accumulation by Stochastic Cooling

accumulation of 8 GeV antiprotons at Accumulator, FNAL, shut down 09/2011 similar facility AC/AA at CERN, shut down 11/1996



momentum distribution of accumulated antiproton beam



kicker array

microwave electronics



cryogenic microwave amplifier



power amplifiers (TWTs)

M. Steck GSI Helmholtzzentrum Darmstadt

### Stochastic Cooling of Rare Isotopes at GSI





electrodes installed inside magnets



combination of signals from electrodes

power amplifiers for generation of correction kicks

### Combination of Stochastic and Electron Cooling





hot secondary beams can be cooled in reduced total time

#### **Coherent Electron Cooling** A combination of electron and stochastic cooling concepts proposed for fast cooling at highest energies energy range several 10 - 100 GeV **Dispersion section** $E < E_h$ (for hadrons) **Kicker** Hadrons Modulator High gain FEL (for electrons) Electrons

The Coherent Electron Cooling system has three major subsystems

- modulator: the ions imprint a "density bump" on the electron distribution
- **amplifier**: FEL interaction amplifies the density bump by orders of magnitude
- kicker: the amplified & phase-shifted electron charge distribution is used to correct the velocity offset of the ions

investigated for the planned electron-ion collider EIC at BNL

# **Optical Stochastic Cooling Concept**



first experimental demonstration with 100 MeV electron beam in IOTA *Nature 608 287-292 (2022)* 

option for cooling hadron beams of highest energy

### **Comparison of Cooling Methods**

#### **Stochastic Cooling**

**Electron Cooling** 

Useful for:	low intensity beams	low energy all intensities
	hot (secondary) beams high charge full 3 D control	warm beams (pre-cooled) high charge bunched beams
Limitations: /problems	high intensity beams beam quality limited bunched beams	space charge effects recombination losses high energy

laser cooling only cools in the longitudinal degree of freedom and can only be applied to very specific ions (with bound electrons and associated atomic transitions)

## **References 1 (general)**

A. Chao, M. Tigner, Handbook of Accelerator Physics and Engineering, Chapter 2.8, World Scientific, Singapore, 1999

M. Minty, F. Zimmermann, Measurement and Control of Charged Particle Beams, Chapter 11, Springer Verlag, Berlin, 2003

D. Möhl, Principle and Technology of Beam Cooling, CERN/PS 86-31,1986

D. Möhl, Beam Cooling, CAS 2005, CERN 2005-04, pp.324-339

H. Danared, Beam Cooling CAS 2005, CERN 2005-06, pp. 343-362

Y. Zhang, W. Chou, ICFA Beam Dynamics Newsletter No. 64 and 65, December 2014, <u>http://icfa-usa.jlab.org/archive/newsletter.shtml</u>

# **References 2 (specialized)**

#### Electron Cooling:

H. Poth, Electron Cooling, CAS 85, CERN 87-03, pp. 534-569, 1987

H. Poth, Electron Cooling: Theory, Experiment, Application, Phys. Rep. Vol. 196 Issues 3-4, pp. 135-297, 1990

I. Meshkov, Electron Cooling: Status and Perspectives, Physics of Particles and Nuclei, Vol. 25, Issue 6, pp. 631-661, 1994

#### **Stochastic Cooling:**

- D. Möhl, Stochastic Cooling for Beginners, CAS 1983, CERN 84-15, pp. 97-162
- D. Möhl, Stochastic Cooling, CAS 85, CERN 87-03, pp. 453-533, 1987
- D. Möhl, Stochastic Cooling of Particle Beams, Springer Lecture Notes in Physics 866 (2013)
- S. van der Meer, Rev. Mod. Phys. Vol. 57, No. 3 Part 1, 1985

#### Laser Cooling:

E. Bonderup, Laser Cooling, CAS 1993, CERN 95-06, pp. 731-748

#### Ionization Cooling:

D. Neuffer, Introduction to Muon Cooling, Nucl. Instr. Meth. A 532 (2004) 26-31

Biannual Workshops on Beam Cooling: e. g. COOL'19, Novosibirsk, Russia

