Neutrino masses, oscillations, and some further experiments

Slides / insights \rightarrow U. Uwer Errors / confusion \rightarrow SMD

(many concepts and details: K. Zuber, Neutrino Physics)

From neutrino oscillation experiments we know that neutrinos are massive fermions. Cosmological observations yield an upper bound on the sum of masses:

$$\sum_{i=1,2,3} m_{\nu_i} \le 0.2 \mathrm{eV}$$

Do neutrinos obtain their mass through the Higgs-mechanism? If yes, why are the Yukawa couplings (masses) so much smaller than for all other SM fermions?

Closer look to the possible mass terms that respect Lorentz and gauge invariance. For charged fermions in the SM the only possible mass term is the so-called Dirac mass:

 $\mathcal{L} = -m\bar{\psi}\psi = -m(\bar{\psi}_L\psi_R + \bar{\psi}_R\psi_L) \quad \text{with} \quad \bar{\psi} = \psi^{\dagger}\gamma^0 \quad \frac{\text{Mass terms mix LH}}{\text{and RH chiral states}}$

For neutral particles (could be their own anti-particles) other Lorentzinvariant combinations are also possible as mass terms : $\bar{\psi}^c \psi$ and $\bar{\psi} \psi^c$

(with ψ^c the C-conjugated state)

<u>Charge-conjugation operator C (particle-anti-particle transformation):</u>

To deduce the charge-conjugation operator C, we can examine the Dirac Eqs. for an electron and its anti-particle (i.e., positron) in an electric field:

Electron
$$[\gamma^{\mu}(i\partial_{\mu} + eA_{\mu}) - m]\psi = 0$$

Positron $[\gamma^{\mu}(i\partial_{\mu} - eA_{\mu}) - m]\psi^{c} = 0$

From these one finds (see text books) for ψ^c and the C-operator:

$$\psi^{c} = i\gamma_{2}\psi^{*} = i\gamma_{2}\gamma_{0}\bar{\psi}^{T} \equiv C\bar{\psi}^{T} \qquad \qquad \bar{\psi} = \psi^{\dagger}\gamma^{0}$$

The C-operator flips all charge-like quantum-numbers. One finds:

C is real, antisymmetric and unitary

And further:

$$\begin{aligned}
C^{\dagger} &= C^{T} = C^{-1} = -C \\
C\gamma_{\mu}C^{-1} &= -\gamma_{\mu}^{T} \\
C\gamma_{5}C^{-1} &= \gamma_{5}^{T} \\
C\gamma_{\mu}\gamma_{5}C^{-1} &= (\gamma_{\mu}\gamma_{5})^{T}
\end{aligned}$$

$$\begin{aligned}
(\psi^{c})^{c} &= \psi \\
\bar{\psi}^{c} &= \psi^{T}C \\
(\bar{\psi}_{1}\psi_{2}^{c})^{\dagger} &= \bar{\psi}_{2}^{c}\psi_{1}
\end{aligned}$$

(see e.g. K. Zuber, Neutrino Physics)

C-operator flips the chirality!

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1. Dirac mass terms

Dirac masses for neutrinos can be created in the SM by extending the particle content and by adding a RH neutrino singlet v_R :

$$\mathcal{L}_{\nu}^{\text{Yukawa}} = -\sum_{i,j} \left\{ Y_{\nu}^{ij} \overline{L}_{L}^{i} \nu_{R}^{j} H + h.c. \right\}$$

 v_R is a singlet under all SM gauge transformations: \rightarrow no interaction, or "sterile"

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Resulting in a Dirac mass term $m\bar{\nu}v$ after symmetry breaking:

$$\mathcal{L}_{\mathrm{D}}^{\mathrm{Mass}} = -\sum_{i,j} \left\{ \bar{v}_{L}^{i} M_{\mathrm{D}}^{ij} v_{R}^{j} + h.c. \right\}$$

i, j are the flavor indices: *e*, μ , τ $M_{\rm D}$ is a 3x3 complex matrix, in general non-diagonal.

Mass terms are invariant under a global phase transformation: $\nu'_{L,R}^{i} = e^{i\Lambda}\nu_{L,R}^{i}$ \rightarrow From invariance follows the conservation of lepton-number. $\ell'_{L,R}^{i} = e^{i\Lambda}\ell_{L,R}^{i}$

Diagonalization of the mass term works as for quarks (see also theory lectures):

$$\boldsymbol{M}_{\mathrm{D}} = \boldsymbol{U}_{L}^{\dagger} \boldsymbol{m} \boldsymbol{V}_{R}$$

with <u>two unitary matrices</u> to transform the LH and RH chiral components independently: $\frac{3}{2}$

$$\nu_L^{\ell} = \sum_{i=1}^{\ell} U_L^{\ell i} \nu_L^i \text{ and } \nu_R^{\ell} = \sum_{i=1}^{\ell} V_R^{\ell i} \nu_R^i \qquad \ell = e, \mu, \tau$$

Expressed in the mass eigenstates v^i the mass term takes the form:

$$\mathcal{L}_{\rm D}^{\rm Mass} = -\sum_{i=1}^{3} \{ m_i \bar{v}_L^i v_R^i + h. c. \} = -\sum_{i=1}^{3} m_i \bar{v}^i v^i$$

- $v_{1,2,3}$ are the neutrino mass eigenstates with masses $m_{1,2,3}$
- The LH flavor states $v_{e,\mu,\tau}$ which enter into the standard charged and neutral currents are linear combinations of the mass states.
- The unitary matrix U is called PMNS matrix (see above) V does not enter
- The Lagrangian is invariant under global phase transformation: lepton number conservation.

The smallness of the neutrinos masses are a result of very tiny Yukawa couplings

$$M_{ij} = \frac{v}{\sqrt{2}} Y_{ij} \to Y_{ij} \sim O(10^{-12})$$

It is not clear why compared to the quark sector the differences between the v masses and the charged leptons masses are so large.

The RH neutrino singlets have weak hypercharge Y=0 and weak isospin T=0 They do not interact with anything: sterile neutrinos. Massive Dirac neutrinos v and their anti-particles v^{C} are described by four independent chiral components:

$$\nu_L$$
, ν_R , ν_L^C , ν_R^C

In the "original" formulation of the Standard Model, neutrinos masses are zero because of the missing RH v-singlets. The observation of non-vanishing neutrino masses therefore indicates physics beyond the Standard Model.

Remark: massive neutrinos are now often treated as "part of the SM" by assuming the existence of RH neutrinos: the additional new particle does not modify the gauge structure of the theory.

The very small neutrino masses, as well as the existence of a sterile particle, is not motivated.

2. Majorana mass terms

As indicated above, mass terms with $\bar{\psi}^c \psi$ and $\bar{\psi}\psi^c$ also satisfy Lorentz invariance. Moreover $(\psi_L)^c$ is a RH chiral state – thus no need to introduce an additional RH neutrino component. Using LH particle and the anti-particle spinor (RH), the mass term would have the following form:

$$\mathcal{L}_{M}^{Mass} = -\frac{1}{2} \sum_{i,j} \left\{ \bar{\nu}_{L}^{i} M_{M}^{ij} \left(\nu_{L}^{j} \right)^{C} + h.c. \right\} \qquad \text{i, j are the flavor indices: e, } \mu, \tau$$

With the matrix $M_{\rm M}$ (3x3 complex matrix, in general non-diagonal) the mass term can be rewritten in the following matrix form:

$$\mathcal{L}_{M}^{Mass} = -\frac{1}{2} \bar{\nu}_{L} \boldsymbol{M}_{M} (\nu_{L})^{C} + h.c. \qquad \text{with} \quad \nu_{L} = \begin{pmatrix} \nu_{eL} \\ \nu_{\mu L} \\ \nu_{\tau L} \end{pmatrix}$$

We can diagonalize the matrix $M_{\rm M}$ with an unitary transformation U:

$$\mathcal{L}_{M}^{Mass} = -\frac{1}{2} \bar{\nu}^{M} \mathbf{m} \nu^{M} \quad \text{with} \quad \nu^{M} = U^{\dagger} \nu_{L} + \left(U^{\dagger} \nu_{L}\right)^{C} = \begin{pmatrix} \nu_{1} \\ \nu_{2} \\ \nu_{3} \end{pmatrix} \quad (*)$$
$$\mathbf{m} = \text{diag}(m_{1}, m_{2}, m_{3})$$

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 v_i is the field of the neutrino with mass m_i . From Eq. (*) follows:

$$\left(\nu^{\mathsf{M}}\right)^{\mathsf{C}} = \nu^{\mathsf{M}}$$

Thus the fields of the neutrinos with definite mass satisfy the Majorana condition:

 $v_i^C = v_i$

For neutrino field satisfying the Majorana condition: neutrino = antineutrino

The field v^{M} is the sum of a LH and RH component:

$$\nu^{\rm M} = \nu^{\rm M}_L + \nu^{\rm M}_R$$

Comparing with $v^{M} = U^{\dagger}v_{L} + (U^{\dagger}v_{L})^{C}$ one finds

$$\nu_L^{\mathrm{M}} = U^{\dagger} \nu_L$$
 and $\nu_R^{\mathrm{M}} = (U^{\dagger} \nu_L)^C$

i.e. the LH and RH chiral components of the Majorana field are connected by:

$$v_R^{\rm M} = (v_L^{\rm M})^{\rm C}$$
 and consequently $v_{i,R} = (v_{i,L})^{\rm C}$

Which means also the fields $v_{1,2,3}$ satisfy the condition

$$\nu_i = \nu_{i,L} + \left(\nu_{i,L}\right)^C$$

While for Dirac fermion LH and RH components are independent, for Majorana fermions they are connected: $v_{i,R} = (v_{i,L})^{C}$

Under a global phase transformation the two components transform as:

$$v'_{i,L} = e^{i\Lambda}v_{i,L}$$
 and $(v'_{i,L})^C = e^{-i\Lambda}(v_{i,L})^C$

The mass terms $m_i \bar{v}_{i,L} (v_{i,L})^c$ therefore violate lepton number conservation.

It should be stressed that in case of an introduced Majorana mass term, only active left-handed neutrino fields $v_{i,L}$ (RH anti-neutrinos) enter the total Lagrangian: weak interaction cannot distinguish if neutrinos are Dirac or Majorana fermions.

Mass terms $m_i \bar{\nu}_{i,L} (\nu_{i,L})^C$ cannot be generated in a gauge invariant way within the SM: $\nu_L = \begin{bmatrix} I_3 = +\frac{1}{2} & (\bar{\nu}_L)^C \nu_L \\ Y = -1 & Y = -2 \end{bmatrix} \begin{bmatrix} I_3 = +1 \\ Y = -2 \end{bmatrix}$

To generate such a mass term via a Higgs-coupling, a Higgs triplet with I=1, Y=2 is necessary \rightarrow this does not exist in SM.

Neutrino mass terms (Dirac or Majorana) require physics beyond SM: v_R or Higgs-triplet or new mass generation.

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3. Dirac vs. Majorana mass, and the seesaw mechanism

For simplicity we discuss here the case of only one neutrino generation. For 3 generations a diagonalization of the mass matrices is required – this is only a technical complication.

The most general Lorentz invariant mass term has Dirac and Majorana contributions for LH and RH neutrinos:

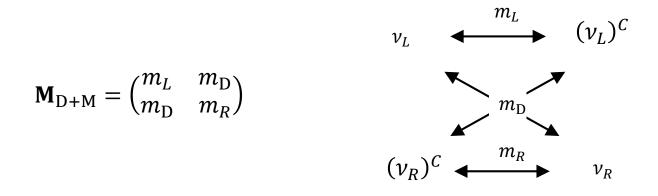
$$\mathcal{L}_{\rm D+M}^{\rm Mass} = -\frac{1}{2}m_L\bar{\nu}_L(\nu_L)^C - m_D\bar{\nu}_L\nu_R - \frac{1}{2}m_R\overline{(\nu_R)^C}\nu_R + h.c.$$

 m_{I} and m_{R} are LH and RH Majorana masses, m_{D} is the Dirac mass.

Introducing the neutrino vector n_L the mass term can be written in matrix form:

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The mass matrix couples the chiral states in the following way:



The chiral fields v_L and $(v_R)^c = v_L^c$ are not the mass eigenstates - these are found by diagonalizing the matrix \mathbf{M}_{D+M} using the orthogonal matrix \mathbf{O} :

$$\mathbf{O} = \begin{pmatrix} \cos \theta & \sin \theta \\ -\sin \theta & \cos \theta \end{pmatrix} \qquad \mathbf{M}_{\mathrm{D+M}} = \mathbf{OM'O^T} \qquad \mathbf{M'} = \mathrm{diag}(m'_1, m'_2)$$

with
$$\tan \theta = \frac{2m_{\mathrm{D}}}{m_R - m_L} \qquad \text{and} \qquad m'_{1,2} = \frac{1}{2}(m_R + m_L) \mp \frac{1}{2}\sqrt{(m_R - m_L)^2 + 4m_{\mathrm{D}}^2}$$

As $m'_{1,2}$ can be positive and negative one rewrites

$$m'_i = \eta_i m_i \text{ with } \eta_i = \pm 1 \text{ and } m_i > 0$$

Taking this into account, one can express the diagonalization of M_{D+M} as

(*)
$$\mathbf{M}_{\mathrm{D+M}} = \mathbf{O}\eta\mathbf{M}\mathbf{O}^T = U\mathbf{M}U^T$$

with $\mathbf{M} = \operatorname{diag}(m_1, m_2)$ and $U = \sqrt{\eta}O = \operatorname{unitary matrix}$

For the neutrino mass eigenstates one now finds from (*):

$$(* *) \qquad \nu^{M} = U^{\dagger} n_{L} + \left(U^{\dagger} n_{L} \right)^{C} = \begin{pmatrix} \nu_{1} \\ \nu_{2} \end{pmatrix}^{C}$$

and thus
$$\mathcal{L}_{D+M} = -\frac{1}{2}\bar{\nu}^{M}\mathbf{M}\nu^{M} = -\frac{1}{2}\sum_{i=1}^{2}m_{i}\bar{\nu}_{i}\nu_{i}$$

Evidently $(v_i)^c = v_i \rightarrow$ mass eigenstates are Majorana neutrinos.

Using (* *) one obtains the following mixing equation:

$$\nu_L = \sqrt{\eta_1} \cos \theta \, \nu_{1,L} + \sqrt{\eta_2} \sin \theta \, \nu_{2,L}$$
$$(\nu_R)^C = -\sqrt{\eta_1} \sin \theta \, \nu_{1,L} + \sqrt{\eta_2} \cos \theta \, \nu_{2,L}$$

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The parameter η_i determines the CP parity of the Majorana neutrino v_{i} 13

Seesaw mechanism: (simplest case, for one neutrino family)

The seesaw mechanism was proposed at the end of the 1970s and is based on the Dirac and Majorana mass terms. It is a natural and viable way to generate neutrino masses.

The three parameters m_L , m_R , and m_D characterize the LH and RH Majorana mass terms and the Dirac mass term. The mass eigenstates characterized by m_1 and m_2 are Majorana states (see above).

Assumptions:

- 1. There is no LH Majorana mass term
- 2. Dirac mass term generated by a SM Higgs coupling $\rightarrow m_{\rm D}$ is of the order of a lepton or quark mass.
- 3. RH Majorana mass term \neq 0 for neutrino N_R , breaks lepton number conservation: we assume that this happens at a mass scale M_R much larger than the electroweak scale:

$$m_R \equiv M_R >> M_W$$
, $M_Z >> m_D$

One obtains for the mass eigenvalues (see above):

$$m_1 \approx \frac{m_D^2}{m_R} = \frac{m_D^2}{M_R} << m_D \qquad m_2 \approx M_R >> m_D \qquad m_{1,2}' = \frac{1}{2}(m_R + m_L) \mp \frac{1}{2}\sqrt{(m_R - m_L)^2 + 4m_D^2}$$
see p. 11 14

With the mixing angle $\theta \approx \frac{m_{\rm D}}{M_R} << 1$ and $\eta_1 = -1$ and $\eta_2 = +1$:

 \implies mixing relations:

$$\nu_L = i\nu_{1,L} + \frac{m_{\rm D}}{M_R}\nu_{2,L}$$

$$(N_R)^C = -i \frac{m_D}{M_R} v_{1,L} + v_{2,L}$$

For the physical states one obtains (up to phases):

 $\nu_1 \approx \nu_L$ LH neutrino w/ low mass \rightarrow active

 $v_2 \approx N_R$ RH neutrino w/ high mass \rightarrow sterile

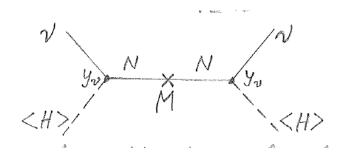
Estimation of scale M_R:

$$m_{\rm D} \le m_t \approx 170 {
m GeV}$$

$$\begin{split} m_{1} \approx \sqrt{\Delta m^{2}} \Big|_{\substack{\text{heaviest} \\ \text{neutrino}}} \approx 5 \cdot 10^{-2} \text{eV} \\ \hline M_{R} \approx \frac{m_{D}^{2}}{m_{1}} \approx 10^{15} \text{GeV} \end{split}$$

Thus, the seesaw mechanism explains why the neutrinos which we observe are so light. The energy scale M_R far exceeds the energies colliders can reach. The Majorana mass term can be generated through BSM extensions of the Standard Model:

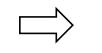
Interaction of "lepton-Higgs pairs" with a heavy Majorana singlet fermion N_R . Due to the "decoupling" of the heavy neutrino the virtual exchange of N_R leads to an effective dimension five operator (gauge invariant) with only SM fields:



(only dim-5 operator which breaks lepton number at tree-level)

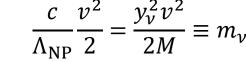
$$\mathcal{L}_{eff} \sim \frac{C}{\Lambda_{\rm NP}} (\bar{L}_L \tilde{\phi}) (\tilde{\phi}^T L_L^C) + h.c.$$
$$L_L = \begin{pmatrix} \nu_L \\ \ell_L \end{pmatrix} \qquad \tilde{\phi} = \sigma_2 \phi = \sigma_2 \begin{pmatrix} \phi^+ \\ \phi^0 \end{pmatrix}$$

After symmetry breaking



In the limit $M \rightarrow \infty$, where N_{R} decouples, neutrinos are effectively massless.

 $\Box \sum \mathcal{L}_{eff} \sim \frac{c}{\Lambda_{\rm NP}} \frac{v^2}{2} v_L v_L^C + h.c.$ $\Box \sum \frac{c}{\Lambda_{\rm NP}} \frac{v^2}{2} = \frac{y_\nu^2 v^2}{2M} \equiv m_\nu$



We notice that a theory where New Physics is composed of heavy sterile neutrinos, provides a specific example of a theory which at low energy contains three light mass eigenstates with an effective dim-5 interaction with $\Lambda_{\rm NP} = M$. In this case the New Physics scale is the characteristic mass scale of the heavy sterile neutrinos.

If the seesaw is realized in nature:

- Neutrinos are Majorana particles
- Neutrino masses are much smaller than lepton and quark masses
- Sterile heavy Majorana particle the seesaw partner must exist.

<u>Question:</u>

If neutrinos are Majorana particles $v = \overline{v}$ why does the reaction

$$\bar{\nu} + n \rightarrow e^- + p$$

not exist?

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Question:

If neutrinos are Majorana particles $v = \overline{v}$ why does the reaction

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not exist? \rightarrow only the LH component of $\nu = \overline{\nu}$ can interact in the weak charged current reaction: strong helicity suppression (see below).

Neutrino mixing for Majorana neutrinos:

The weak eigenstates v_{α} which by default are the states produced in the weak CC interaction of a charged lepton ℓ_{α} (flavor eigenstates) are the linear combinations of the mass eigenstates v_i determined by the PMNS mixing matrix U:

$$|\nu_{\alpha}\rangle = \sum_{i=1}^{3} U_{\alpha i}^{*} |\nu_{i}\rangle$$

While for Dirac neutrinos the PMNS mixing matrix is given by three mixing angles and one phase δ ,

$$U = \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{pmatrix} \begin{pmatrix} c_{13} & 0 & s_{13}e^{-i\delta_{CP}} \\ 0 & 1 & 0 \\ -s_{13}e^{i\delta_{CP}} & c_{13} \end{pmatrix} \begin{pmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix},$$

for Majorana neutrinos there are two additional Majorana phases which cannot be absorbed in the redefinition of the neutrino states:

$$U = \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{pmatrix} \begin{pmatrix} c_{13} & 0 & s_{13}e^{-i\delta_{CP}} \\ 0 & 1 & 0 \\ -s_{13}e^{i\delta_{CP}} & c_{13} \end{pmatrix} \begin{pmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} e^{i\phi_1} & 0 & 0 \\ 0 & e^{i\phi_2} & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

(there are different conventions; here the PDG convention)

4. Neutrino oscillations

If neutrinos have masses and lepton flavors are mixed by weak CC interactions, then lepton flavor is not conserved in neutrino propagation.

This phenomenon is usually referred to as neutrino oscillations. In brief, a weak eigenstate v_{α} which by default is the state produced in the weak CC interaction of a charged lepton ℓ_{α} , is the linear combination determined by the mixing matrix U

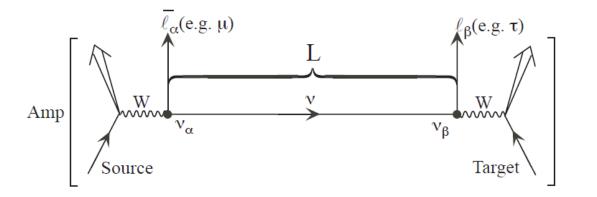
$$|\nu_{\alpha}\rangle = \sum_{i=1}^{3} U_{\alpha i}^{*} |\nu_{i}\rangle$$
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Where v_i are the mass eigenstates

Neutrino oscillations in vacuum

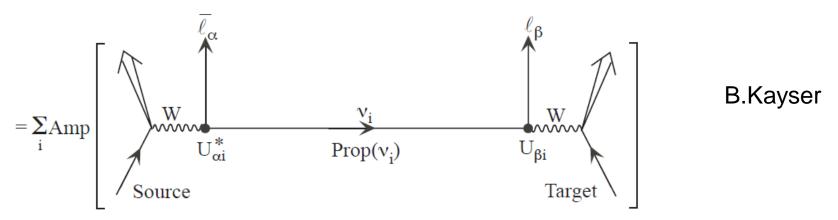
(follows a derivation by Boris Kayser)

A neutrino produced with flavor v_{α} in the source can thus interact as v_{β} in the target:



B.Kayser

Neutrino propagation: mass states



Assumption:

Coherent mass states propagate as plane waves: $|v_i(t,x)\rangle = |v_i(0)\rangle \exp(-ip_\mu x^\mu)$

The amplitude $A(\nu_{\alpha} \rightarrow \nu_{\beta})$ for oscillation, i.e. the amplitude that a ν_{α} produced in the source is detected as ν_{β} in the target is given by:

$$A(\nu_{\alpha} \to \nu_{\beta}) \sim \sum_{i} A(W \to \bar{\ell}_{\alpha} \nu_{i}) \operatorname{Propagator}(\nu_{i}) A(\nu_{i} \to \ell_{\beta} W)$$
$$\sim \sum_{i} U_{\alpha i}^{*} \cdot \operatorname{Propagator}(\nu_{i}) \cdot U_{\beta i}$$

The propagator $\sim \exp(ip_{\mu}x^{\mu})$ describes the neutrino propagation along some distance L and is given in the lab frame by $\exp(-i(E_it - p_iL))$, where t is the flight time from the source to the target at distance L. E_i and p_i are the energy and the momentum in the lab frame. That is, each mass eigenstate v_i picks up the phase factor $\phi_i = -i(E_it - p_iL)$

As the oscillation probability is given by $P_{\alpha\beta} = |A(\nu_{\alpha} \rightarrow \nu_{b})|^{2}$ only the <u>relative</u> phase differences between the different propagation phases are relevant:

$$\Delta \phi_{ij} = -(E_i t - p_i L) + (E_j t - p_j L) = (p_i - p_j)L - (E_i - E_j)t$$

In practice experiments do not measure *t*. Instead *t* is replaced by L/\bar{v} where \bar{v} is the average velocity of the 2 neutrino mass states.

$$\bar{v} = \frac{p_1 + p_2}{E_1 + E_2}$$
 (C=1)

One obtains then for the phase difference:

$$\Delta \phi_{ij} = \frac{p_i^2 - p_j^2}{p_i + p_j} L - \frac{E_i^2 - E_j^2}{p_i + p_j} L = \frac{m_j^2 - m_i^2}{p_i + p_j} L = \frac{\Delta m_{ij}^2}{2E} L$$

where we have used that for highly relativistic neutrinos p_1 and p_2 can be approximated by the neutrino beam energy $E_1 \approx E_1 \approx E$ (minor differences play no role in the sum) Thus the <u>relative</u> phases in $A(\nu_{\alpha} \rightarrow \nu_{\beta})$ between the neutrinos are correct if we take as propagator:

$$Propgator(v_i) = \exp\left(im_i^2 \frac{L}{2E}\right)$$

For the transition amplitude $A(\nu_{\alpha} \rightarrow \nu_{\beta})$ one thus obtains:

$$A(\nu_{\alpha} \to \nu_{\beta}) = \sum_{i} U_{\alpha i}^{*} \exp\left(im_{i}^{2} \frac{L}{2E}\right) U_{\beta i}$$

The oscillation probability $P(\nu_{\alpha} \rightarrow \nu_{\beta})$ is then obtained from $|A(\nu_{\alpha} \rightarrow \nu_{\beta})|^2$ and exploiting unitarity:

$$P(\nu_{\alpha} \rightarrow \nu_{\beta}) = |A(\nu_{\alpha} \rightarrow \nu_{\beta})|^{2} = \delta_{\alpha\beta} - 4 \sum_{i,j:i>j} \Re\{U_{\alpha i}^{*}U_{\beta i}U_{\alpha j}^{*}U_{\beta j}\}\sin\left(\Delta m_{ij}^{2}\frac{L}{2E}\right)$$

$$+2 \sum_{i,j:i>j} \Im\{U_{\alpha i}^{*}U_{\beta i}U_{\alpha j}^{*}U_{\beta j}\}\sin\left(\Delta m_{ij}^{2}\frac{L}{2E}\right)$$
While for anti-neutrinos:
$$P(\bar{\nu}_{\alpha} \rightarrow \bar{\nu}_{\beta}) = \dots \qquad \text{with "-" sign}$$

(complex conj. PMNS matrix elements)

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Excursus: Majorana-Phases:

For Majorana neutrinos:

rana neutrinos:

$$U_{PMNS} = V_{PMNS} \cdot \operatorname{diag}(e^{i\eta_1}, e^{i\eta_2}, 1) = \begin{pmatrix} e^{i\eta_1}U_{e_1} & e^{i\eta_2}U_{e_2} & U_{e_3} \\ e^{i\eta_1}U_{\mu_1} & e^{i\eta_2}U_{\mu_2} & U_{\mu_3} \\ e^{i\eta_1}U_{\tau_1} & e^{i\eta_2}U_{\tau_2} & U_{\tau_3} \end{pmatrix}$$

the additional phases leave the combinations $U_{\alpha i}^* U_{\beta i} U_{\alpha j}^* U_{\beta j}$ invariant.

The Majorana phases do not change mixing (no additional CP violation)

Majorana phases are only observable in processes which change the lepton number by two units. Neutrino mixing changes the flavor.

 \rightarrow Majorana phases are not visible, and for now not constrained.

CP-violation in neutrino mixing:

Jarlskog invariant (cf. CKM for quarks):

$$J_{CP} = \Im \{ U_{\alpha i}^* U_{\beta i} U_{\alpha j}^* U_{\beta j} \} \neq 0 \qquad \Longleftrightarrow \qquad P(\nu_{\alpha} \to \nu_{\beta}) \neq P(\bar{\nu}_{\alpha} \to \bar{\nu}_{\beta})$$

i.e. if U_{PMNS} is complex ($\delta_{CP} \neq 0, \pi$).

Usage of SI-units:

The expression
$$\left(\Delta m_{ij}^2 \frac{L}{2E}\right)$$
 uses natural units. Use \hbar and c to

transform to SI-units:

$$\Delta m_{ij}^2 \frac{L}{2E} \to 1.27 \cdot \Delta m_{ij}^2 [\text{eV}^2] \frac{L[\text{km}]}{2E[\text{GeV}]} \qquad (\text{an often-used} \\ \text{expression})$$

Example: Experiments studying 1 GeV neutrinos travelling L \approx 10⁴ km is sensitive to m_{ij}² – splitting as small as ~10⁻⁴ eV² (Sensitivity of atmospheric neutrinos passing the earth)

Some remarks on the derivation of the mixing formula:

Many text books use either equal energy or equal momentum assumption:

$$\Delta \phi_{ij} = -(E_i t - p_i L) + (E_j t - p_j L) = (p_i - p_j)L - (E_i - E_j)t$$

Equal energy: $E_i = E_j = E$ and $p_i = \sqrt{E^2 - m_i^2} = E - \frac{m_i^2}{2E}$
 $\Delta \phi_{ij} = (p_i - p_j)L - (E_i - E_j)t = \frac{m_i^2 - m_j^2}{2E}L = \frac{\Delta m_{ij}^2}{2E}L$
Equal momentum: $p_i = p_j = p$ and $E_i = \sqrt{p^2 + m_i^2} = p - \frac{m_i^2}{2p}$
 $\Delta \phi_{ij} = (p_i - p_j)L - (E_i - E_j)t = \frac{-(m_i^2 - m_j^2)}{2p}t = \frac{\Delta m_{ij}^2}{2E}L$

(where in the last equality L=ct and pc=E has been used)

It turns out that neither the equal momentum nor the equal energy ansatz is correct (see e.g. E. Akhmedov arXiv:1901.05232v1).

Most derivations (including ours) use a plane-wave treatment for the propagation of the neutrino - instead a wave-packet ansatz is needed (see arXiv:1901.05232v1) However, a correct treatment using wave-packages results in the same formula. ₂₆ Plane wave: no spatial localization. Cannot describe creation at source and conversion at target.

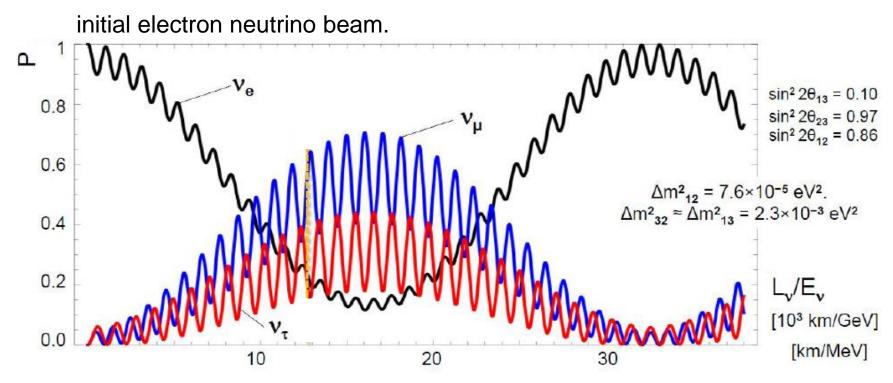
Three neutrino oscillation:

Formula is quite complex

$$P(\nu_{\alpha} \to \nu_{\beta}) = \left| U_{\alpha 1} U_{\beta 1}^{*} + U_{\alpha 2} U_{\beta 2}^{*} \exp\left(-i\frac{\Delta m_{21}^{2}}{2E}L\right) + U_{\alpha 3} U_{\beta 3}^{*} \exp\left(-i\frac{\Delta m_{31}^{2}}{2E}L\right) \right|^{2}$$

It depends on two Δm^2 with three angles $\theta_{12}, \theta_{23}, \theta_{13}$ and one CPV phase. Assume:

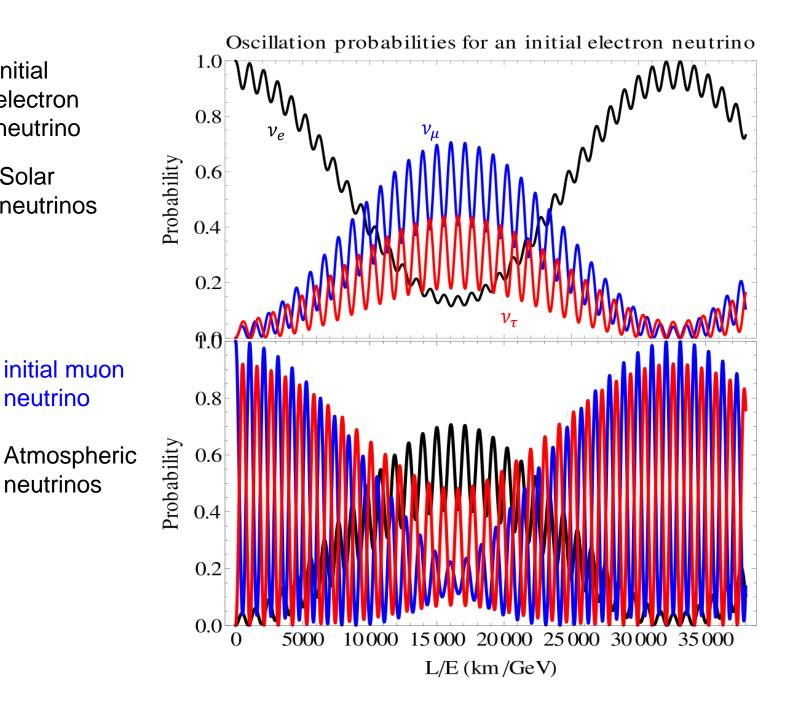
$$\Delta m_{21}^2 \ll \Delta m_{31}^2 \approx \Delta m_{32}^2$$



initial electron neutrino

Solar neutrinos

neutrino



Summary of neutrino oscillations in vacuum:

- if we observe oscillations:
 - $\Rightarrow \Delta m_{ij}^2 \neq 0 \Rightarrow m_i \text{ or } m_j \neq 0$
 - U_{PMNS} is non diagonal. (\rightarrow mixing)
- Oscillation provides access to very small Δm_{ij}^2
- Observation of neutrino oscillation in two ways: disappearance of ν_{α} or appearance of ν_{β}
- Neutrinos oscillation does not alter the total v-flux: $\sum_{\nu_{\beta}} P(\nu_{\alpha} \rightarrow \nu_{\beta}) = 1$
 - However, if some of v_{β} are "sterile flavors" (no weak interactions,) then the total flux of the active neutrinos (v_e , v_{μ} , v_{τ}) is reduced.

<u>Measurement of θ_{13} </u>

$$U = \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{pmatrix} \begin{pmatrix} c_{13} & 0 & s_{13}e^{-i\delta_{CP}} \\ 0 & 1 & 0 \\ -s_{13}e^{i\delta_{CP}} & c_{13} \end{pmatrix} \begin{pmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

Atmospheric reactor neutrinos; Solar neutrino mixing; KamLAND
accelerator neutrinos $\Delta m_{atm}^2 \sim 2.4 \cdot 10^{-3} \text{eV}^2$
 $\theta_{23} \sim 49^o$ $\theta_{13} \sim 9^o$ $\theta_{12} \sim 33^o$

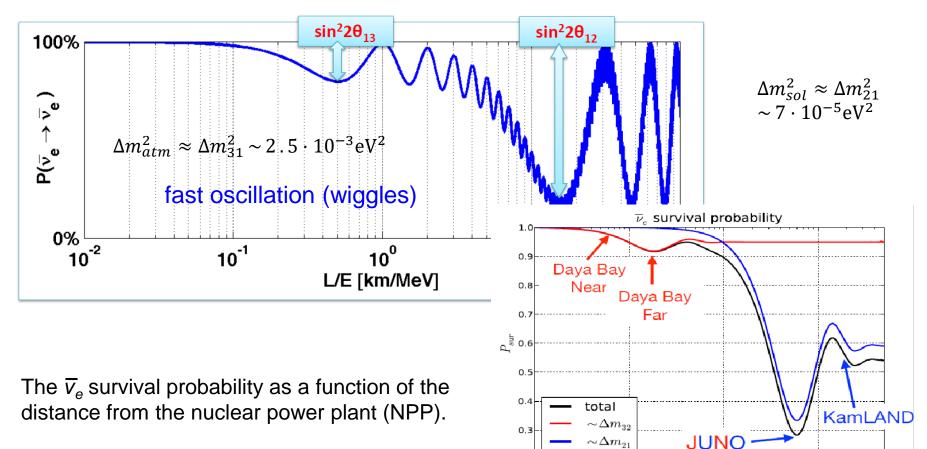
To observe CP violation in neutrino mixing a finite value of $sin^2\theta_{13}$ is necessary.

 $|\Delta m_{32}^2| \sim |\Delta m_{31}^2|$...but sign unknown $\delta_{CP} \sim 200^o$ (indirectly)

$\underline{\theta}_{13}$ with reactor neutrinos:

Survival probability for 3-neutrino mixing:

$$P_{ee} \approx 1 - \sin^2 2\theta_{13} \sin^2 \left(\frac{\Delta m_{31}^2 L}{4E_v} \right) - \cos^4 \theta_{13} \sin^2 2\theta_{12} \sin^2 \left(\frac{\Delta m_{21}^2 L}{4E_v} \right)$$



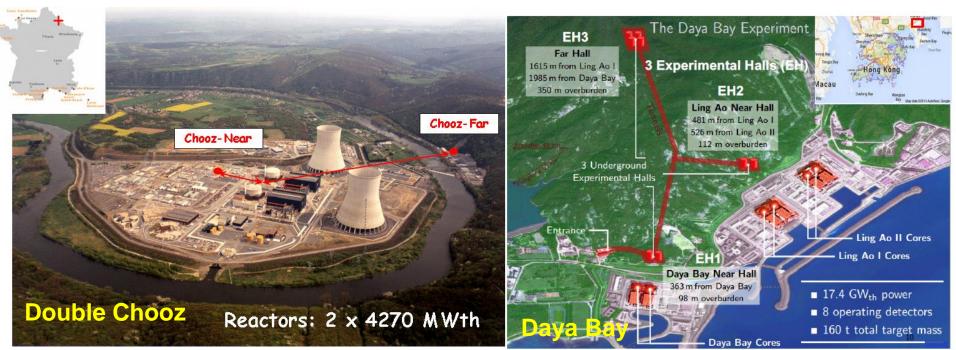
0.2L

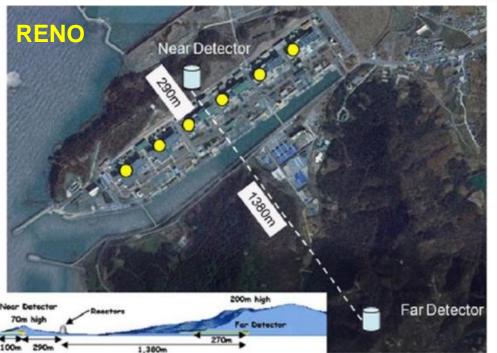
1

10

L, km

100



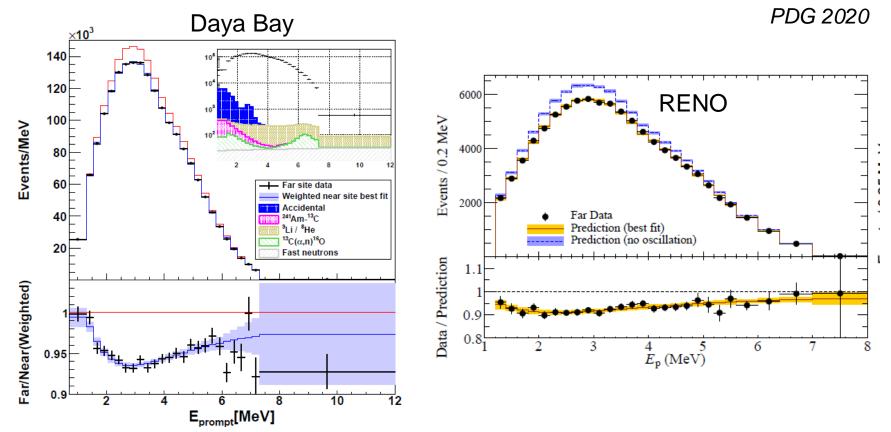


(China)

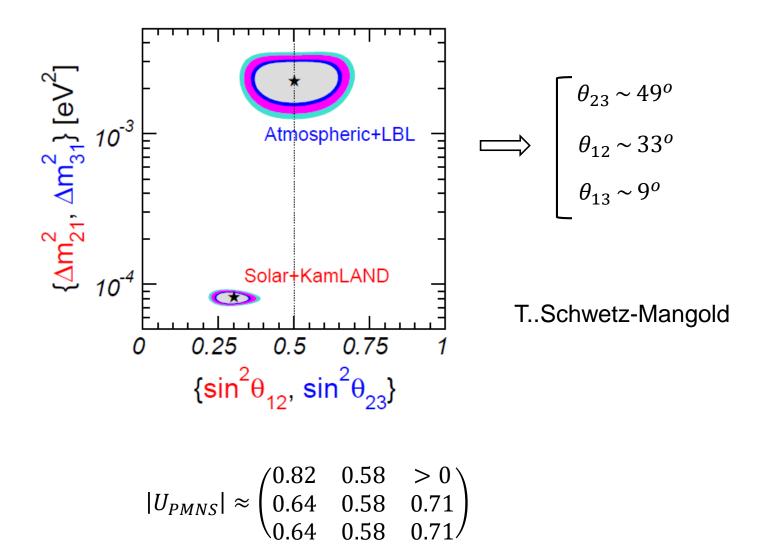
All experiments have a "near" detector to monitor the neutrino flux and a "far" (typ. Distance 1.5 km) to measure the deficit.

(South Korea)

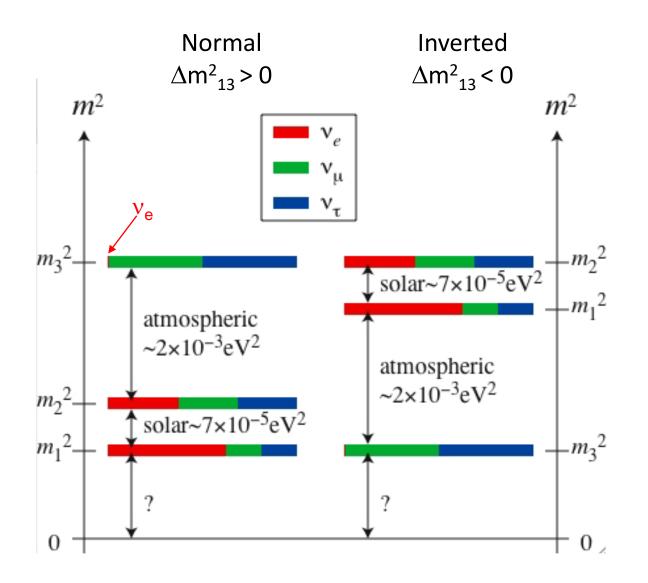
The 3 reactor neutrino experiments published first results in 2012: Double Chooz reported an indication of electron antineutrino disappearance with the ratio of observed to expected events of R= $0.944\pm0.016\pm0.04$ ruling out the no-oscillation hypothesis at 94.6% CL. Daya Bay observed of R= $0.940\pm0.011\pm0.004$ corresponding to 5.2σ of a non-zero value of θ_{13} . RENO reported R= $0.920\pm0.000\pm0.014$ indicating a non-zero value of θ_{13} with a significance of 4.9σ .



Summary: Neutrino Mixing



Summary: Neutrino masses



5. Neutrino mass scale determination

For massive neutrinos the flavor states are linear combinations of the mass states. Mass limits can only be put on the <u>effective mass</u> of a neutrino with lepton flavor ℓ :

$$m_{\nu_{\ell},eff}^2 = \sum_i |U_{\ell i}|^2 m_i^2$$

Upper bounds on neutrino masses can be deduced from weak decays:

${}^{3}\text{H}_{2} \rightarrow {}^{3}\text{He} {}^{3}\text{H}^{+} + e^{-} + \bar{\nu}_{e}$ PDG 2024	
$(n \to p + e^- + \bar{\nu}_e)$ $m_{\bar{\nu}_e, eff} < 0.8 \text{ eV}$	
$\mu^{\pm} \rightarrow \nu_{\mu} + e^{\pm} + \nu_{e} \qquad m_{\nu_{\mu}, eff} < 0.19 \text{MeV}$	<u>}</u>
$\tau^{\pm} \rightarrow n \cdot \pi + \nu_{\tau} \qquad m_{\nu_{\tau}, eff} < 18.2 \mathrm{MeV}$	

Study energy distribution of visible final-state particles: "missing" invariant mass → neutrino mass

Upper bounds also exist from cosmology:

Large scale structure of galaxies, cosmic microwave background, type la supernovae, and big bang nucleosynthesis:

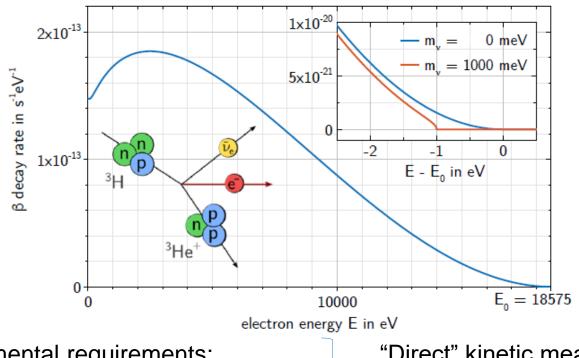
$$\sum m_i < 0.26 \text{eV} \quad \text{arXiv:1811.02578v2}_{36}$$

a) Effective electron anti-neutrino mass:

End-point method of a β -emitter (tritium, ³H)

$$\frac{dN}{dE} = Cp(E + m_e)(E_0 - E)\sqrt{(E_0 - E)^2 - (m_{\nu_e}^{eff})^2} \cdot F(Z, E)$$
$$\equiv R(E)\sqrt{(E_0 - E)^2 - (m_{\nu_e}^{eff})^2}$$

 E_0 = Mass diff. of nuclei E = kin. energy of electron P = e⁻ momentum F: Fermi function



Experimental requirements:

- High activity source
- Excellent energy resolution

"Direct" kinetic measurement: spectral distortion measures the "effective" mass squared: Effective neutrino mass – consider mixing:

$$\frac{dN}{dE} = R(E)\sqrt{(E_0 - E)^2 - (m_{\nu_e}^{eff})^2} \quad \text{with:} \quad m_{\nu_e, eff}^2 = \sum_i |U_{ei}|^2 m_i^2$$

The KATRIN experiment has provided an upper bound for the effective neutrino mass:

$$0.8 \text{ eV} \ge m_{\nu_e, eff} = \sqrt{\sum_i |U_{ei}|^2 m_i^2}$$

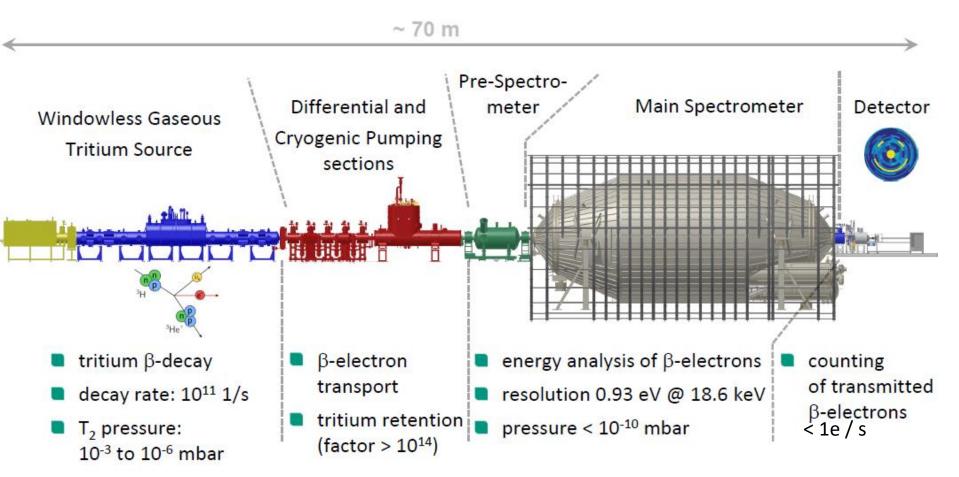
Г

Depending on the neu hierarchy, this leads to dence on the light neu

$$m_{\nu_e}^{\text{eff}} = \sqrt{\sum_{i} m_i^2 |U_{ei}|^2} = \begin{cases} \sqrt{m_0^2 + \Delta m_{21}^2 c_{13}^2 c_{12}^2 - \Delta m_{32}^2 c_{13}^2} & \text{in NO}, \\ \sqrt{m_0^2 + \Delta m_{21}^2 c_{13}^2 c_{12}^2 - \Delta m_{32}^2 c_{13}^2} & \text{in IO}, \end{cases}$$

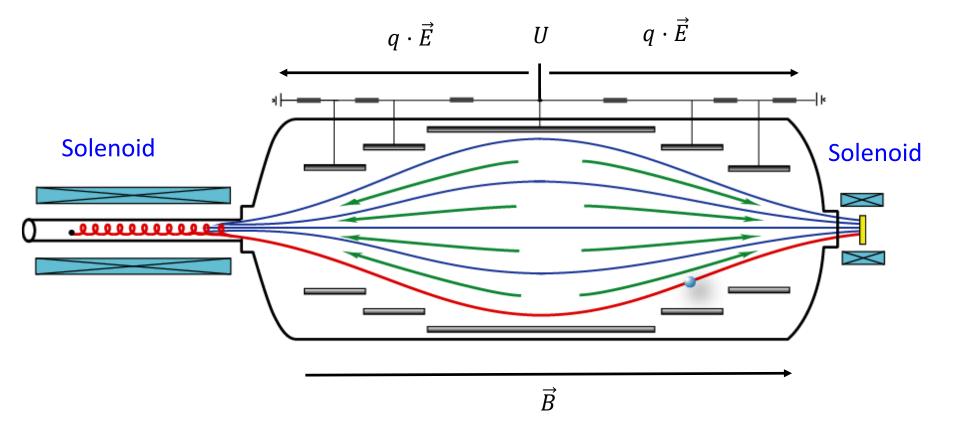
KATRIN = Karlsruhe Tritium Neutrino Experiment

Goal: measure neutrino mass w/ sensitivity of 0.2 eV (90%CL)



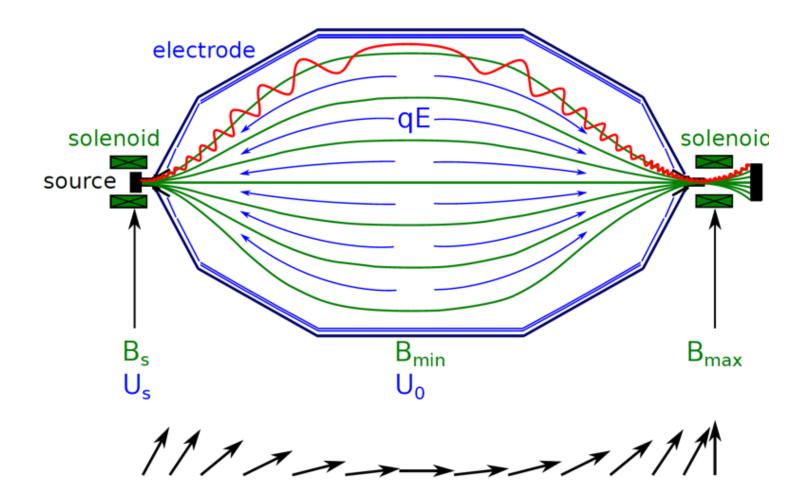
"magnetic adiabatic collimation and electrostatic"

Electrostatic spectrometer:



No electron flux for: $E_{kin} = e \cdot U_{max}$

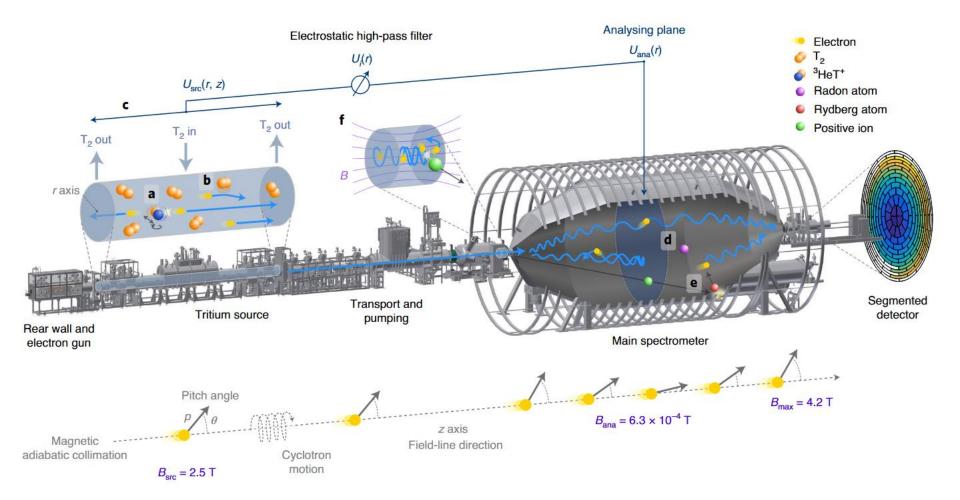
B fields serves to align the electron directions.



Adiabatic variation of B-field leads to alignment of momentum vector.

MAC-E Filter: Principle

B fields serves to align the electron directions.



Adiabatic variation of B-field leads to alignment of momentum vector.



arXiv:1909.06048

KATRIN-Results:

First results from a 4 weeks measurement; Source activity 2.45×10^{10} Bq (Tritium density 1/5 of nominal).

Fit in the interval around the kinematic endpoint at 18.57 keV gives an effective neutrino mass square value of

$$m_{\nu,eff}^2 = (-1.0^{+0.9}_{-1.1}) \text{eV}^2$$

From this an upper limit of

 $m_{\nu,eff} < 1.1 \text{eV} (90\% \text{CL})$

on the absolute mass scale of neutrinos is derived.

Sensitivity after 1000 days of data-taking and nominal tritium density: 0.2 eV

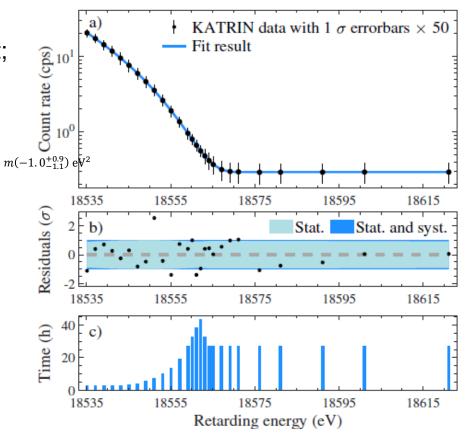


FIG. 3. a) Spectrum of electrons $R(\langle qU \rangle)$ over a 90 eVwide interval from all 274 tritium scans and best-fit model $R_{\rm calc}(\langle qU \rangle)$ (line). The integral β -decay spectrum extends up to E_0 on top of a flat background $R_{\rm bg}$. Experimental data are stacked at the average value $\langle qU \rangle_l$ of each HV set point and are displayed with 1- σ statistical uncertainties enlarged by a factor 50. b) Residuals of $R(\langle qU \rangle)$ relative to the 1- σ uncertainty band of the best fit model. c) Integral measurement time distribution of all 27 HV set points.

KATRIN-Results:

Latest results from 2022: Source activity 9.5×10^{10} Bq (Tritium density nominal).

Fit in the interval around the kinematic endpoint at 18.57 keV gives an effective neutrino mass-squared of:

 $m_{\nu,eff}^2 = 0.26_{-0.34}^{+0.34} \text{ eV}^2$

From this, an upper limit of

 $m_{\nu,eff} < 0.8 \text{ eV} (90\% \text{CL})$ on the absolute mass scale of (electron anti-)neutrinos is derived.

Sensitivity after 1000 days of data-taking and nominal tritium density: 0.2 eV

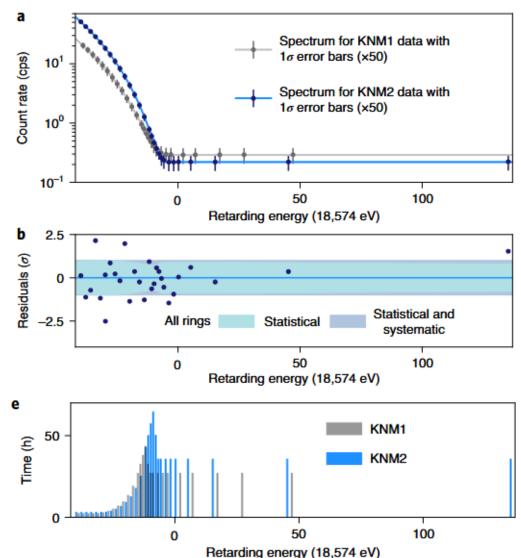
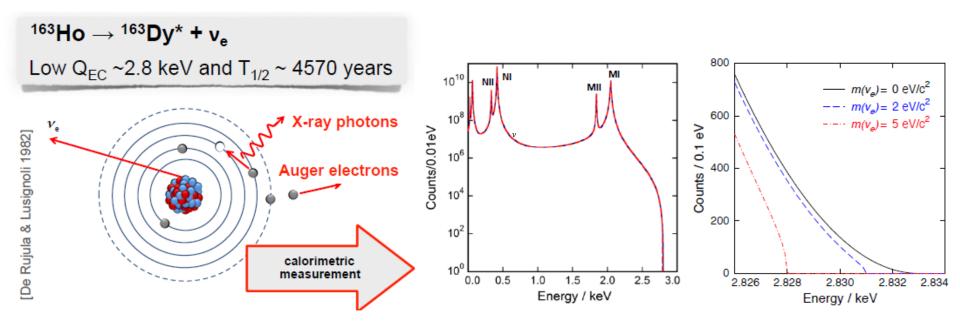


Fig. 2 | Measured rate at each retarding energy for KNM1 (refs. ^{17,18}**) and KNM2 campaigns. a**, Data points with statistical error (multiplied by a factor of 50) and best-fit model (blue and grey lines) individually shown for each campaign. The count rates are summed over all the detector rings.

Holmium Electron Capture:

Slide by K. Valerius

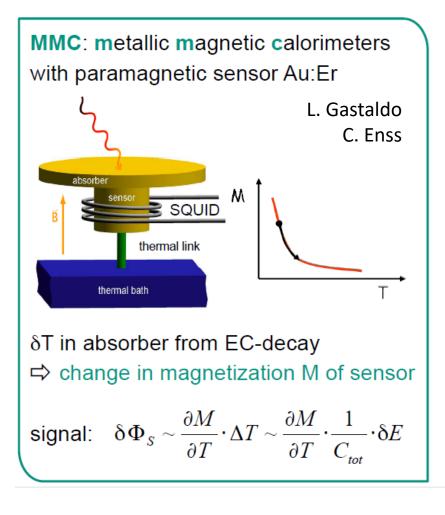


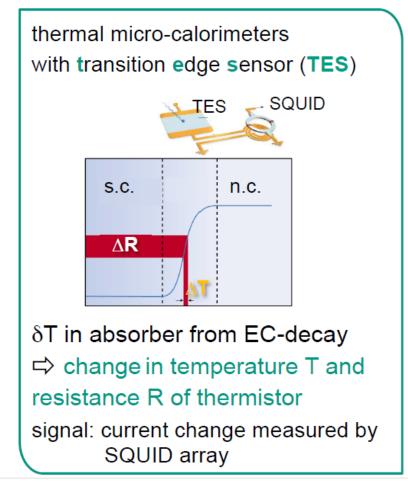
Challenges:

- production & purification of isotope ¹⁶³Ho
- incorporation of ¹⁶³Ho into high-resolution detectors
- operation & readout of large calorimeter arrays
- detailed understanding of calorimetric spectrum (nuclear & atomic physics + detector response)

How to measure 2.8 keV w/ high precision?

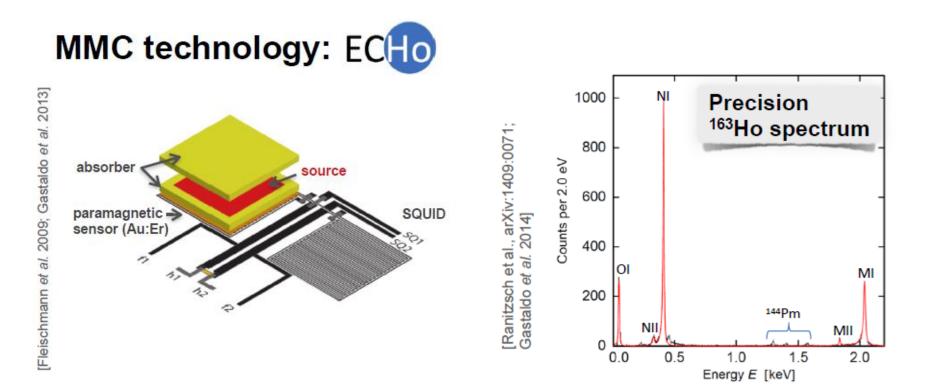
Micro Calorimeters: MMCs





ECHo Experiment

Uni Heidelberg: C. Enss, L. Gastaldo



5. Dirac vs. Majorana: Neutrinoless Double-beta Decay

The problem of the nature of massive neutrinos v_i (Dirac or Majorana?) is one of the most fundamental problems of neutrino physics. The answer to this question will have an important impact on the understanding of the origin of neutrino masses.

The Majorana mass term breaks lepton number by two units - the Majorana mass term is the lowest dimension operator which uses SM fields and obeys SM gauge symmetries and which breaks lepton number at tree-level. In order to reveal the nature of neutrinos with definite masses it is necessary to study processes in which the total lepton number L is violated by two units (i.e., neither neutrino oscillations nor CC interactions can reveal the neutrino nature).

Lepton flavor violation experiments:

• In case of Majorana particle $v = v^{C}$ the following process becomes possible:

$$\pi^+ \to \mu^+ + \nu_i; \quad \nu_i + N \to \mu^+ + p \quad \text{with} \quad A(\nu_i N \to \mu^+ N) \sim \frac{m_\nu}{E_\nu} \to \sigma \sim \left(\frac{m_\nu}{E_\nu}\right)^-$$

neutrino beam

Thus the cross section for observing this reaction in a collider experiment (E_v larger than typ. 1 MeV, $m_v < 1 \text{ eV}$) is suppressed by (×10⁻¹²). This is much too small for observation with current experiments.

• Decays of B or K-mesons. E. g.: $K^+ \rightarrow \pi^- \mu^+ \mu^+$

Experimental bounds:
$$\frac{\Gamma(K^+ \to \pi^- \mu^+ \mu^+)}{\Gamma(K^+ \to \text{ all})} \le 3 \cdot 10^{-9} \implies$$

Limit on the effective mass $|m_{\mu\mu}| < 4 \cdot 10^4 \text{MeV}$ (not very strong) (meaning of "effective mass" : see below)

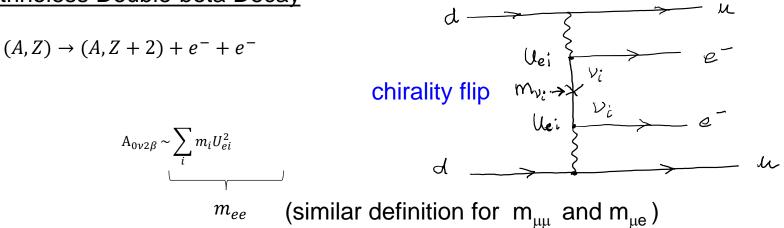
• Processes such as $\mu^- + (A, Z) \rightarrow (A, Z - 2) + e^+$

Experimental bounds:
$$\frac{\Gamma(\mu^{-}\text{Ti} \rightarrow e^{-}\text{Ca})}{\Gamma(\mu^{-}\text{Ti} \rightarrow \text{ all})} \leq 1.7 \cdot 10^{-12} \implies$$

Limit on the effective mass $|m_{\mu e}| < 82 \text{MeV}$ (not very strong) (meaning of "effective mass" : see below)

 The most sensitive probe to whether neutrinos are Dirac or Majorana states is the neutrinoless double-beta decay (0vββ) of a nucleus.

Neutrinoless Double-beta Decay



Under the assumption that the Majorana neutrino mass is the only source of lepton number violation at low energies, the decay half-life is given by:

$$\Gamma_{1/2}^{0\nu} \sim (T_{1/2}^{0\nu})^{-1} = G^{0\nu} |\mathsf{M}^{0\nu}|^2 \left(\frac{m_{ee}}{m_e}\right)^2$$

 G^{0v} is the phase space integral taking into account the final atomic state; \mathcal{M}^{0v} is the nuclear matrix element of the transition;

 m_{ee} is the effective Majorana mass of v_e :

$$m_{ee} = \left| \sum_{i} m_i U_{ei}^2 \right|$$

Note that the term $\sum_{m_i U_{ei}^2}$ is in general complex and depends on the phases of the PMNS elements (δ_{CP} and the two Majorana phases $\eta_{1,2}$)

Thus, in addition to the masses and mixing parameters the decay spectrum depends also on the leptonic CP violating phases (\rightarrow allows determination):

$$m_{ee} = \left| \sum_{i} m_{i} U_{ei}^{2} \right| = \left| m_{1} c_{13}^{2} c_{12}^{2} e^{i2\eta_{1}} + m_{2} c_{13}^{2} s_{12}^{2} e^{i2\eta_{2}} + m_{3} s_{13}^{2} e^{-i2\delta_{CP}} \right|$$

arXiv:1811.05487

One can discuss two different mass orderings:

(inspired by experimental data)

- 1. Normal ordering (NO): $m_1 < m_2 < m_3$; $\Delta m_{12}^2 \ll \Delta m_{23}^2$; $\Rightarrow m_1 < m_2 \ll m_3$
- 2. Inverted ordering (IO): $m_3 < m_1 < m_2$; $\Delta m_{12}^2 \ll |\Delta m_{13}^2|$; $\Rightarrow m_3 \ll m_1 < m_2$

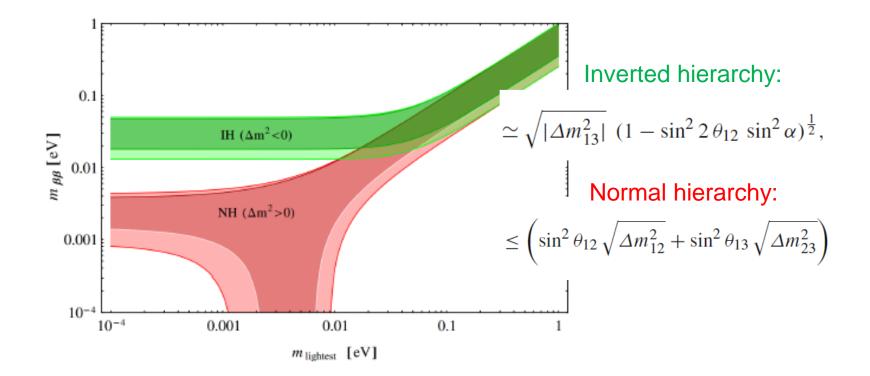
$$\begin{split} m_{ee} &= \left| \sum_{i} m_{i} U_{ei}^{2} \right| \qquad \text{with } m_{0} = m_{1} \text{ (NO), } m_{3} \text{ (IO), smallest mass} \\ &= \left\{ \begin{array}{l} \left| m_{0} c_{12}^{2} c_{13}^{2} + \sqrt{\Delta m_{21}^{2} + m_{0}^{2}} s_{12}^{2} c_{13}^{2} e^{2i(\eta_{2} - \eta_{1})} + \sqrt{\Delta m_{32}^{2} + \Delta m_{21}^{2} + m_{0}^{2}} s_{13}^{2} e^{-2i(\delta_{\rm CP} + \eta_{1})} \right| \quad \text{in NO,} \\ m_{0} s_{13}^{2} + \sqrt{m_{0}^{2} - \Delta m_{32}^{2}} s_{12}^{2} c_{13}^{2} e^{2i(\eta_{2} + \delta_{\rm CP})} + \sqrt{m_{0}^{2} - \Delta m_{32}^{2} - \Delta m_{21}^{2}} c_{12}^{2} c_{13}^{2} e^{2i(\eta_{1} + \delta_{\rm CP})} \right| \quad \text{in IO,} \end{split}$$

$$\begin{bmatrix} \leq \left(\sin^2 \theta_{12} \sqrt{\Delta m_{12}^2} + \sin^2 \theta_{13} \sqrt{\Delta m_{23}^2}\right) & \text{in NO} \\ \simeq \sqrt{|\Delta m_{13}^2|} & (1 - \sin^2 2 \theta_{12} \sin^2 \alpha)^{\frac{1}{2}}, & \text{in IO:} \\ \text{S.Bilenky (2010)} & \alpha \text{ is Matrix} \end{bmatrix}$$

in NO: m_{ee} can me arbitrarily small

in IO: there is a lower bound on m_{ee}_{α} is Majorana phase diff. 52

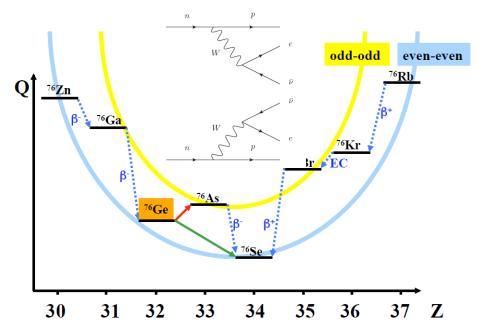
Neutrinoless double beta decay can help to resolve the neutrino mass hierarchy (of course only if neutrinos are Majorana particles):



Searching for neutrinoless double-beta decay:

2β decay:

mass parabola from Weizsäcker formula



Normal β -decay energetically forbidden for ⁷⁴Ge.

Double β -decay allowed: even-even nuclei.

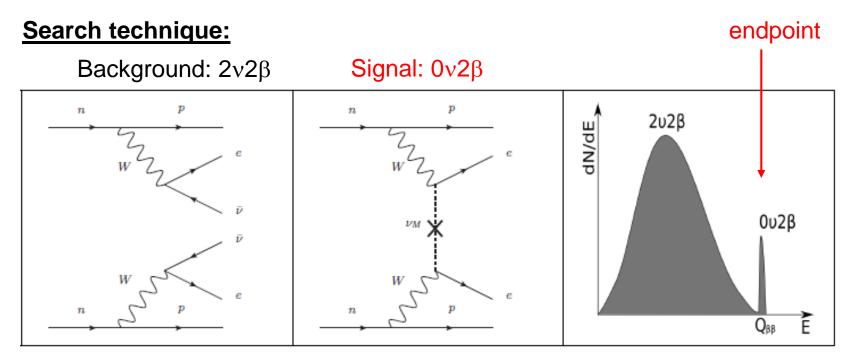
Possible 2β candidates:

Transition	$T_0 = Q_{\beta\beta} \; (\text{KeV})$
$^{76}\text{Ge} \rightarrow ^{76}\text{Se}$	$2,039.6 \pm 0.9$
100 Mo \rightarrow 100 Ru	$3,934 \pm 6$
$^{130}\text{Te} \rightarrow ^{130}\text{Xe}$	$2,533 \pm 4$
136 Xe \rightarrow 136 Ba	$2,479 \pm 8$
150 Nd \rightarrow 150 Sm	$3,367.1 \pm 2.2$
82 Se \rightarrow 82 Kr	$2,995 \pm 6$
48 Ca \rightarrow 48 Ti	$4,271 \pm 4$

 $T_{1/2}^{2\nu}(^{76}\text{Ge}) =$ (1.929 ± 0.095) · 10²¹yr

arXiv:1501.02345

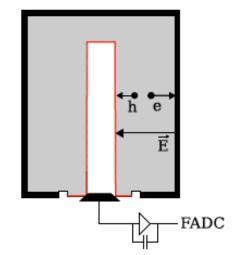
Two-neutrino double β decay is a process of second order in the Fermi constant G_F, which is governed by the standard CC Hamiltonian of the weak interaction. This decay was observed in more than ten different nuclei with half-lives in the range $(10^{18}-10^{24})$ years.



Source = Detector

Decay & detection material ⁷⁶Ge:

- Ge is a 2β decay isotope
- Source material = detector material
- Germanium detectors (=semiconductor) have excellent energy resolution: FWHM ~ 1.5 10⁻³ @ 2 keV
- Enrichment of ⁷⁶Ge up to 86%



Ge diode w/ reverse biasing $_{55}$