

Bennet-Brassard  
protocol

Photon number  
splitting

Decoy state  
QKD

Micius satellite

Entanglement  
distribution

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# Master Seminar: Your passion for physics

## Quantum Key Distribution

Kilian Welz  
Heidelberg University

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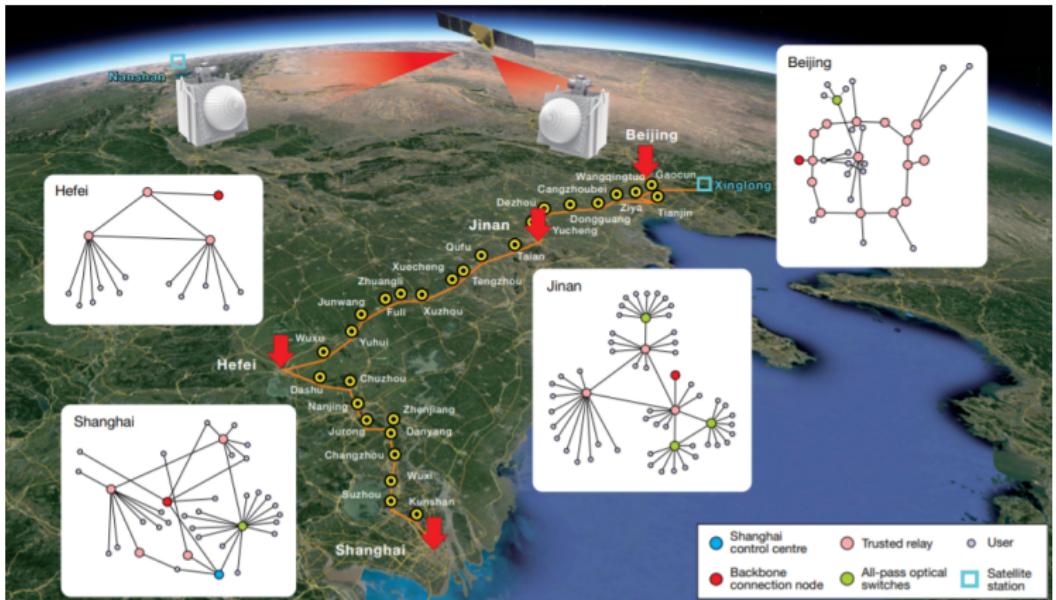


Figure 1: The Shanghai-Beijing integrated space-to-ground quantum network (adapted from [1])

# Quantum Key Distribution methods

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Bennet-Brassard protocol:

- ▶ polarized single photons
- ▶ sent via optical fiber
- ▶ a lot channel loss

Entanglement distribution  
protocol:

- ▶ entangled pairs of  
photons
- ▶ satellite-to-ground link
- ▶ less channel loss

# Outline

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# Bennet-Brassard '84 protocol

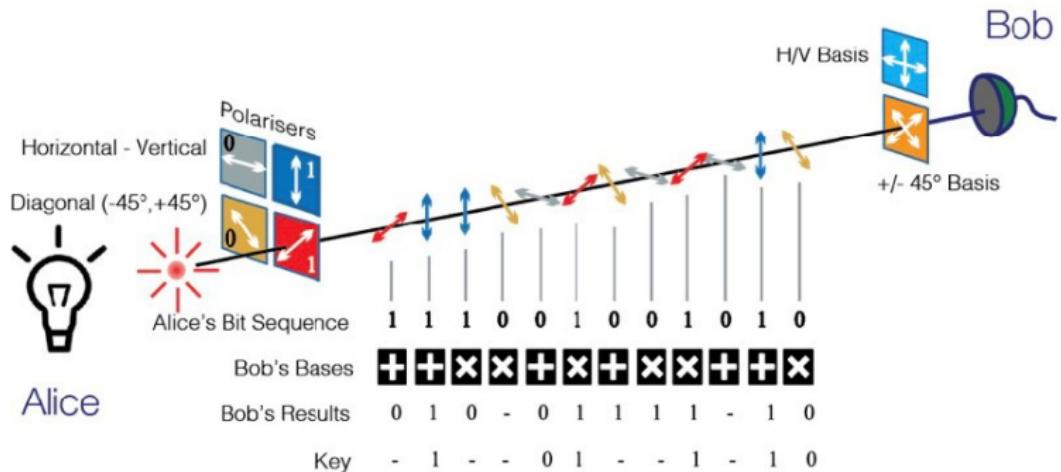


Figure 2: The scheme for the BB'84 protocol (adapted from <https://qt.eu/discover-quantum/underlying-principles/quantum-key-distribution-qkd/>)

1. Send random key in random bases
2. Compare bases publicly
3. Sift key
4. Error correction and verification

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# Bennet-Brassard '84 setup

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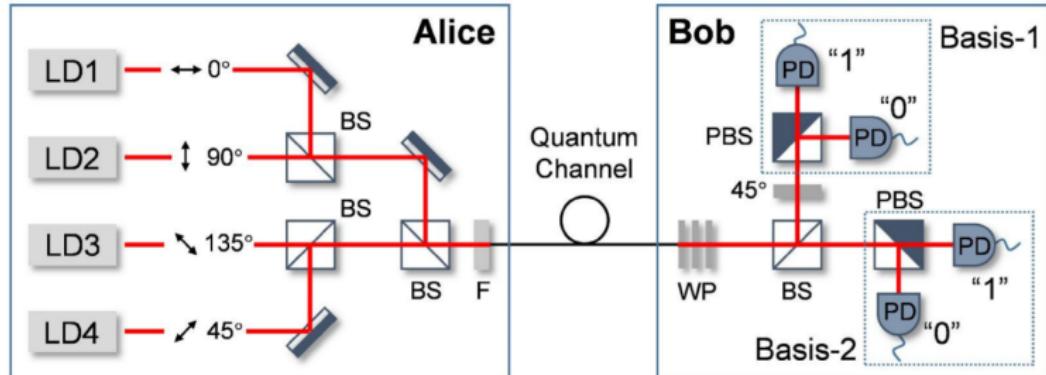


Figure 3: A typical system for BB84 QKD polarization encoding (adapted from [http://www.e-jikei.org/Conf/ICMEMIS2017/proceedings/materials/proc\\_files/GS\\_papers/GS-03/ICMEMIS2017-GS-03.pdf](http://www.e-jikei.org/Conf/ICMEMIS2017/proceedings/materials/proc_files/GS_papers/GS-03/ICMEMIS2017-GS-03.pdf))

- ▶ LD: Laser diode
- ▶ BS: Beam splitter
- ▶ WP: Wave plate
- ▶ PBS: polarizing Beam splitter

# Photon number splitting attack

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$$- \text{coherent laser pulse} : |\alpha\rangle = e^{-|\alpha|^2/2} \sum_{n=0}^{\infty} \frac{\alpha^n}{\sqrt{n!}} |n\rangle \quad (1)$$

$|\alpha|^2$ : average photon number

$|n\rangle$ : n photon Fock-state

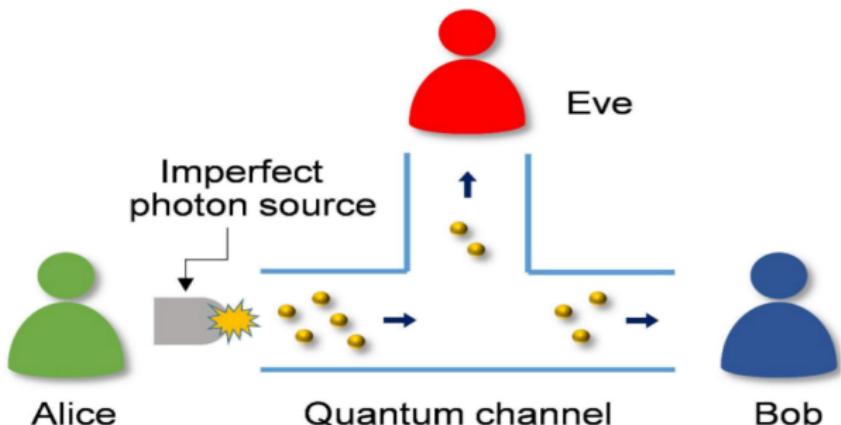


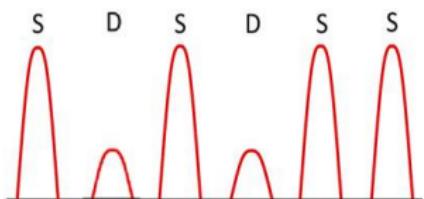
Figure 4: Diagram of Photon Number Splitting attack: PNS attack (adapted from [http://www.e-jikei.org/Conf/ICMEMIS2017/proceedings/materials/proc\\_files/GS\\_papers/GS-03/ICMEMIS2017-GS-03.pdf](http://www.e-jikei.org/Conf/ICMEMIS2017/proceedings/materials/proc_files/GS_papers/GS-03/ICMEMIS2017-GS-03.pdf))

# Decoy state QKD

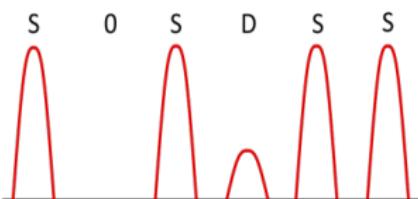
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Distribution

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Alice sends:



Bob receives:



Attenuation with an AOM:

- Signal state
  - ▶  $|\alpha_S|^2 = 0.6$
- Decoy state
  - ▶  $|\alpha_D|^2 = 0.2$

- Eve requires at least 1 photon  
→ *high decoy error rate*

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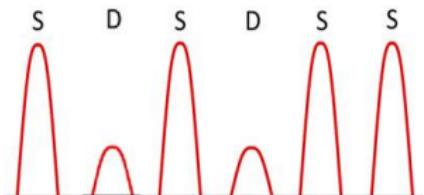
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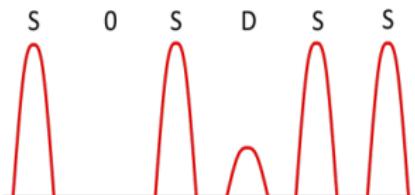
References

# Practical use of decoy state QKD

Alice sends:



Bob receives:



- ▶ Find Eve by comparing error rates (photon number statistics)

Shanghai-Beijing fiber

network:

- pulse rate: 625 MHz
  - key rate: 10-25 kbps
- *only* 1 : $10^4$  photon used

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# Micius satellite

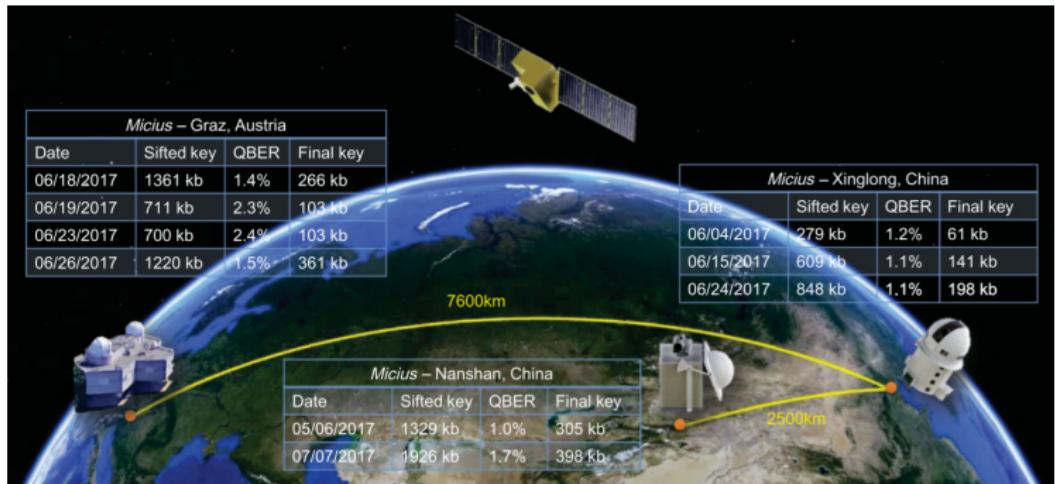


Figure 5: Illustration of the three cooperating ground stations (Graz, Nanshan, and Xinglong) (adapted from <https://arxiv.org/ftp/arxiv/papers/1801/1801.04418.pdf>)

- ▶ Launch: August 2016
- ▶ ca. \$ 100 million
- ▶ quantum optics at a space scale

# Entanglement distribution

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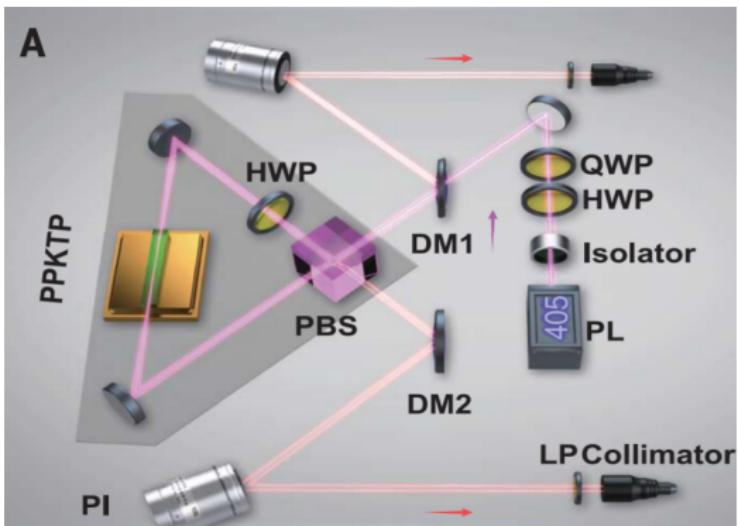


Figure 6: Schematic of the spaceborne entangled-photon source (adapted from [8])

single photon passes through crystal:

- $|\Psi\rangle \rightarrow (|V\rangle_A |H\rangle_B + e^{i\phi} |H\rangle_A |V\rangle_B)/\sqrt{2}$
- 1 photon: 405 nm  $\rightarrow$  2 photons : 810 nm

# Ground-to-space key rates

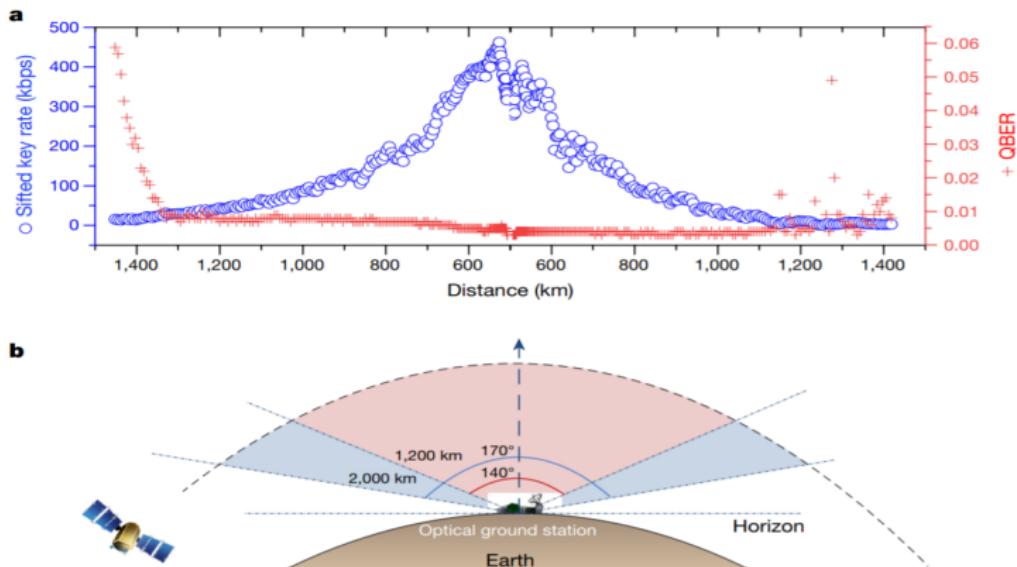


Figure 7: Performance of high-speed satellite-to-ground QKD (adapted from [1])

- pulse rate: 200 MHz
- few photons detected
- sifted key: two-photon coincidence at the ground station
- Quantum bit error rate (QBER): ratio of error rate to key rate

# The Beijing-Shanghai network



Figure 8: Illustration of the backbone network (adapted from  
[https://www.photonics.com/Articles/Quantum\\_Networks\\_Photons\\_Hold\\_Key\\_to\\_Data/a60541](https://www.photonics.com/Articles/Quantum_Networks_Photons_Hold_Key_to_Data/a60541))

- ▶ Megaproject of the 13th five-year plan (2016-2020) of the CCP
- ▶ Micius: "*a satellite for the post-Snowden age*" - Popular Science, 2016
- ▶ 4 Quantum-metropolitan area networks

# Quantum metropolitan-area networks

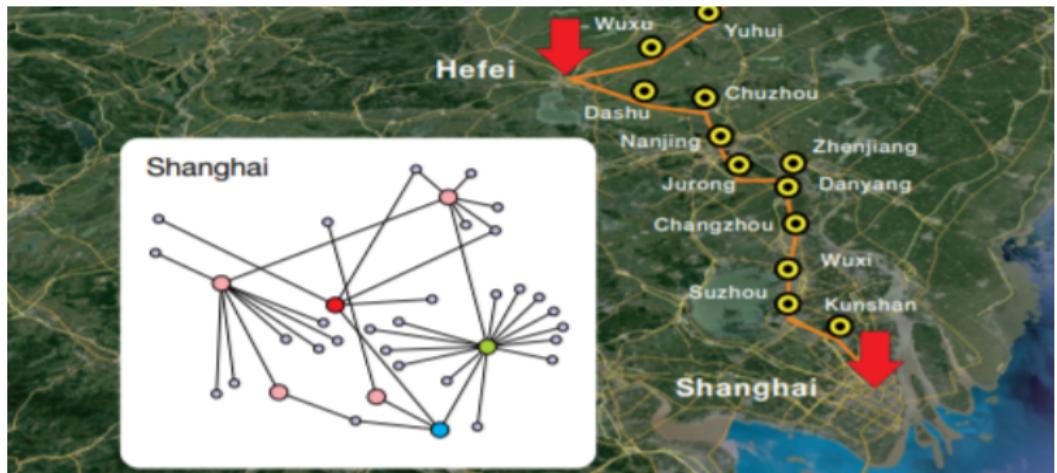
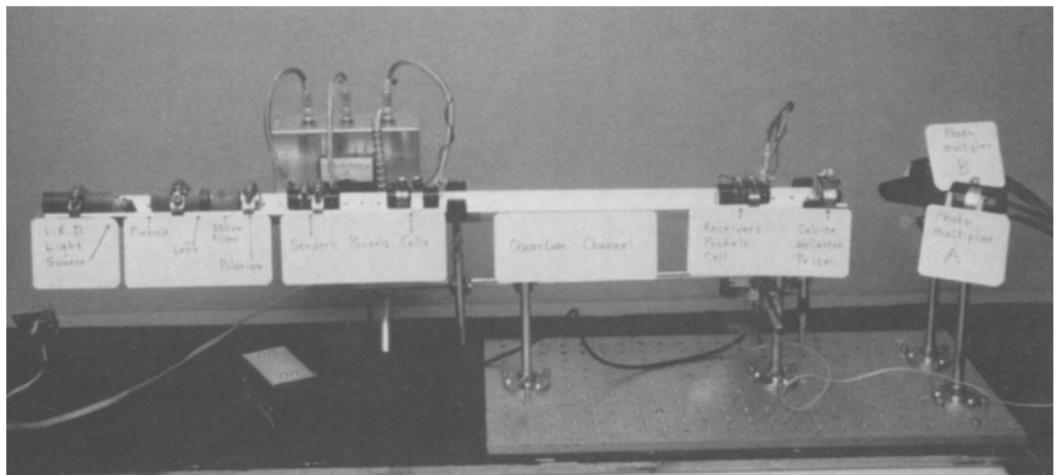


Figure 9: The quantum metropolitan-area network in Shanghai (adapted from [1])

- ▶ 700 fibre links, > 150 users, distances over 2000 km
- ▶ Average Key rates:
  - Metropolitan network: 11.2 - 26.3 kbps
  - backbone network: 79.3 kbps
  - ground-to-space link: 1.1 - 47.8 kbps

# The first setup

Laboratory Implementation achieved in 1992  
by Bennet, Brassard et al.



**Figure 10:** Photograph of the optical setup used in the first QKD experiment (adapted from <https://link.springer.com/content/pdf/10.1007/BF00191318.pdf>)

# Challenges

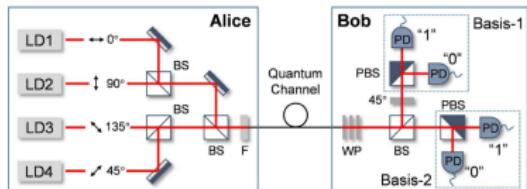
- Costs:
  - ▶ QKD transmitter and receiver modules (>US\$ 100k)
  - ▶ Micius satellite
  - ▶ work hours
- calibrating/ synchronizing/ testing
- establishing protocols:
  - ▶ error correction
  - ▶ automated optimal routing
  - ▶ attack detection (Photon number splitting, Man-in-the-middle, Trojan-horse, denial of service,...)
  - ▶ attack countermeasures



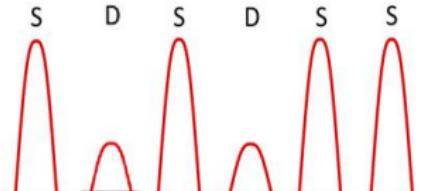
**Figure 11:** InGaAs/InP single-photon detection head (adapted from [http://www.micro-photon-devices.com/  
Products/Photon-Counters/InGaAs-InP](http://www.micro-photon-devices.com/Products/Photon-Counters/InGaAs-InP))

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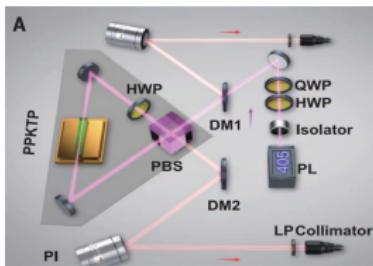
## BB84 protocol:



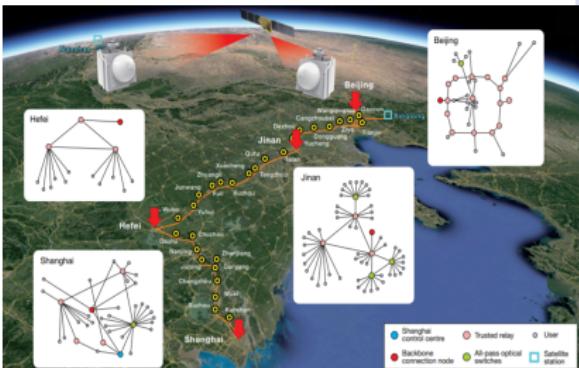
Decoy method:



## Entanglement distribution:



Beijing-Shanghai network:



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# Outlook

- dense wavelength-division multiplexing
- geosynchronous satellite
- weather-independent ground-satellite link
- more efficient protocols
- connecting more national quantum networks
- *global quantum network*

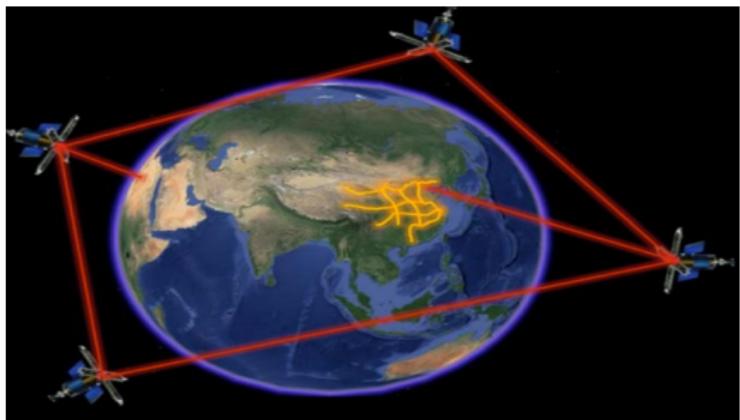


Figure 12: A future global quantum network (adapted from  
<https://iopscience.iop.org/article/10.1088/2058-9565/ab4bea>)

- [1] Yu-Ao Chen et al. "An integrated space-to-ground quantum communication network over 4,600 kilometres". In: *Nature* (2021). DOI: 10.1038/s41586-020-03093-8.
- [2] Charles H. Bennett and Gilles Brassard. "Quantum cryptography: Public key distribution and coin tossing". In: *Theoretical Computer Science* 560 (2014). DOI: <https://doi.org/10.1016/j.tcs.2014.05.025>.
- [3] Sergio L. Castro. "Towards a global space-based QKD network". In: (*Master thesis*) (Jan. 2019). URL: <https://repository.tudelft.nl/islandora/object/uuid%5C%3Ad8a391e8-d21a-4f37-95ec-467a49d391ea>.
- [4] Artur K. Ekert. "Quantum cryptography based on Bell's theorem". In: *Phys. Rev. Lett.* 67 (Aug. 1991). DOI: 10.1103/PhysRevLett.67.661.
- [5] Kevin Günthner et al. "Quantum-limited measurements of optical signals from a geostationary satellite". In: *Optica* 4 (June 2017). DOI: 10.1364/OPTICA.4.000611.
- [6] Won-Young Hwang. "Quantum Key Distribution with High Loss: Toward Global Secure Communication". In: *Phys. Rev. Lett.* 91 (5 Aug. 2003). DOI: 10.1103/PhysRevLett.91.057901.

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