

Reaching low temperatures

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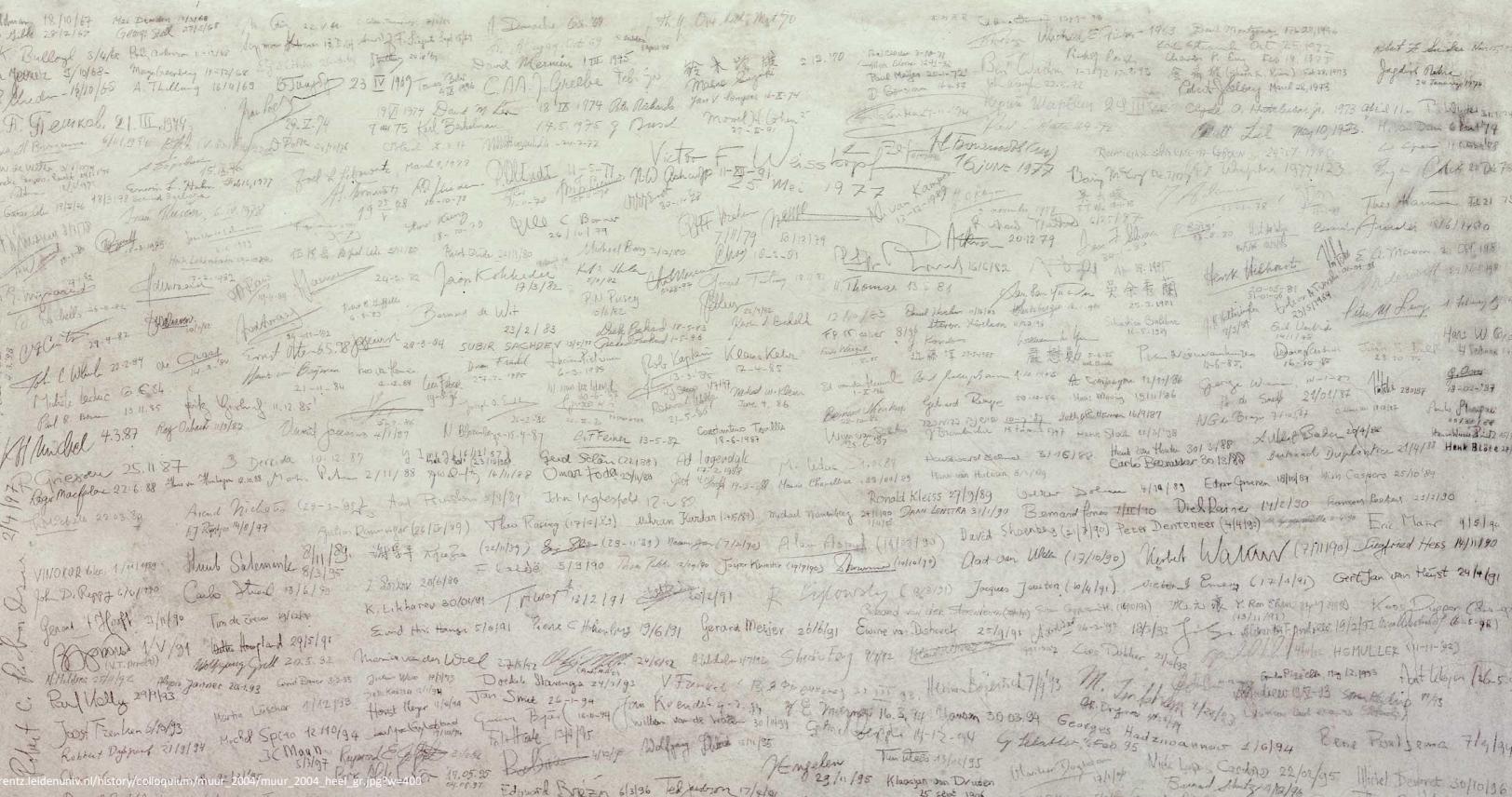
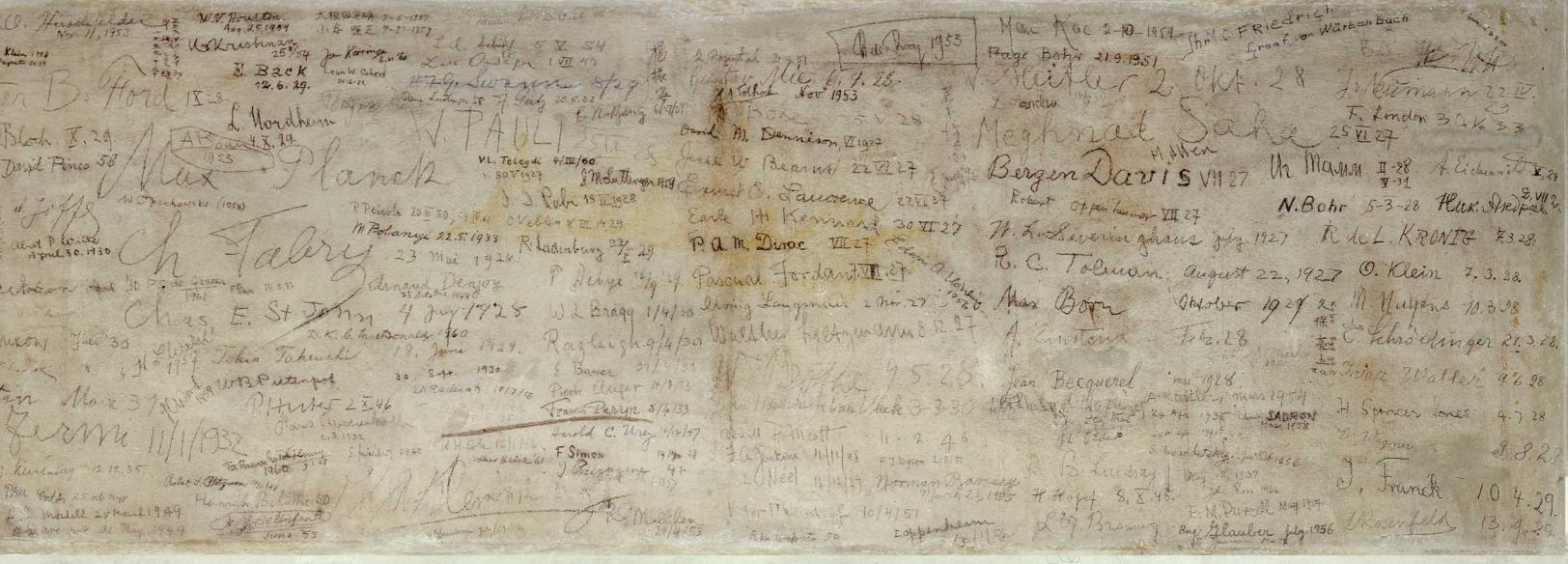


Table of Content

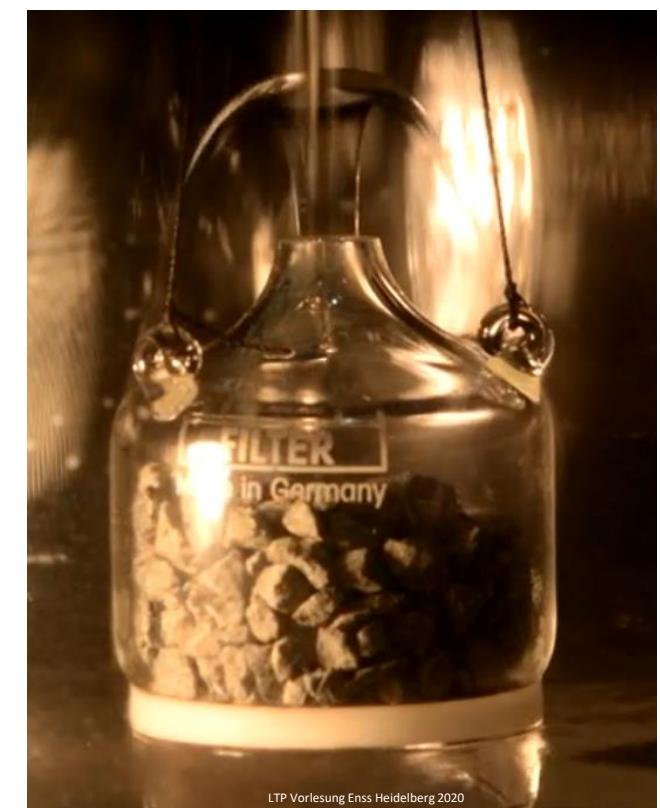
- Why low temperatures
- A historical view
- Expansion Engines
- Joule-Thomson Expansion
- Dilution Refrigeration
- Nuclear Demagnetization
- Summary and where it is used now

Why low temperatures

- Low noise measurements
- Different timescales
- Freezing out degrees of freedom
- Superconductivity
- Superfluidity

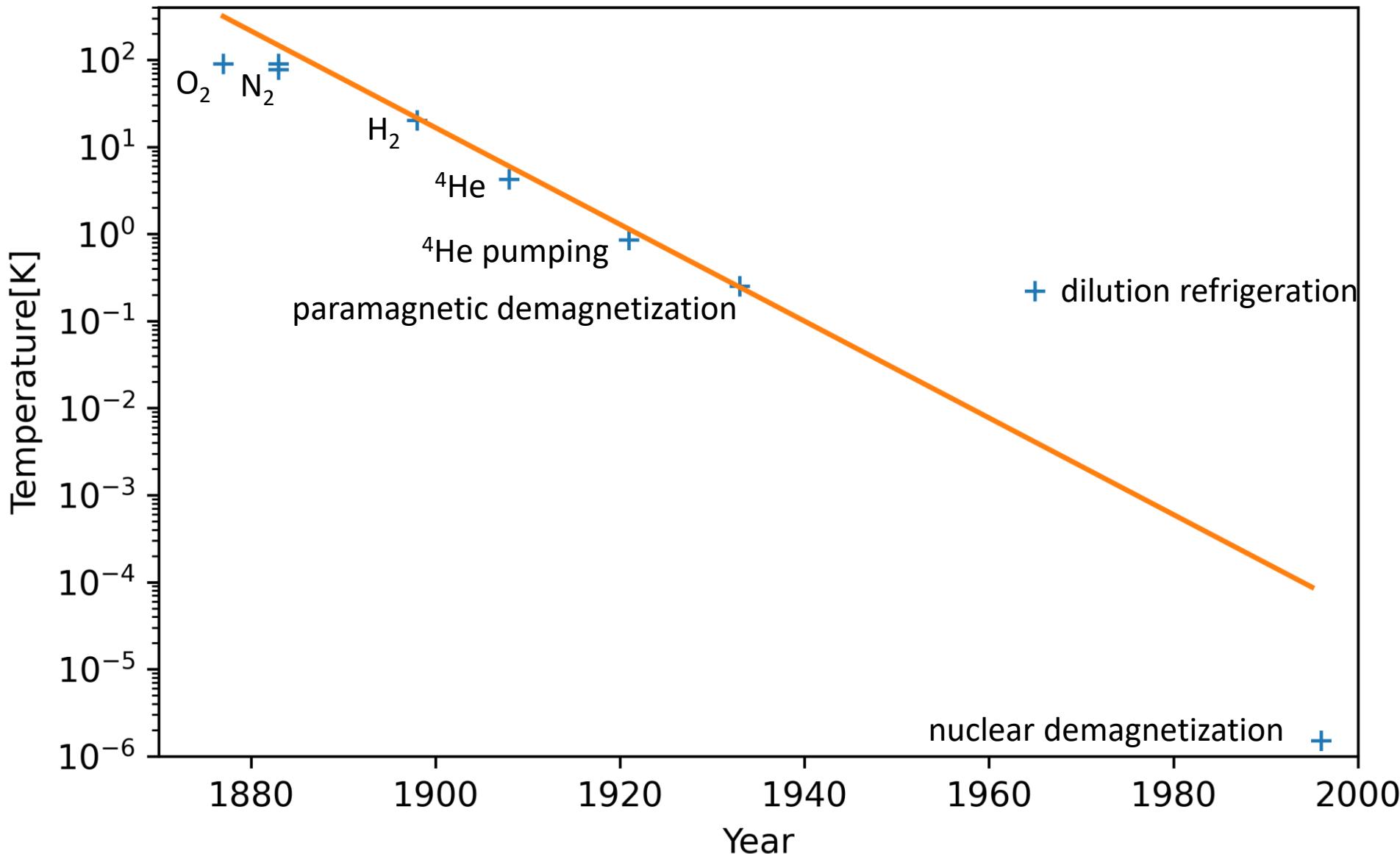


https://de.wikipedia.org/wiki/Supraleiter#/media/File:Magnet_4.jpg



LTP Vorlesung Enss Heidelberg 2020

Reaching low Temperatures

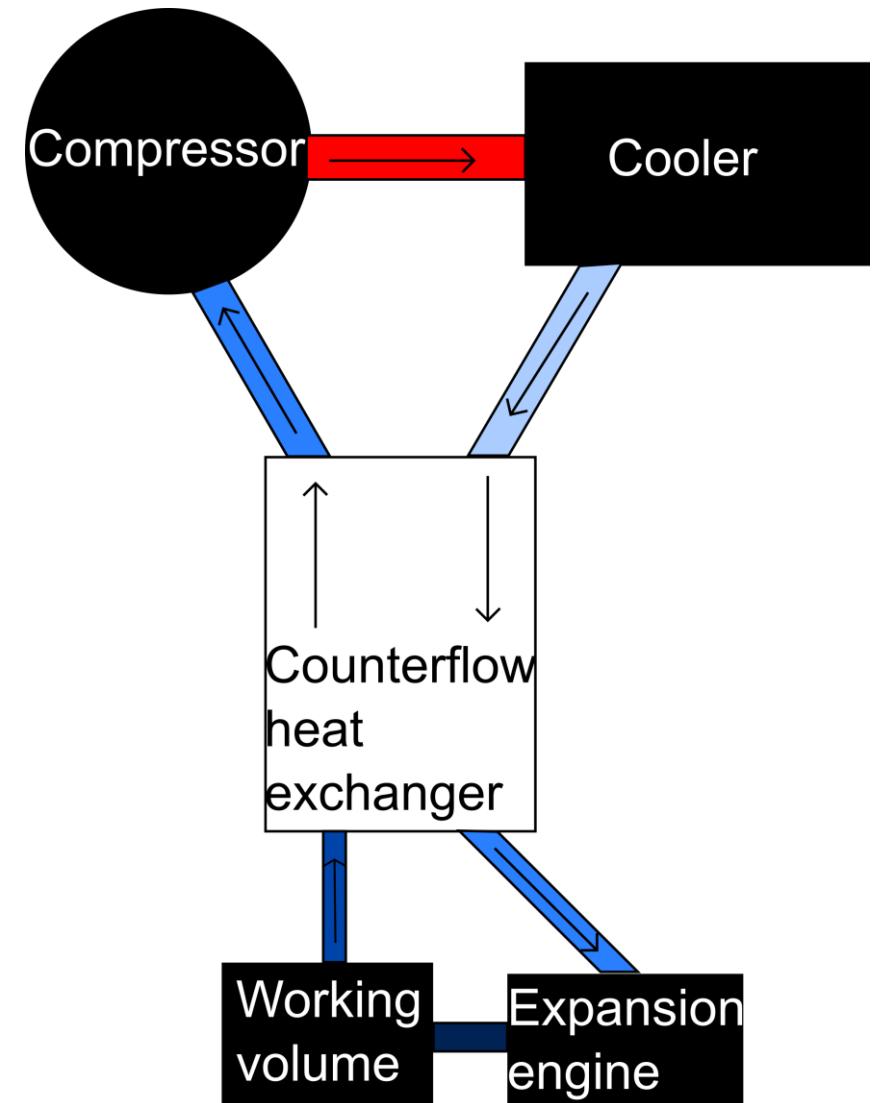


Expansion engines

- Compressing at room temperature
- Approximately adiabatic process
- Cooling gas has to be above critical temperature

$$T_2 = T_1 \left(\frac{p_2}{p_1} \right)^{(\kappa-1)/\kappa}$$

$$\kappa = C_p / C_V$$



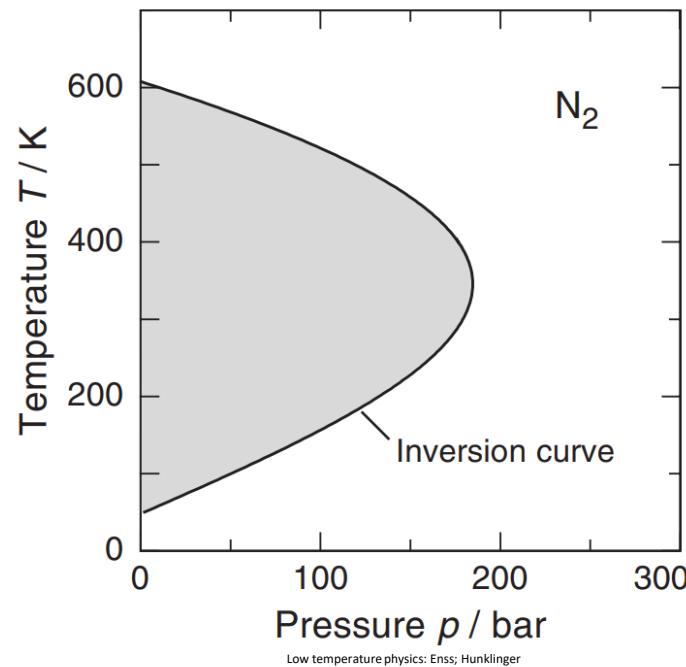
Substance	T_b/K	T_c/K	p_c/bar	$\Delta H/\text{kJ mol}^{-1}$	T_{inv}/K
CO_2	195	304	73.84	25.2	(2050)
CH_4	112	191	45.99	8.18	(1290)
O_2	90.2	154.6	50.43	6.82	762
N_2	77.4	126.0	33.99	5.57	625
H_2	20.3	32.9	12.84	0.90	203
^4He	4.21	5.19	2.29	0.082	43.2
^3He	3.19	3.32	1.16	0.025	(23)

Low temperature physics Enss Hunklinger

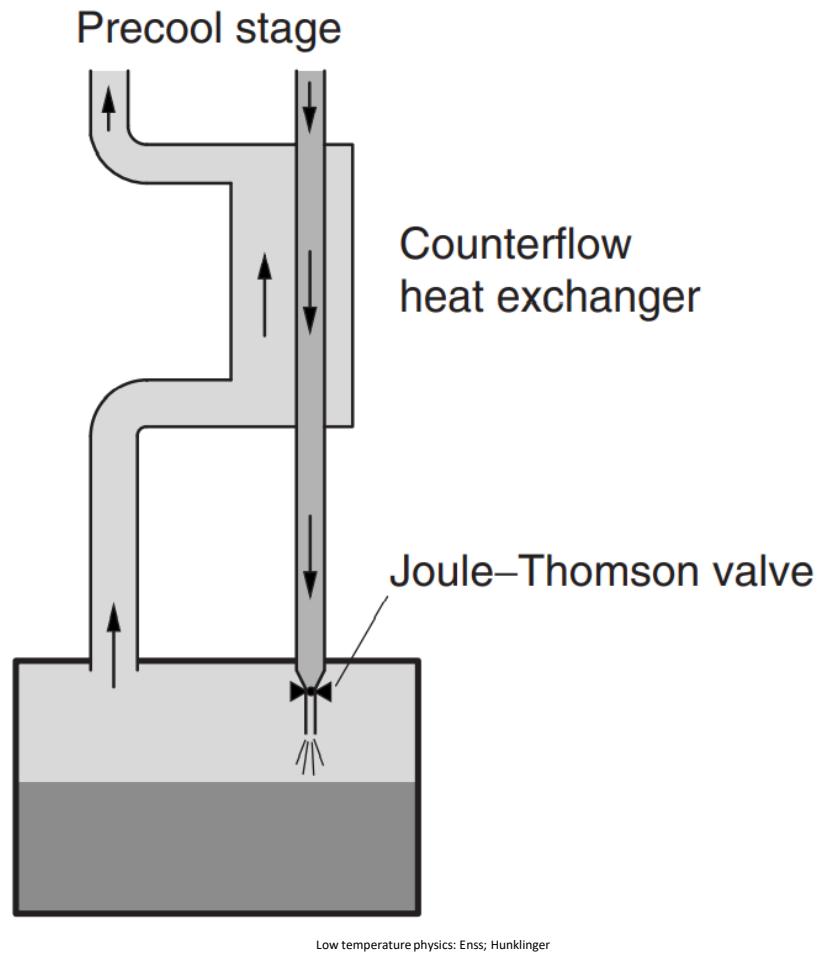


Joule-Thomson Expansion

- Gas performs work against internal forces
- no temperature reduction with ideal gases
- Isenthalp pressure reduction
- Heating or cooling
- Joule-Thomson-coefficient

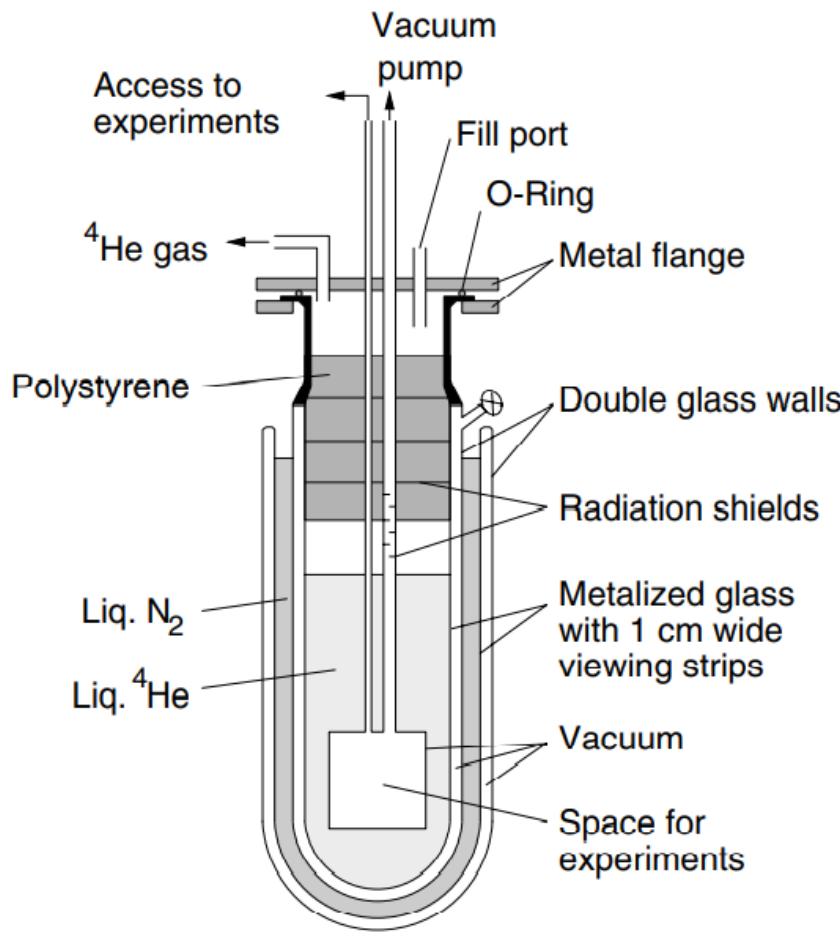


$$\mu_{\text{JT}} = \left(\frac{\partial T}{\partial p} \right)_H$$



(Helium-)Bath Cryostats

- Vacuum-isolated glass vessels (Dewar vessels) (down to 4.2 K)
- Can be pumped to reach lower temperatures
→ Evaporation Cryostats (down to 1.3 K)
- High consumption of Helium (40%)



Clausius-Clapeyron

$$\frac{dp}{dT} = \frac{L}{\Delta V T}$$

$$\Delta V = V_g - V_\ell \approx V_g$$

$$\frac{dp}{dT} = \frac{L}{R T^2} p$$

$$p(T) = p_0 e^{-L/RT}$$

$$\dot{Q} \propto p \propto e^{-L/RT}$$

^4He vs. ^3He

^4He :

- Boson($I=0$)
- Liquid at $T=0$ (and normal p)
- He-I, normalfluid
- He-II, superfluid
- Boilingtemperature: 4.21
- Density at boiling point: 0.055 g/cm^3

^3He :

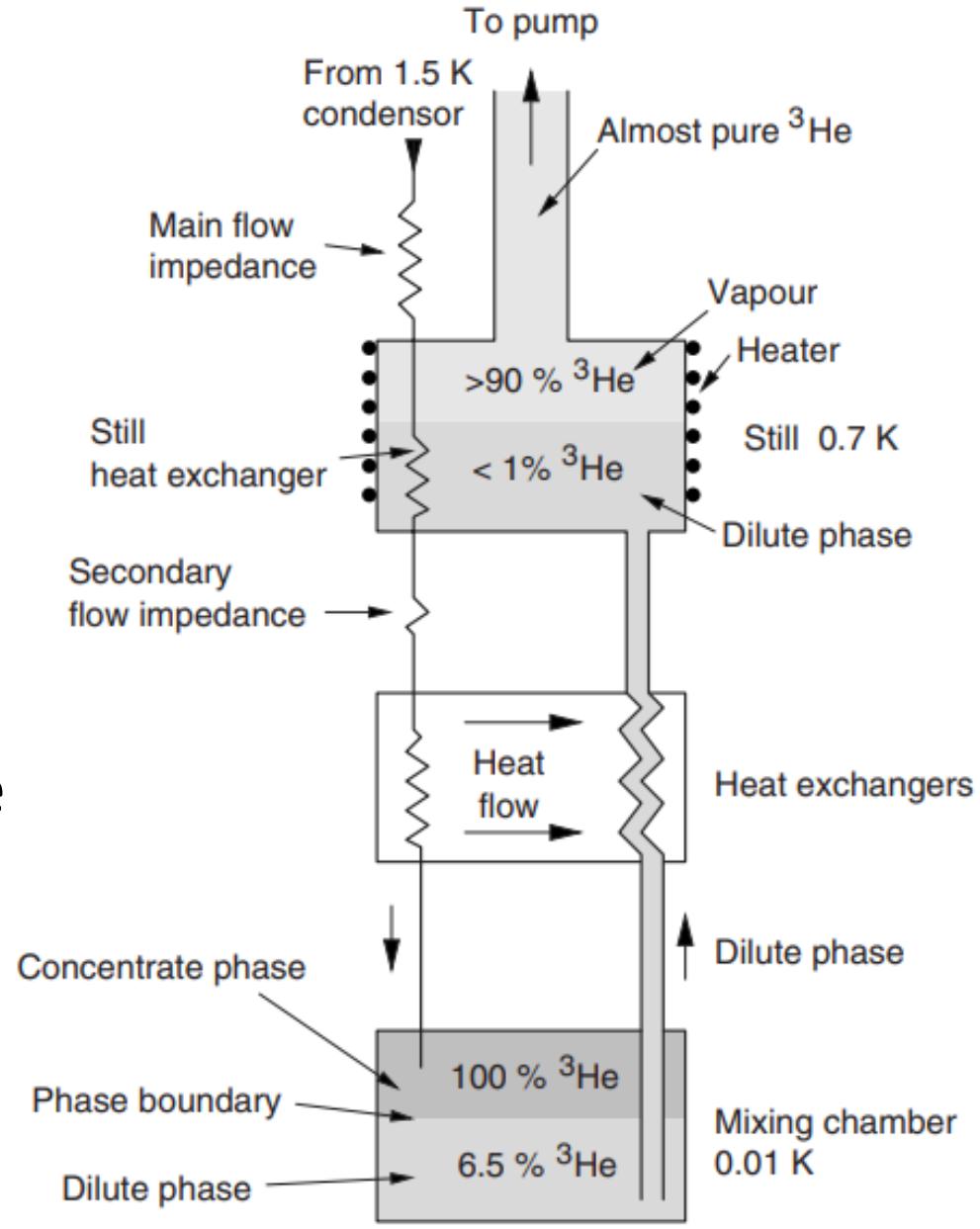
- Fermion($I=1/2$)
- Liquid at $T=0$ (and normal p)
- He-N, normalfluid
- He-A, He-A1, He-B, superfluid
- Boilingtemperature: 3.19
- Density at boiling point: 0.145 g/cm^3



Dilution Refrigeration

- Kinetic Energy of ${}^3\text{He}$ rises with density of ${}^3\text{He}$ (Fermi-statistics)
- effective binding energy is reduced
- At 6.5% ${}^3\text{He}$ in ${}^4\text{He}$ binding energy vanishes ($T \rightarrow 0$)
- Phase separation in ${}^4\text{He}/{}^3\text{He}$ -mixtures (0.86K)
- A light ${}^3\text{He}$ -rich phase and a heavy mixed phase
- ${}^3\text{He}$ has lower entropy in the ${}^3\text{He}$ -rich phase

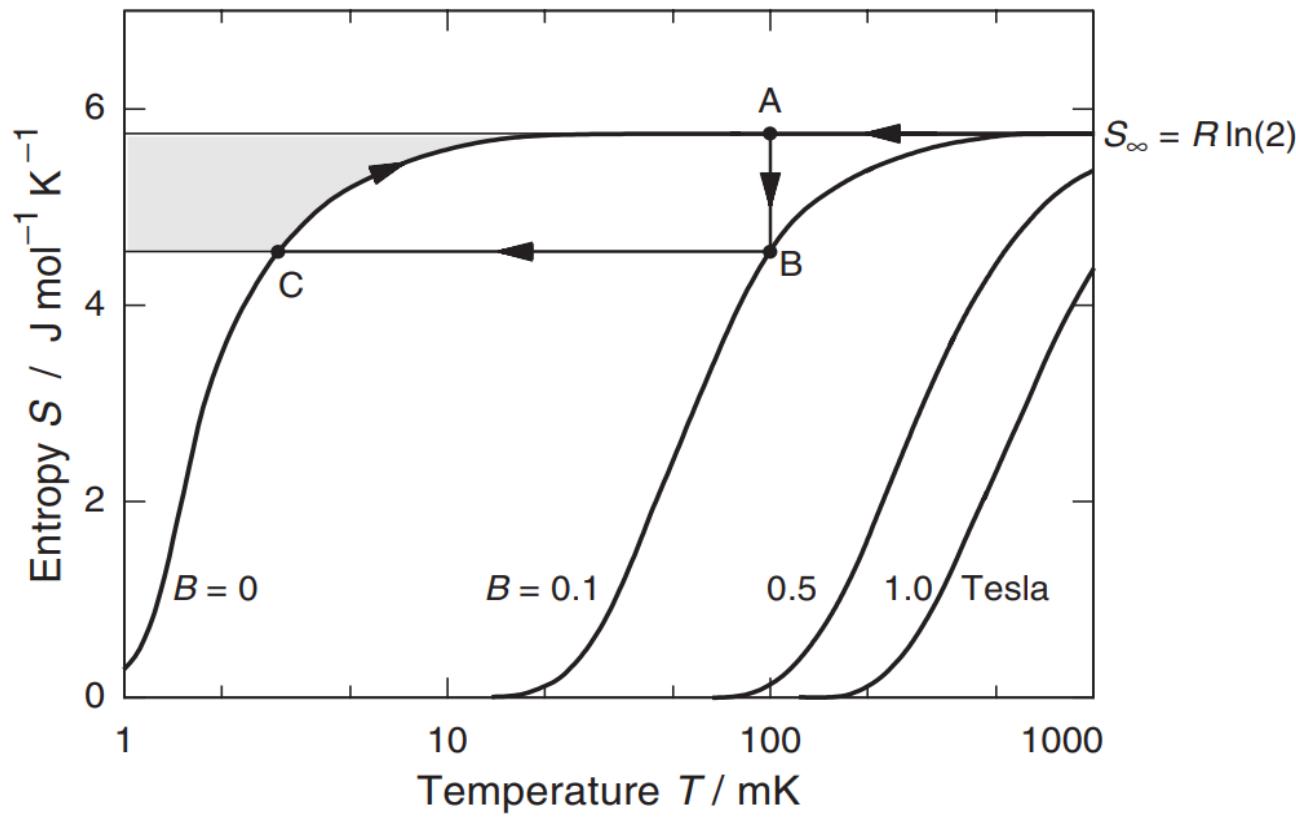
$$\Delta Q = T \Delta S = aT^2$$
$$a = -84 \text{ J K}^{-2}$$



Low temperature physics: Enss; Hunklinger

Magnetic refrigeration

- spin entropy is magnetic field dependent
- Cooled magnetization
- Adiabatic demagnetization
- Isomagnetic entropic transfer



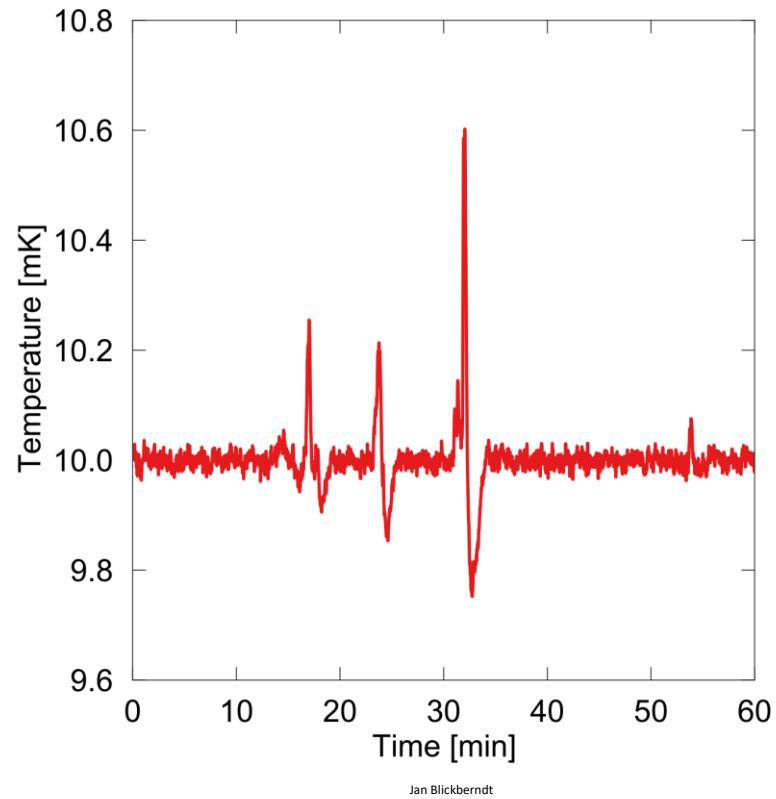
Low temperature physics: Enss; Hunklinger



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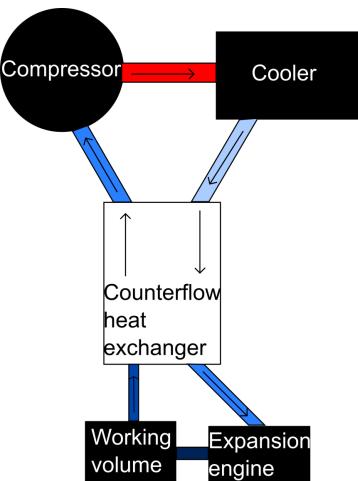
Technical Problems magnetic refrigeration

- Nuclear spin
- Heat switch (superconducting)
- Thermally isolated for long time
- $T < 100 \mu\text{K}$, a leak has to be smaller than 10^{-9} W
 - (eg. $2 \times 10^{-6} \text{ W}$ for a typical watch)
- Vibrations (eddy currents in magnetic field)
- Cosmic rays (10^{-11} W)

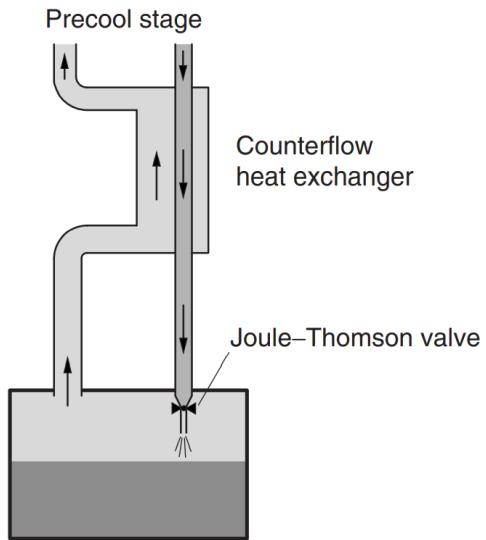


Summary

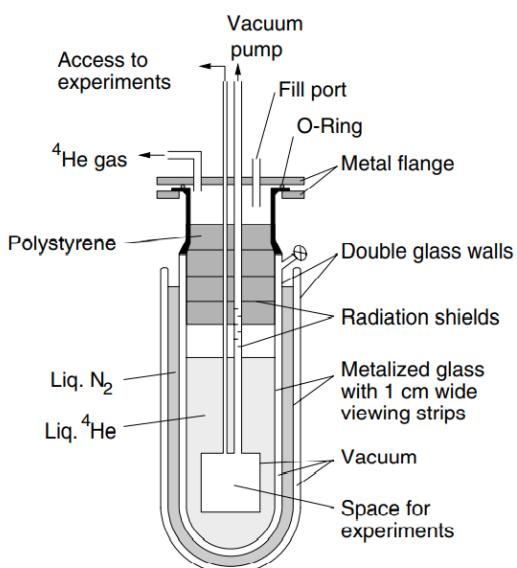
Expansion Engine



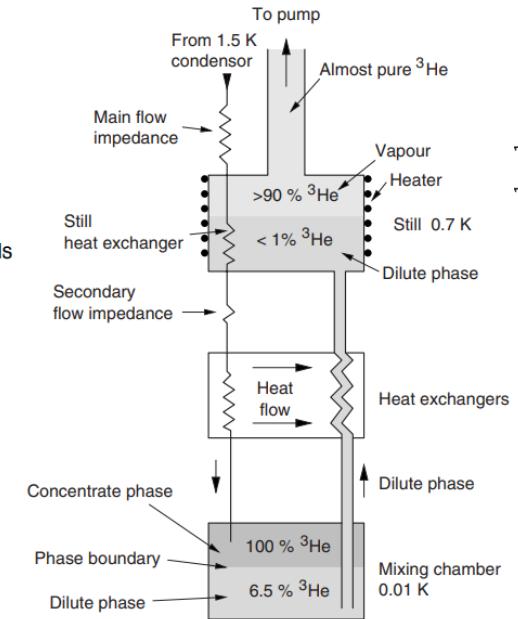
Joule-Thomson Expansion



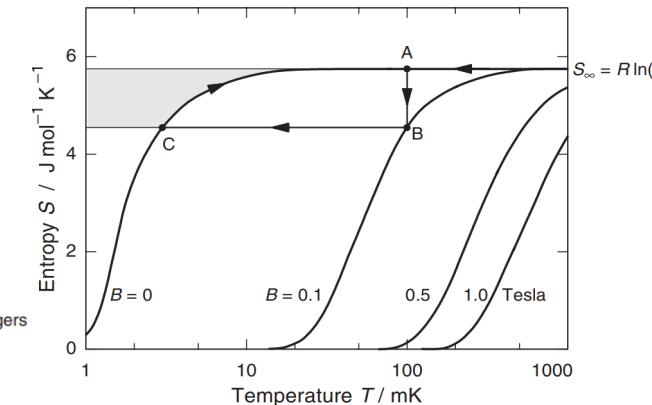
(Helium-)Bath Cryostats



Dilution Refrigeration



Magnetic refrigeration



$T > 5.19 \text{ K}$

$T \approx 4.2 \text{ K}$

$T \approx 1 \text{ K}$

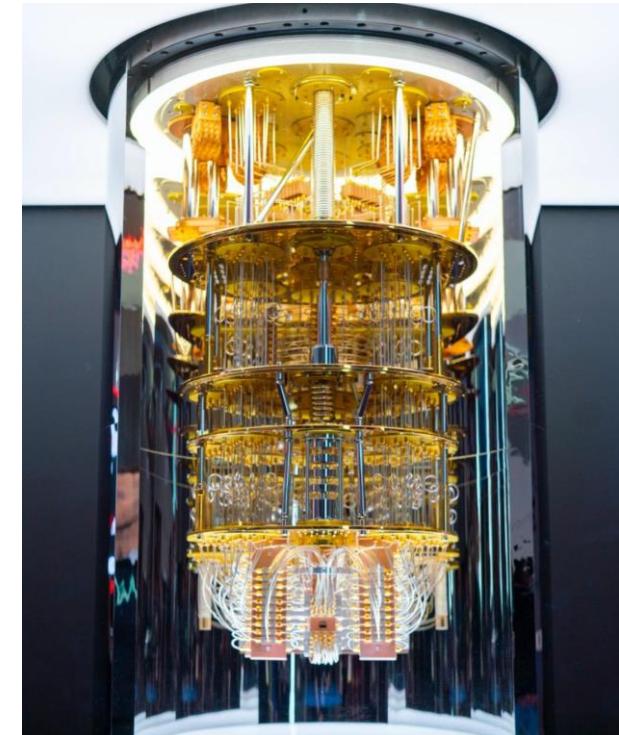
$T \approx 0.01 \text{ K}$

$T \approx 10^{-6} \text{ K}$

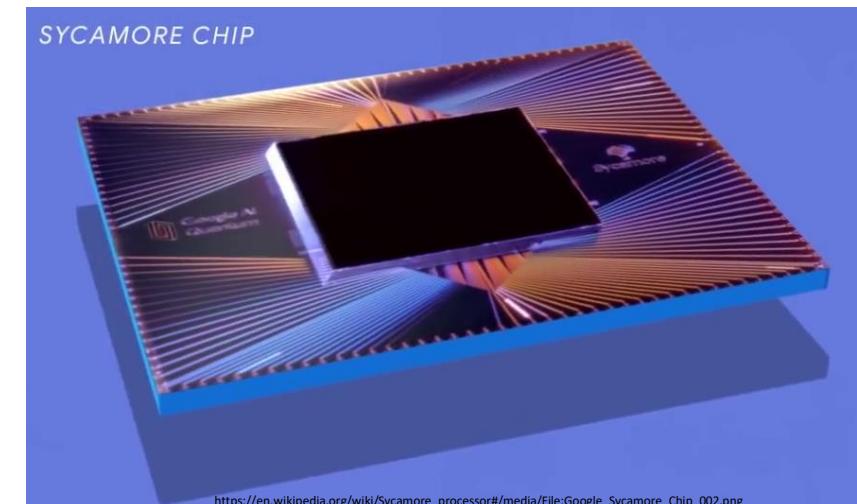


Where is it used now?

- Quantum processors
- Josephson-junctions
→ Superconducting
- Dilution Refrigeration



https://cdn.prod.www.spiegel.de/images/00e7eacb-ae92-4b00-90aa-303d03558082_w1600_r1.4992503748125936_fpx52.67_fpy44.98.jpg



https://en.wikipedia.org/wiki/Sycamore_processor#/media/File:Google_Sycamore_Chip_002.png



Citations

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- Lecture: Enss, Reiser: Low temperature physics Heidelberg, 2020
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- Frossati, G. Experimental techniques: Methods for cooling below 300 mK. *J Low Temp Phys* **87**, 595–633 , 1992

Thank you for the attention

Questions?

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