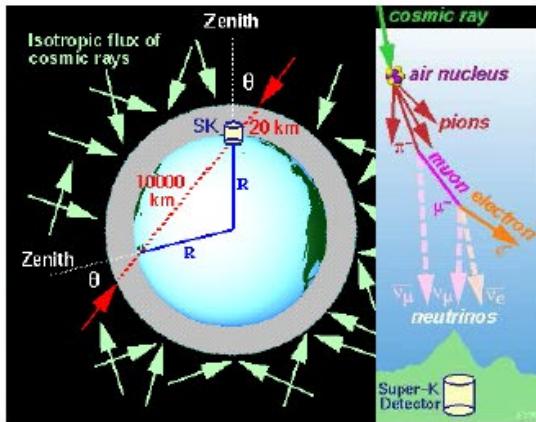
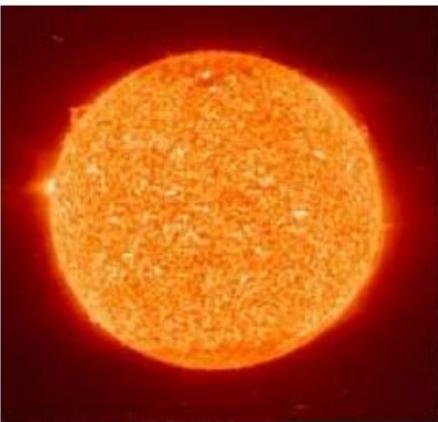


5.3 Neutrino oscillation experiments

Neutrino sources



PDG 2020

Short
Long
baseline

Experiment	L (m)	E (MeV)	$ \Delta m^2 $ (eV 2)
Solar	10^{10}	1	10^{-10}
Atmospheric	$10^4 - 10^7$	$10^2 - 10^5$	$10^{-1} - 10^{-4}$
Reactor	SBL $10^2 - 10^3$	1	$10^{-2} - 10^{-3}$
	LBL $10^4 - 10^5$		$10^{-4} - 10^{-5}$
Accelerator	SBL 10^2	$10^3 - 10^4$	> 0.1
	LBL $10^5 - 10^6$	$10^3 - 10^4$	$10^{-2} - 10^{-3}$

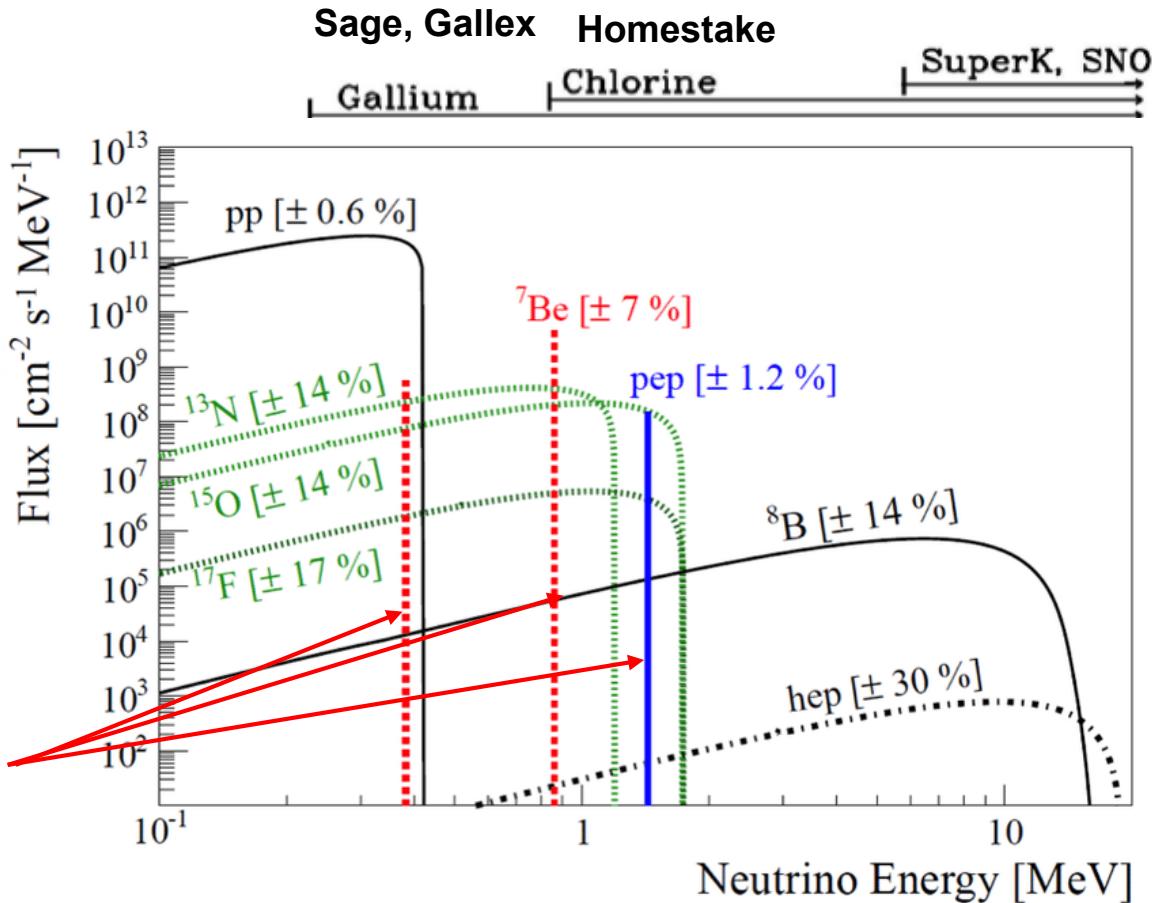
Studied neutrino sources can be well described by a “2-neutrino mixing model”:

e. g. For solar neutrinos:

$$\mathcal{P}(\nu_e \rightarrow \nu_x) = \sin^2(2\theta) \sin^2\left(\frac{\Delta m^2}{4E} L\right)$$

Solar neutrinos:

Solar neutrino spectrum from different fusion reactions



Reaction for neutrino detection on earth:

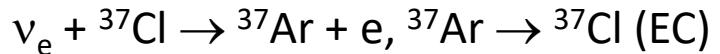
Cl_2 detectors	$\nu_e + {}^{37}\text{Cl} \rightarrow {}^{37}\text{Ar} + e$, ${}^{37}\text{Ar} \rightarrow {}^{37}\text{Cl}$ (EC)	$E_\nu > 0.8 \text{ MeV}$
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Ga detectors	$\nu_e + {}^{71}\text{Ga} \rightarrow {}^{71}\text{Ge} + e$	$E_\nu > 0.2 \text{ MeV}$
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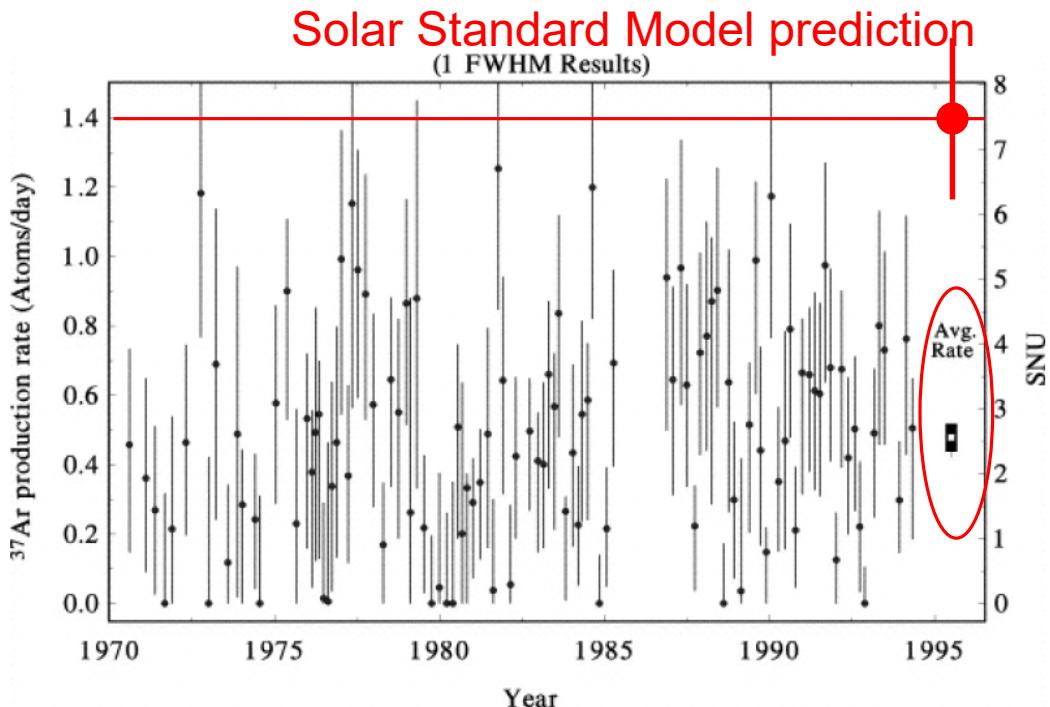
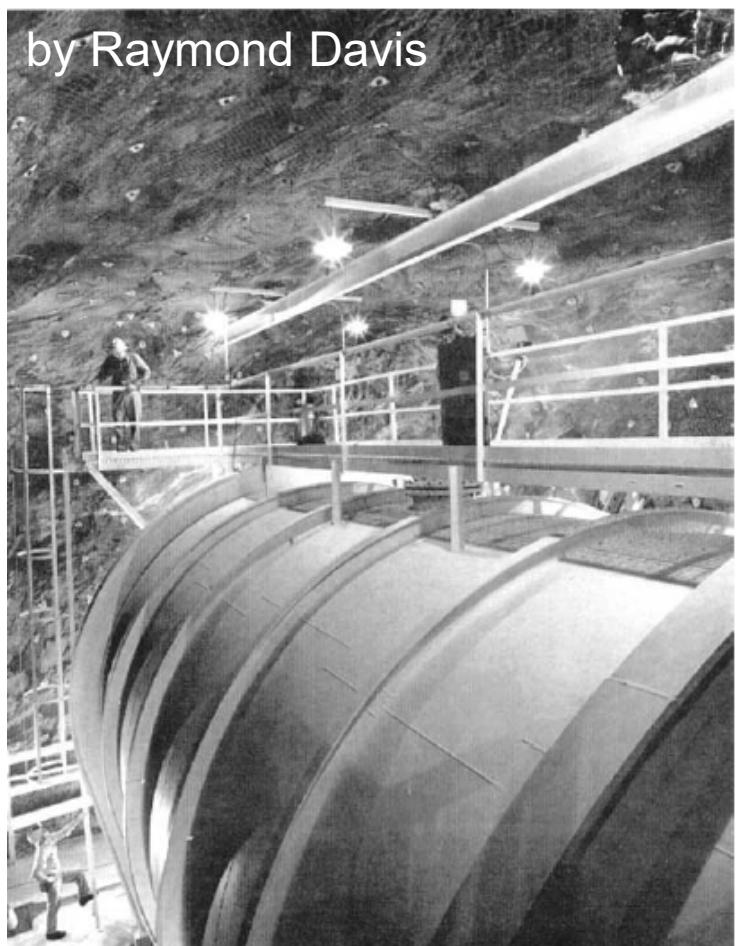
H_2O detectors	Elastic scattering: $\nu_e + e \rightarrow \nu_e + e$	$E_\nu > 5 \text{ MeV}$ (detection)
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Radio-chemical experiments – the pioneer: Homestake

- Homestake mine, 1400 m underground
- 615 t of C_2Cl_4 (perchloroethylene) = 2.2×10^{30} atoms of ^{37}Cl
- Use ^{36}Ar and ^{38}Ar to carry-out the few atoms of ^{37}Ar (~ 1 atom/day)
- Count radioactive ^{37}Ar decays



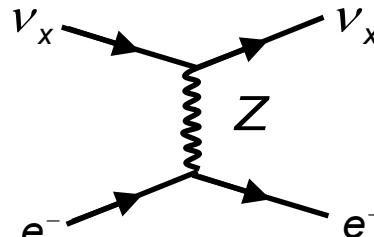
Homestake Cl_2 experiment



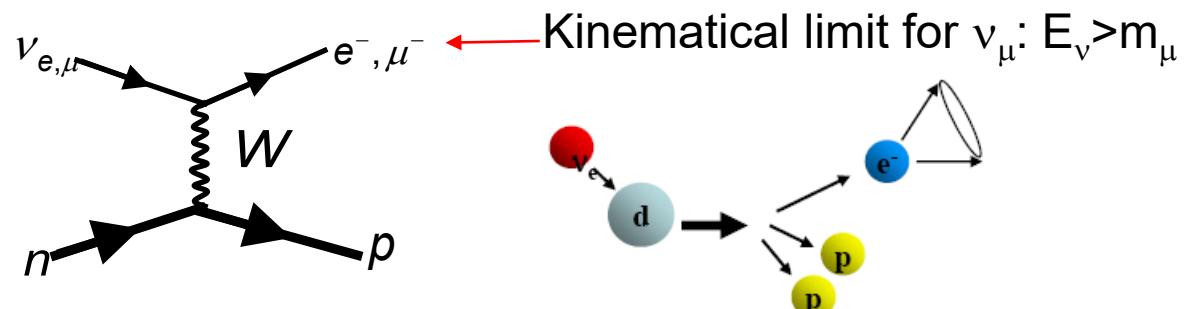
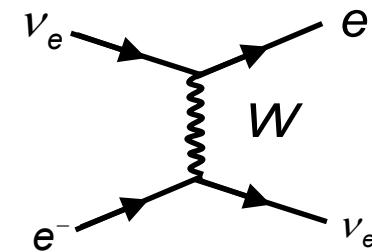
Neutrino detection with water detectors [E_v~O(GeV)]

Water = “active target” (Cherenkov effect)

Elastic scattering ES



Charged current CC

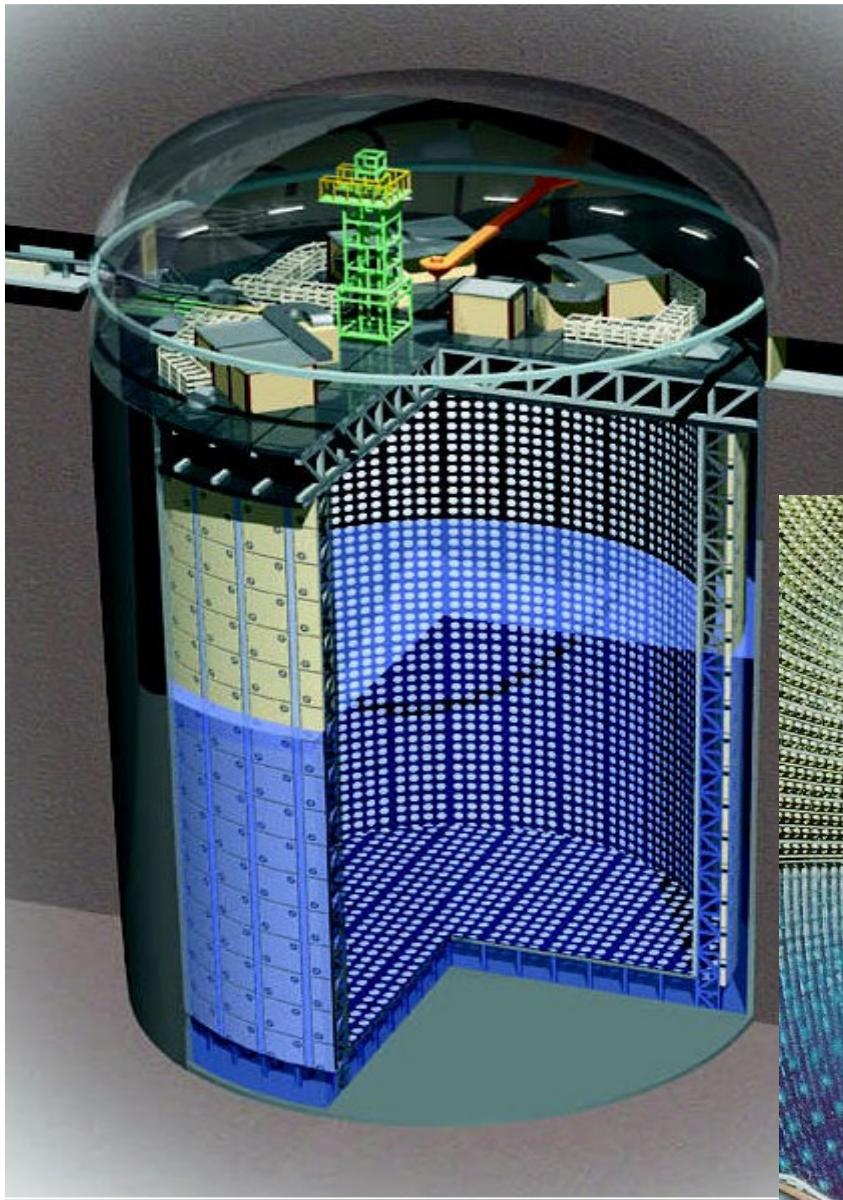


Detection of Cherenkov photons: Photo multiplier

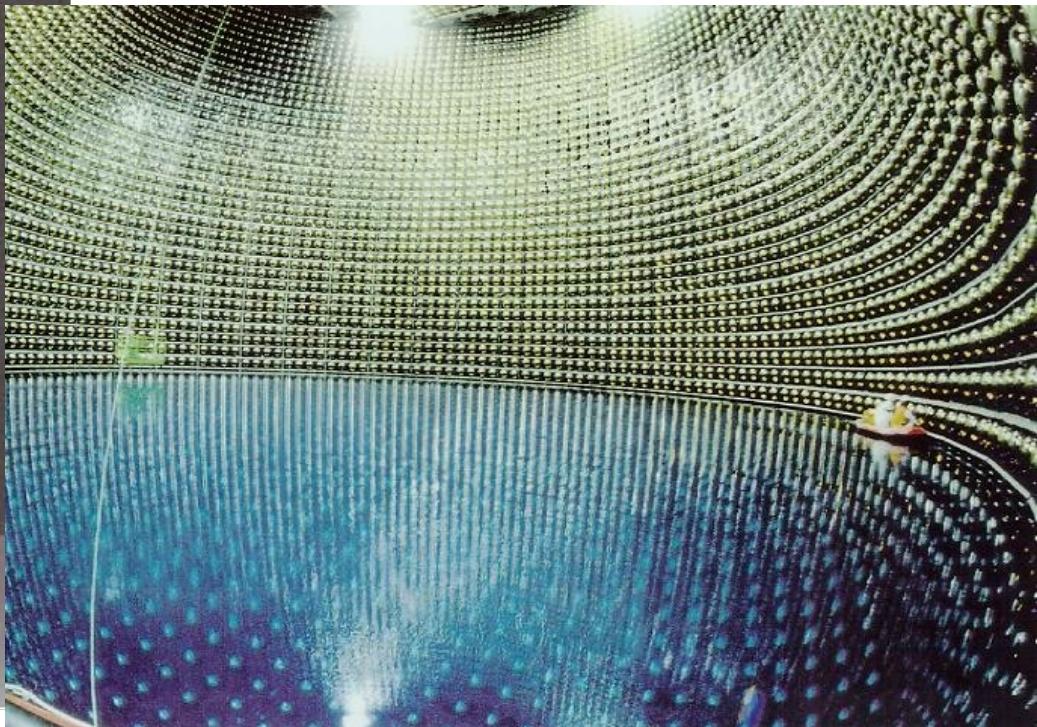
Experiments:

(Super)-Kamiokande

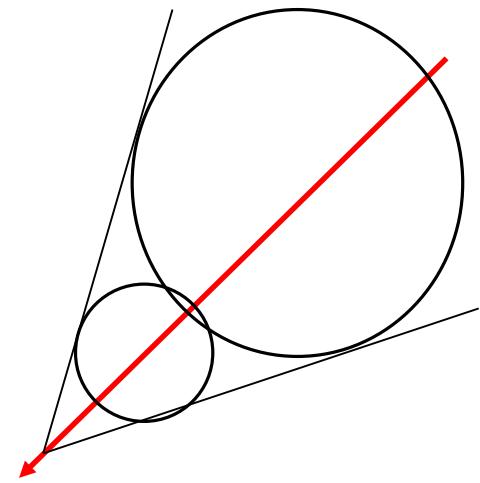
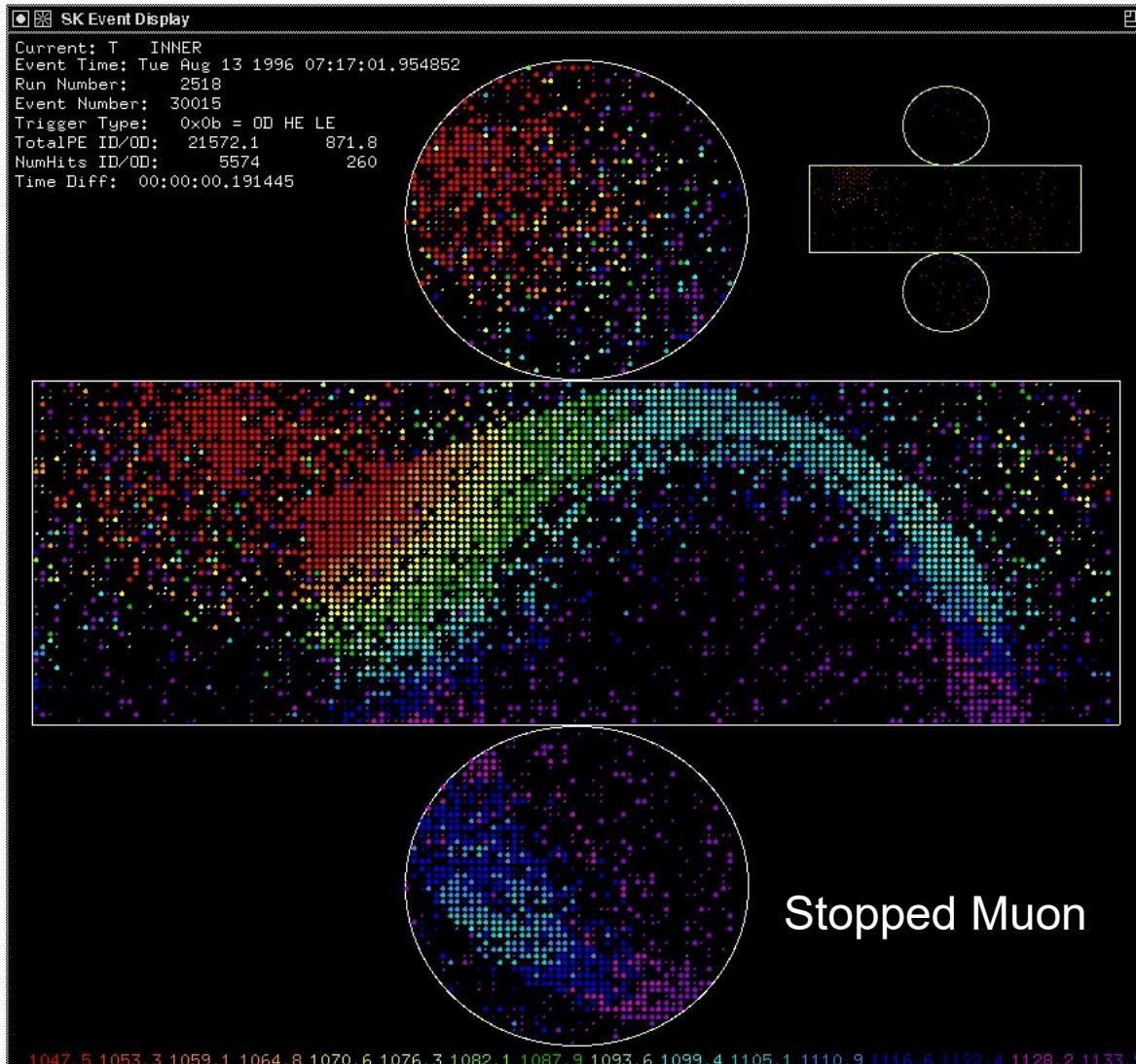
Super-Kamiokande



- Largest artificial water detector (50 kt)
- 11000 PMTs (50 cm tubes!): 40% of surface covered with photo-cathode



$\nu_\mu \rightarrow \mu$ stopped



Cherenkov cone:

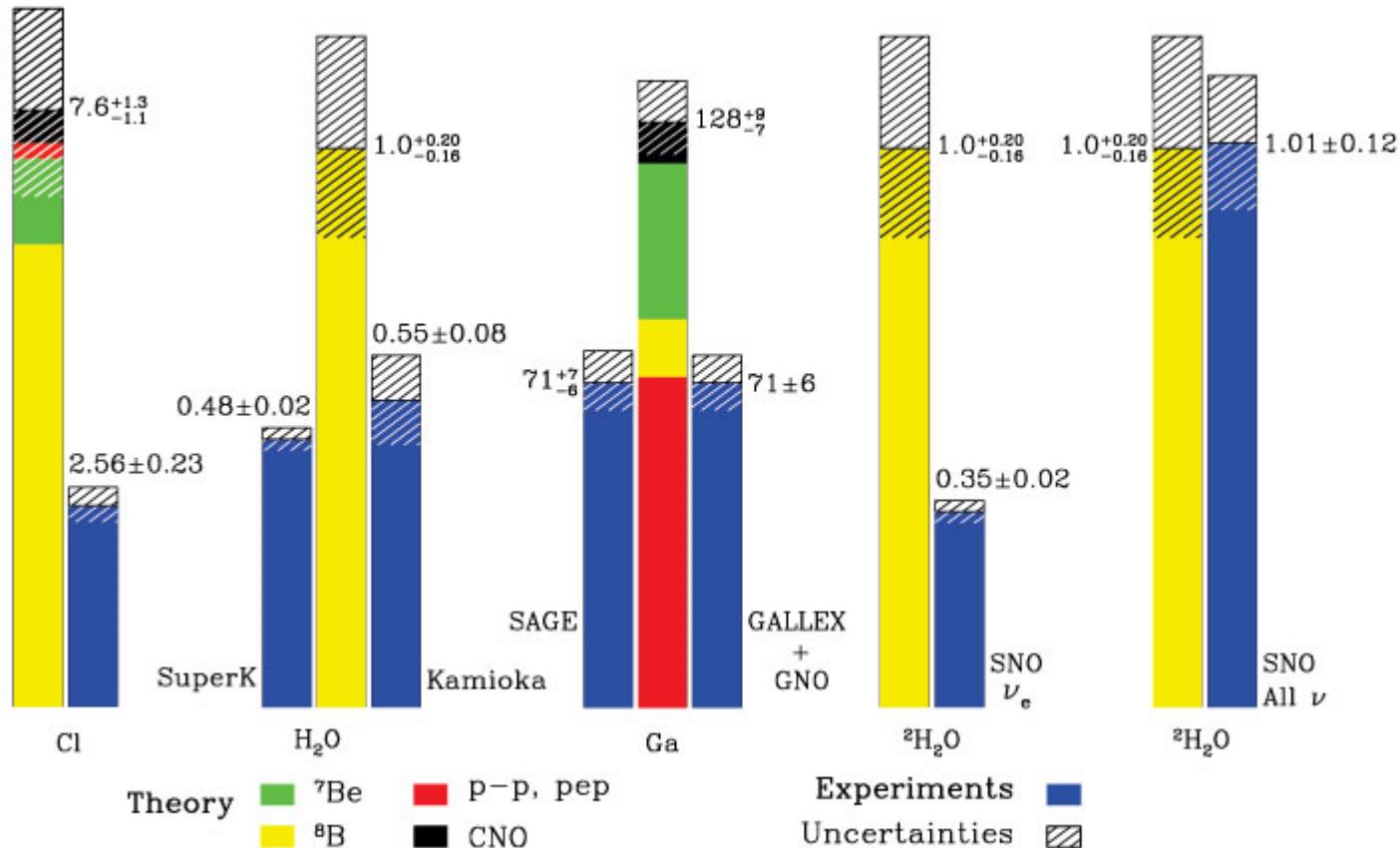
$$\cos \theta = \frac{1}{\beta n}$$
$$\Leftrightarrow \theta = 42^\circ \ (\beta = 1)$$

Experiment can distinguish electron and muon events, can measure energy

Solar Neutrino Problem

Total Rates: Standard Model vs. Experiment

Bahcall–Pinsonneault 2000

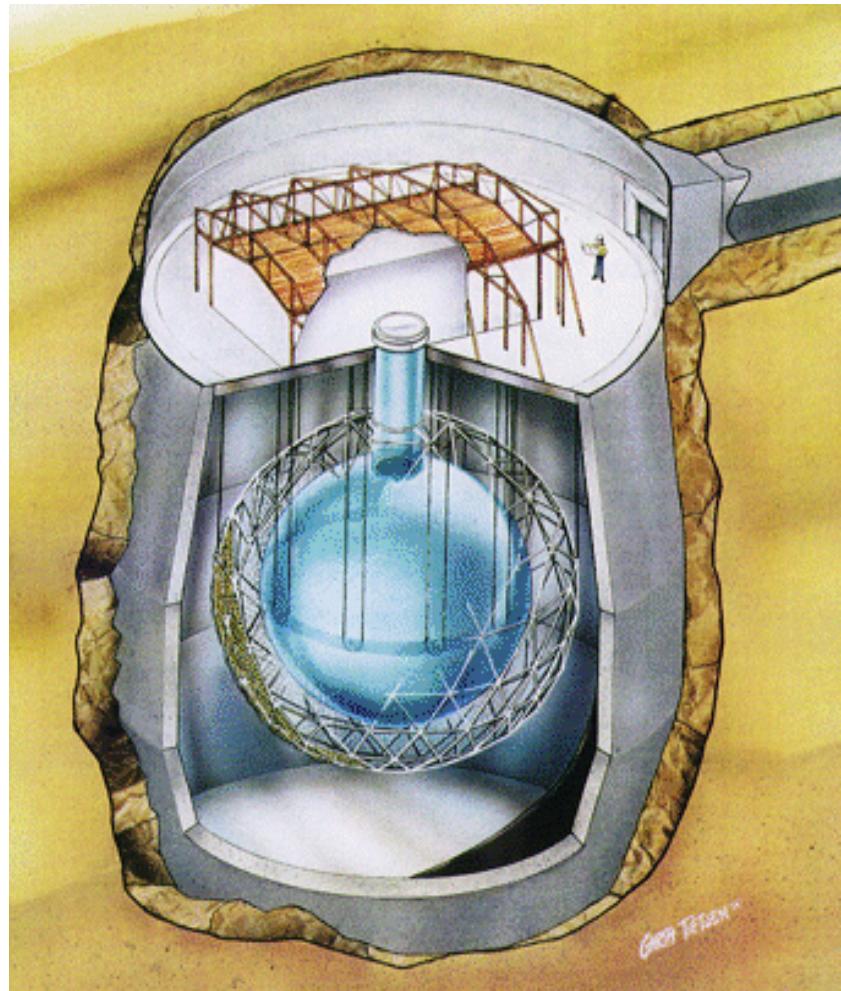
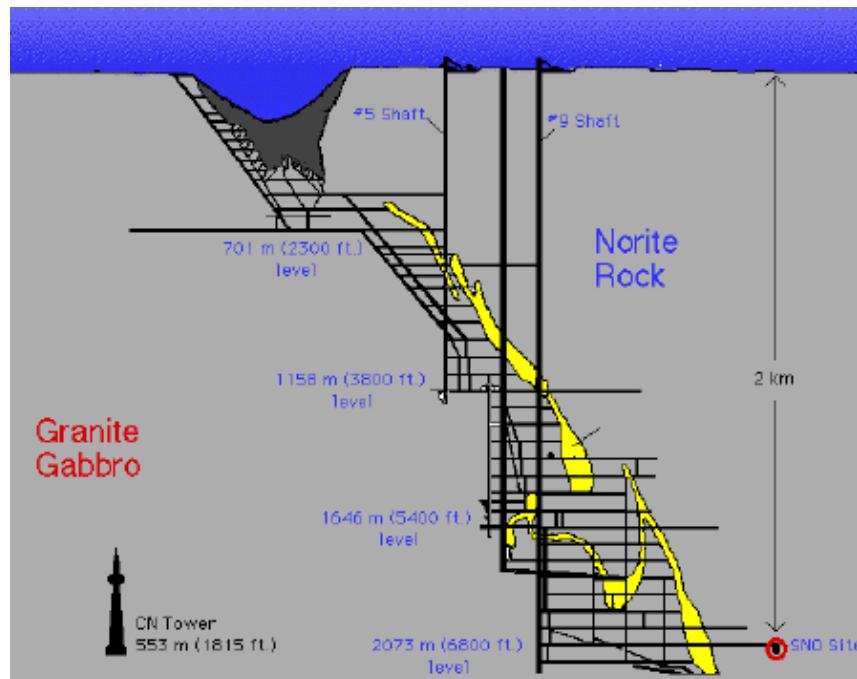


Depending on the neutrino energy between 70% and 35% of the expected neutrino flux from the sun is seen. Solution: $\nu_e \rightarrow \nu_\mu, \nu_\tau$

Sudbury Neutrino Observatory

Try to measure the “oscillated” neutrinos of different flavors

- 6 m radius transparent acrylic vessel
- 1000 t of heavy water (D_2O)
- 9456 inward looking photo multipliers
- Add 2 t of NaCl to detect neutrons

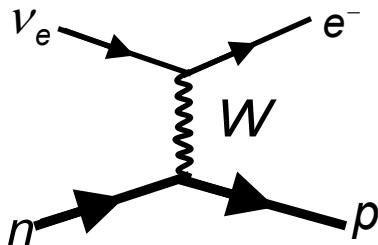


Solar Neutrino (${}^8\text{B}$) detection with SNO

Charged current

$$\sigma(\nu_\mu) = \sigma(\nu_\tau) = 0 \quad (\text{kinematics})$$

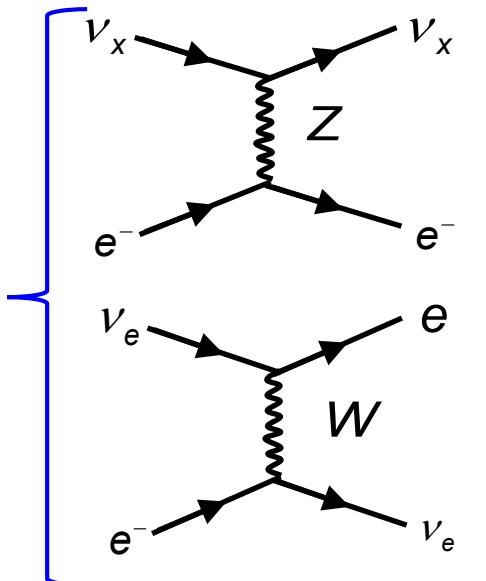
$$\phi_{CC} = \phi_{\nu_e}$$



Elastic scattering

$$0.154 \cdot \sigma(\nu_e) = \sigma(\nu_\mu) = \sigma(\nu_\tau)$$

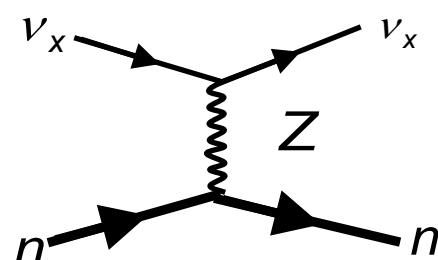
$$\phi_{ES} = \phi_{\nu_e} + (\phi_{\nu_\mu} + \phi_{\nu_\tau}) / 6$$



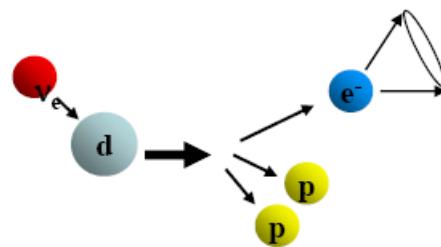
Neutral current

$$\sigma(\nu_e) = \sigma(\nu_\mu) = \sigma(\nu_\tau)$$

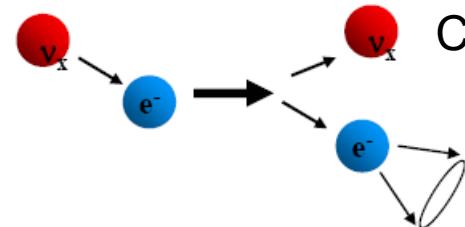
$$\phi_{NC} = \phi_{\nu_e} + \phi_{\nu_\mu} + \phi_{\nu_\tau}$$



Cherenkov Light



Cherenkov Light



Neutron
 ${}^{35}\text{Cl}(n, \gamma){}^{36}\text{Cl}$
123

SNO Evidence for Neutrino Oscillation

Phys. Lett. B539, 179 (2002),

PDG 2020

$$\phi_{CC}^{SNO} = 1.76^{+0.06}_{-0.05} (\text{stat})^{+0.09}_{-0.09} (\text{syst}),$$

$$\phi_{ES}^{SNO} = 2.39^{+0.24}_{-0.23} (\text{stat})^{+0.12}_{-0.12} (\text{syst}),$$

$$\phi_{NC}^{SNO} = 5.09^{+0.44}_{-0.43} (\text{stat})^{+0.46}_{-0.43} (\text{syst}).$$



Electron neutrino flux is too low:

$$P_{\nu e \nu e} = (35 \pm 2)\%$$

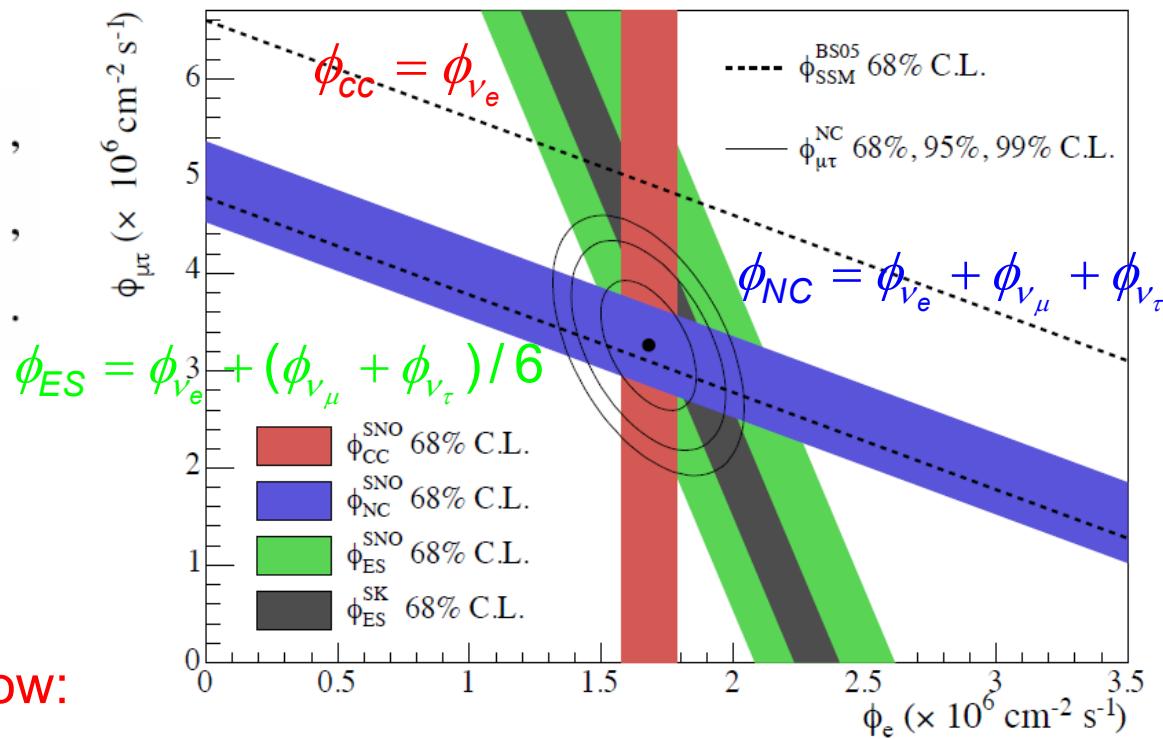
Total flux of neutrinos is correct!!

But in case of simple “vacuum oscillation”:

$$P_{\nu e \nu e} \geq 1 - \frac{1}{2} \sin^2 2\theta \geq 50\%$$

Vacuum oscillation effect is enhanced by matter inside the sun.

Reminder: the neutrino leaves the sun in a fixed mass state.



Interpreted as
 $\nu_e \leftrightarrow \nu_\mu$ or ν_τ oscillation

Fits to data: $\sin^2 \theta_{12} \approx 0.33$

$$\Delta m_{21}^2 \equiv \Delta m_{sol}^2 \approx 7 \times 10^{-5} \text{ eV}^2$$

Only works with “resonance” matter effect in sun:

$$\cos 2\theta_{12} - x > 0$$

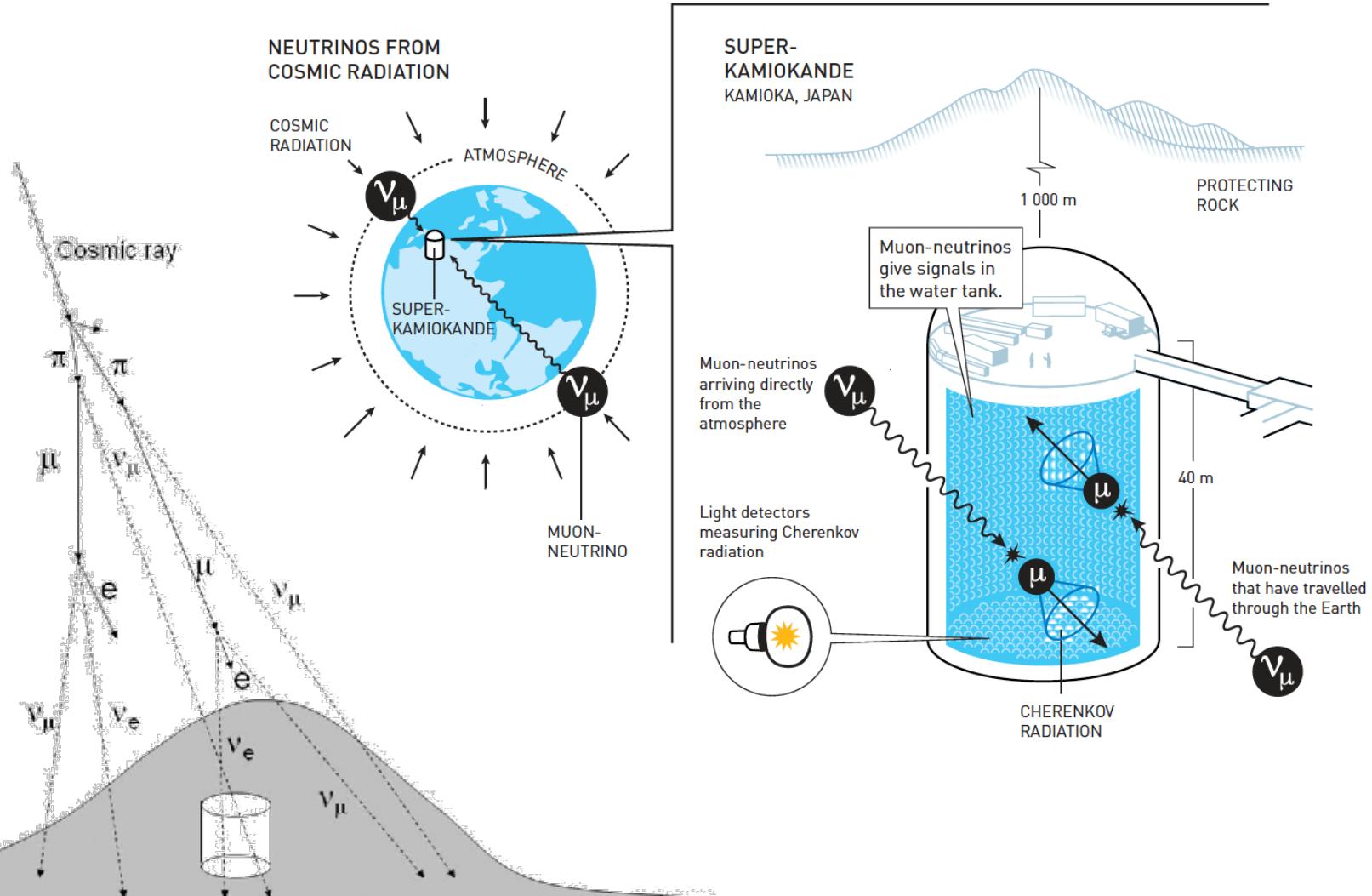
$$\cos 2\theta_{12} - \frac{A}{\Delta m_{sol}^2} > 0 \quad \rightarrow \quad \Delta m_{sol}^2 \cos 2\theta_{12} > A > 0$$

Choosing $\cos 2\theta_{12} > 0$ fixes $\Delta m_{sol}^2 = m_2^2 - m_1^2 > 0$

$$\rightarrow \Delta m_{21}^2 = m_2^2 - m_1^2 > 0$$

i.e. matter effect inside sun fixes $m_2 > m_1$

Atmospheric neutrinos (produce by cosmic rays in the atmosphere)



Muon neutrino : electron neutrino = 2 : 1

Super-Kamiokande:

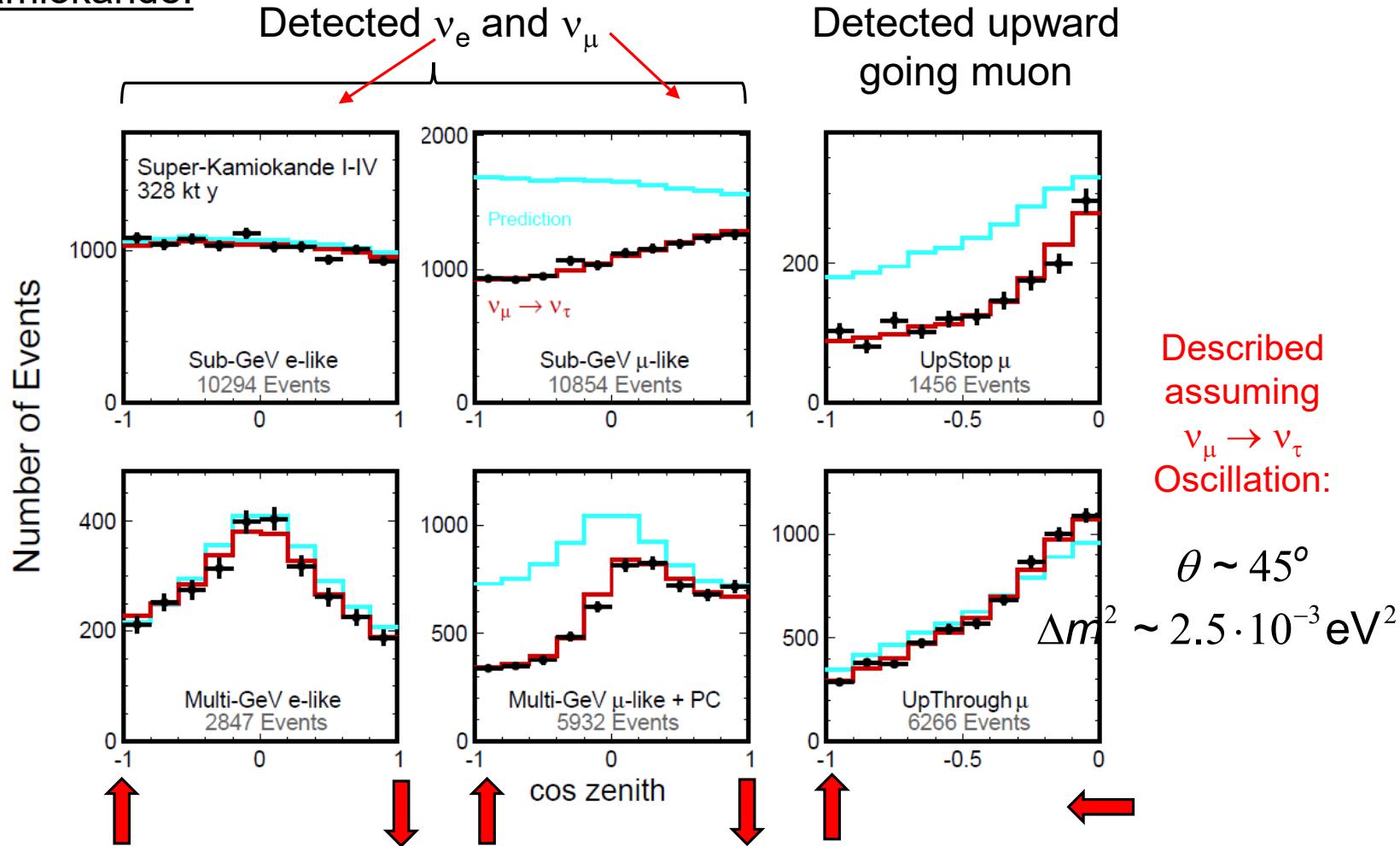


Figure 14.4: The zenith angle distributions of Super-Kamiokande atmospheric neutrino events. Fully contained 1-ring e -like and μ -like events with visible energy $< 1.33 \text{ GeV}$ (sub-GeV) and $> 1.33 \text{ GeV}$ (multi-GeV), as well as upward stopping and upward stopping μ samples are shown. Partially contained (PC) events are combined with multi-GeV μ -like events. The blue histograms show the non-oscillated Monte Carlo events, and the red histograms show the best-fit expectations for $\nu_\mu \rightarrow \nu_\tau$ oscillations. (This figure is provided by the Super-Kamiokande Collaboration)

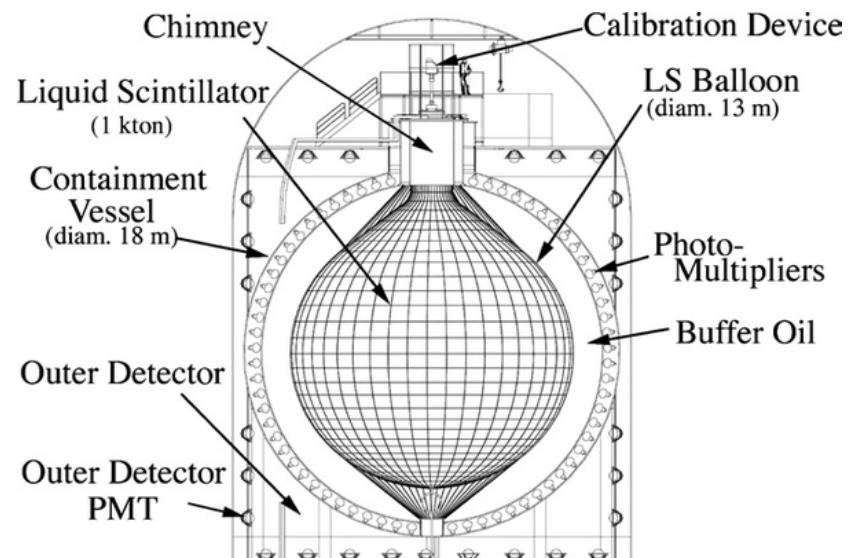
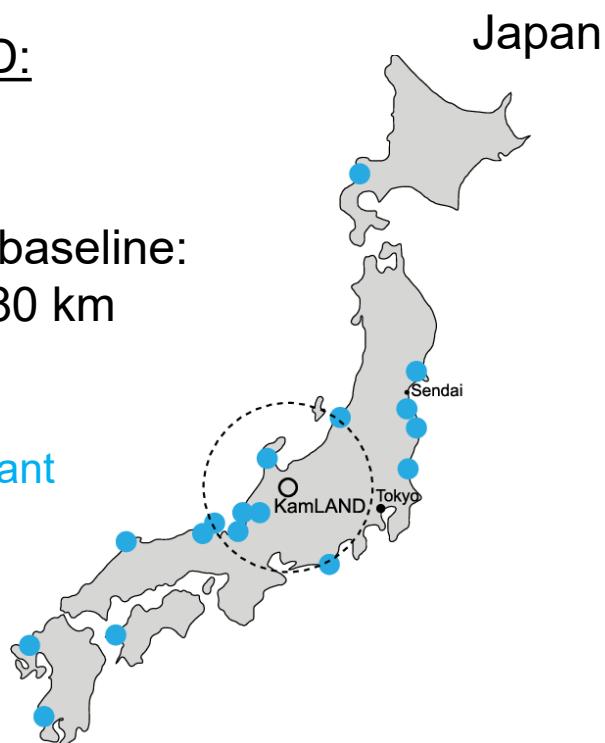
PDG 2020

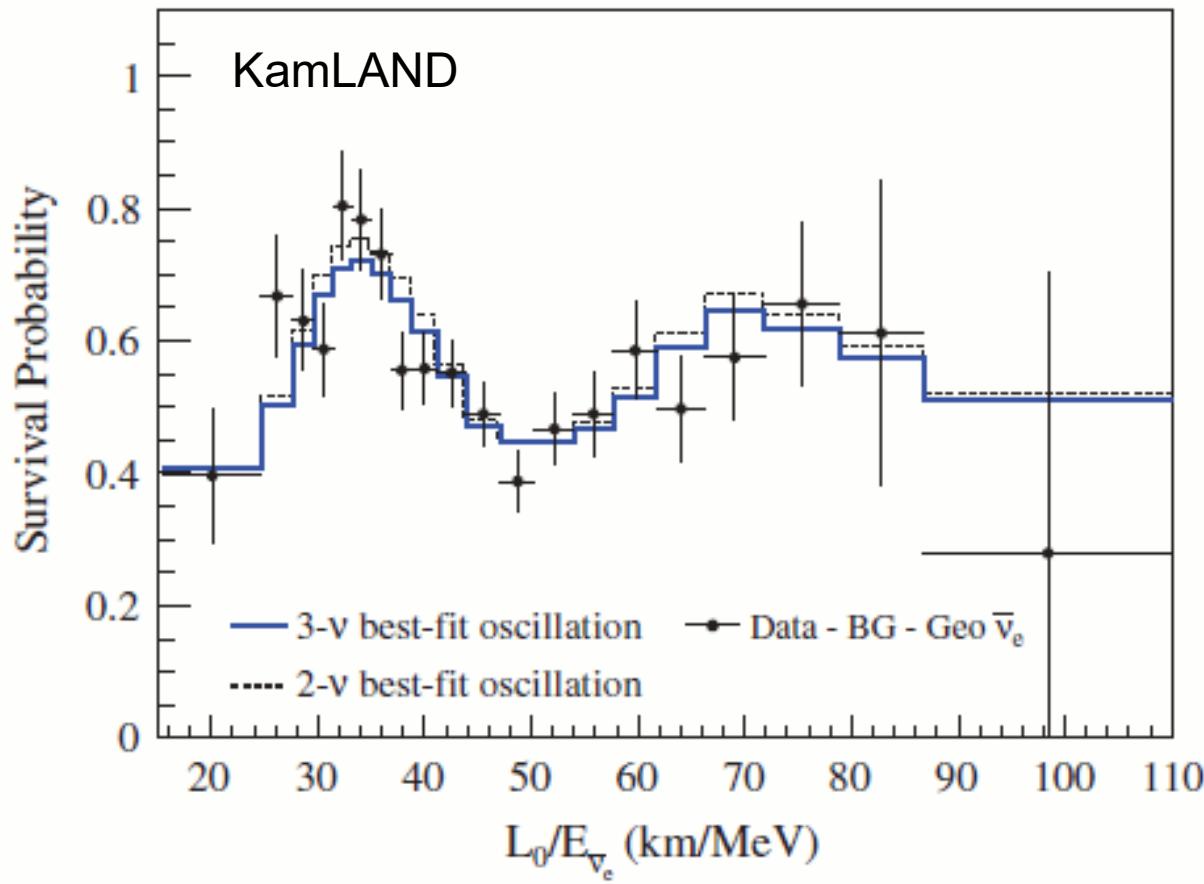
Reactor anti-neutrinos (from neutron β-decays):

Name	Reactor power (GW _{th})	Baseline (km)	Detector mass (t)	Year
KamLAND	various	180 (ave.)	1,000	2001–
Double Chooz	4.25×2	1.05	8.3	2011–2018
Daya Bay	2.9×6	1.65	20×4	2011–
RENO	2.8×6	1.38	16	2011–
JUNO	26.6 (total)	53	20,000	

KamLAND:

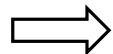
Average baseline:
L = 180 km



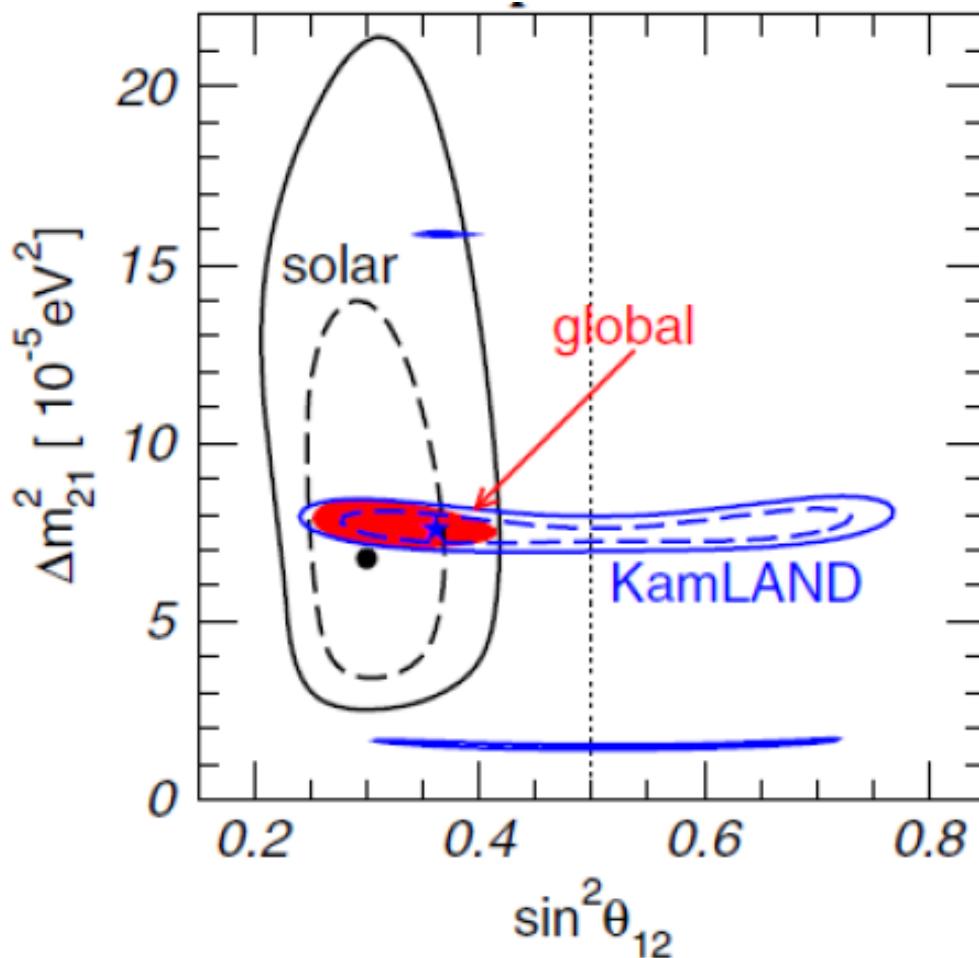


$\nu_e \rightarrow \nu_e$ at distances of $L_0 = 180$ km very well described by the 2 neutrinos model

Figure 14.7: Ratio of the observed $\bar{\nu}_e$ spectrum to the expectation for no-oscillation versus L_0/E for the KamLAND data. $L_0 = 180$ km is the flux-weighted average reactor baseline. The 3- ν histogram is the best-fit survival probability curve from the three-flavour unbinned maximum-likelihood analysis using only the KamLAND data. This figure is taken from [150]. *PDG 2020*



KamLAND confirms solar neutrinos results:
large mixing angle and $\Delta m^2 \approx 7 \times 10^{-5}$ eV 2



Measurement of θ_{13}

$$U = \underbrace{\begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{pmatrix}}_{\text{Atmospheric neutrino mixing}} \underbrace{\begin{pmatrix} c_{13} & 0 & s_{13} e^{-i\delta_{CP}} \\ 0 & 1 & 0 \\ -s_{13} e^{i\delta_{CP}} & 0 & c_{13} \end{pmatrix}}_{\text{reactor neutrinos; accelerator neutrinos}} \underbrace{\begin{pmatrix} c_{12} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix}}_{\text{Solar neutrino mixing; KamLAND}}$$

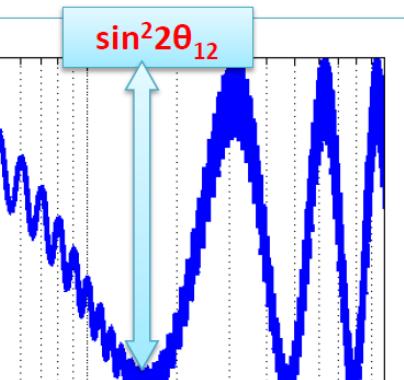
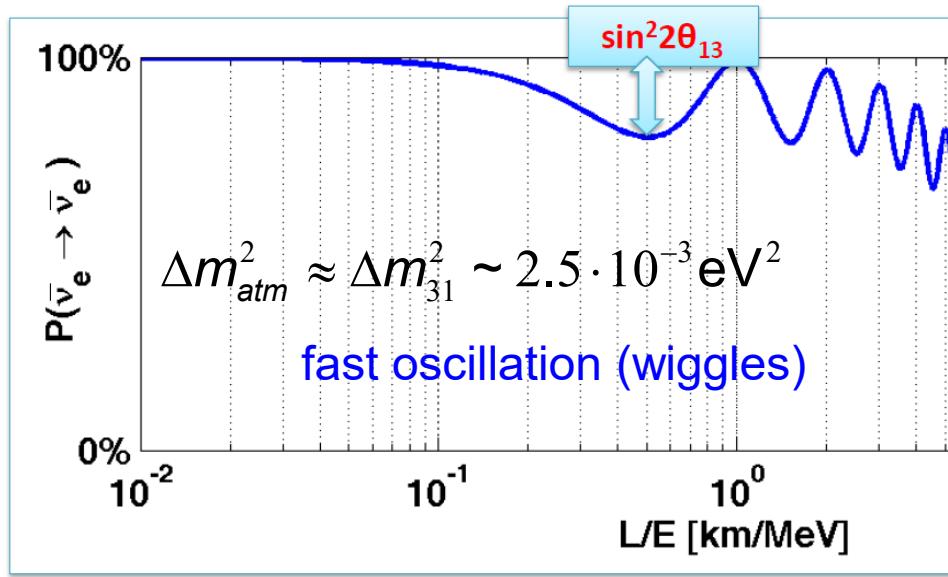
$\Delta m_{atm}^2 \sim 2.5 \cdot 10^{-3} \text{ eV}^2$ $\Delta m_{sol}^2 \sim 7 \cdot 10^{-5} \text{ eV}^2$
 $\theta_{23} \sim 45^\circ$ $\theta_{13} > ??$ $\theta_{12} \sim 33^\circ$

To observe CP violation in neutrino mixing a finite value of $\sin^2 \theta_{13}$ is necessary.

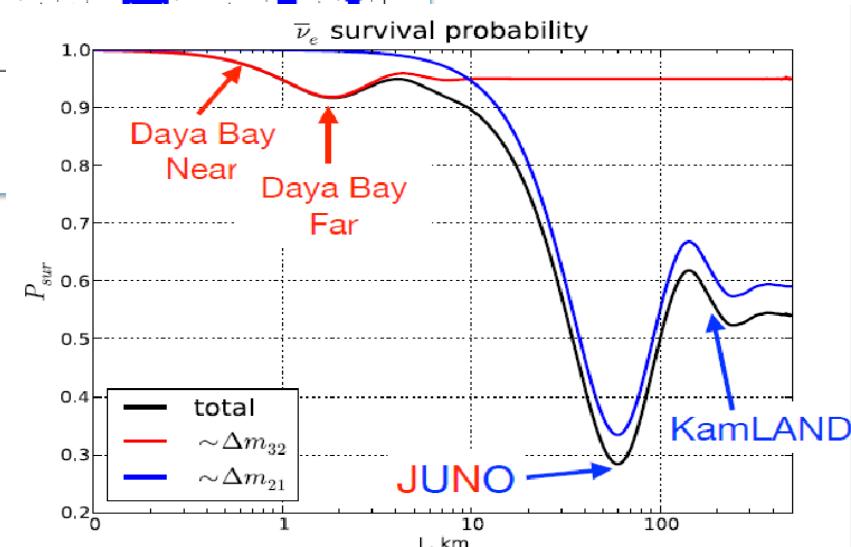
θ_{13} with reactor neutrinos:

Survival probability for 3-neutrino mixing:

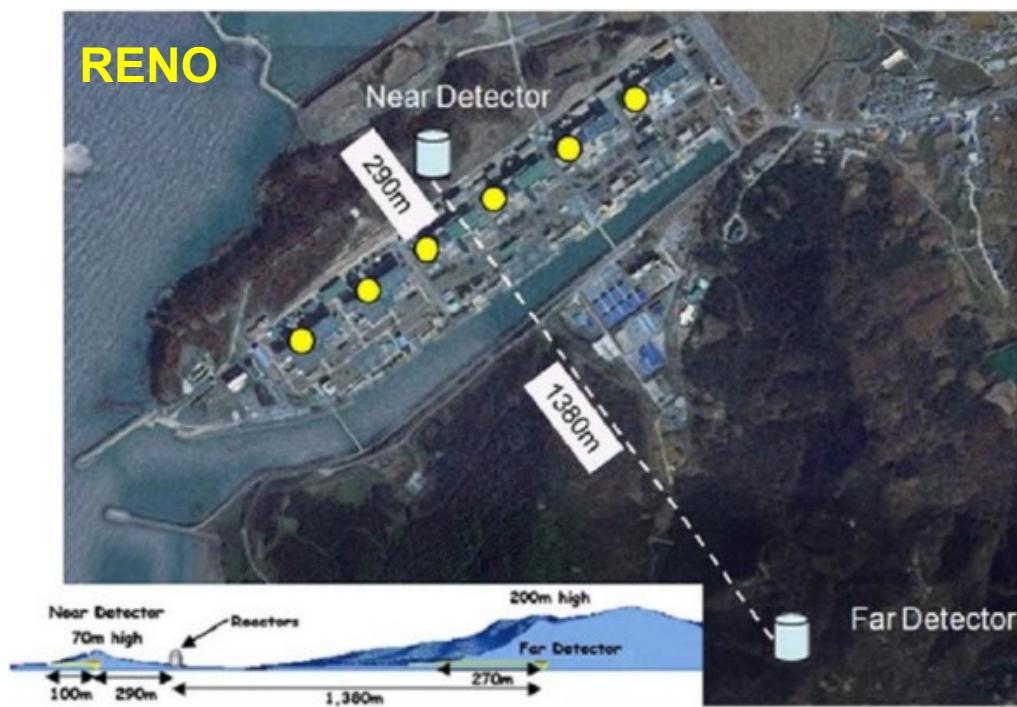
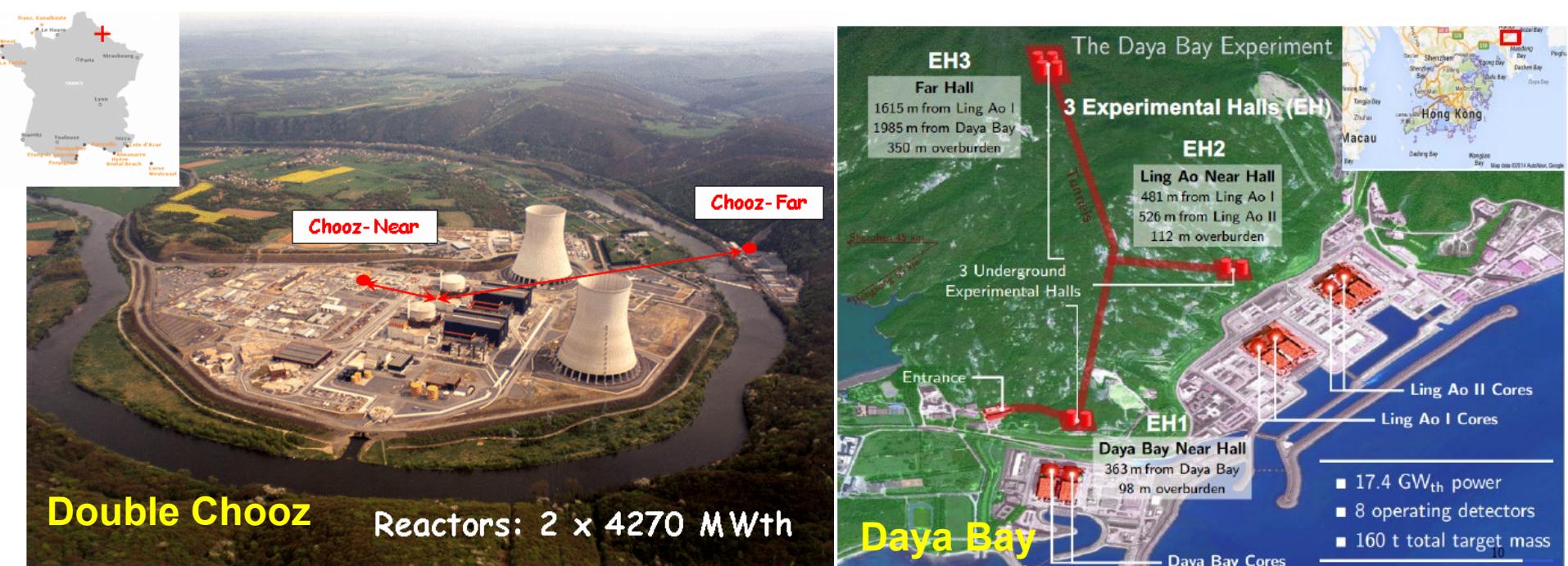
$$P_{ee} \approx 1 - \sin^2 2\theta_{13} \sin^2 \left(\frac{\Delta m_{31}^2 L}{4E_\nu} \right) - \cos^4 \theta_{13} \sin^2 2\theta_{12} \sin^2 \left(\frac{\Delta m_{21}^2 L}{4E_\nu} \right)$$



$$\Delta m_{sol}^2 \approx \Delta m_{21}^2 \\ \sim 7 \cdot 10^{-5} \text{ eV}^2$$



The $\bar{\nu}_e$ survival probability as a function of the distance from the nuclear power plant (NPP).

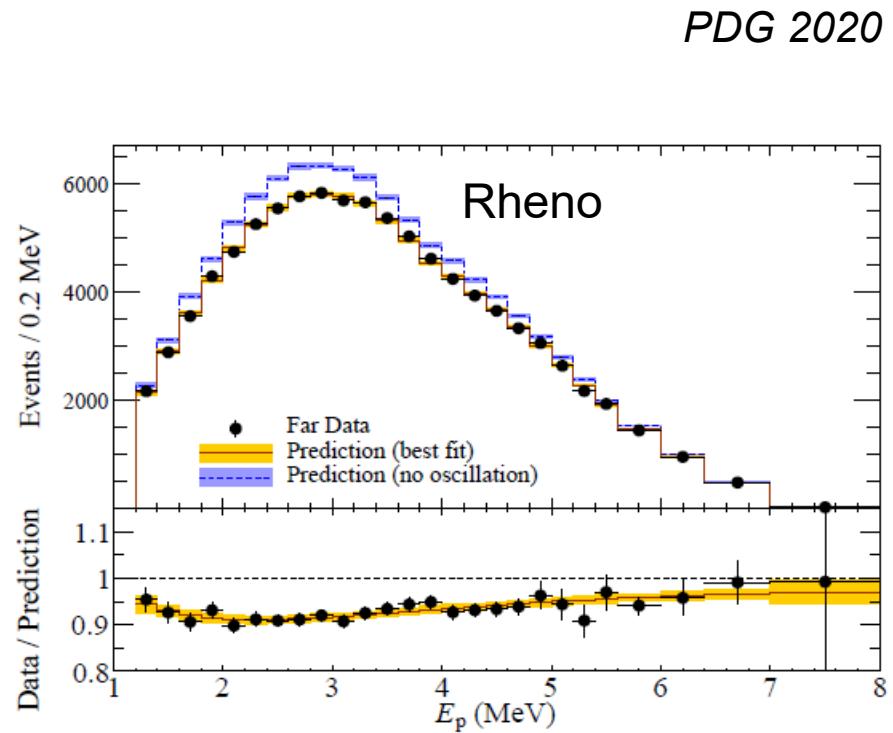
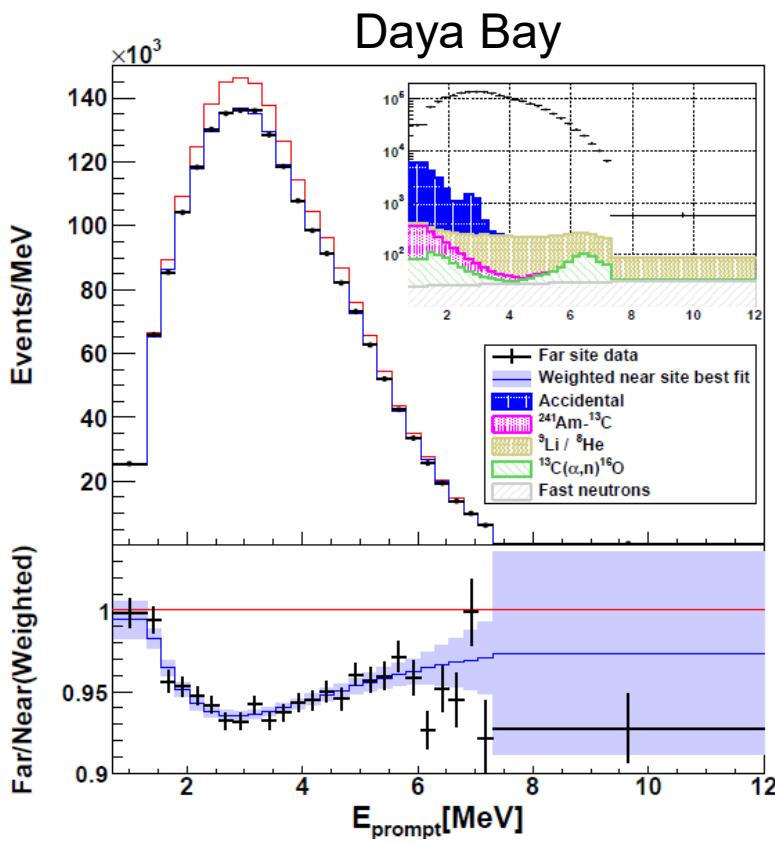


(China)

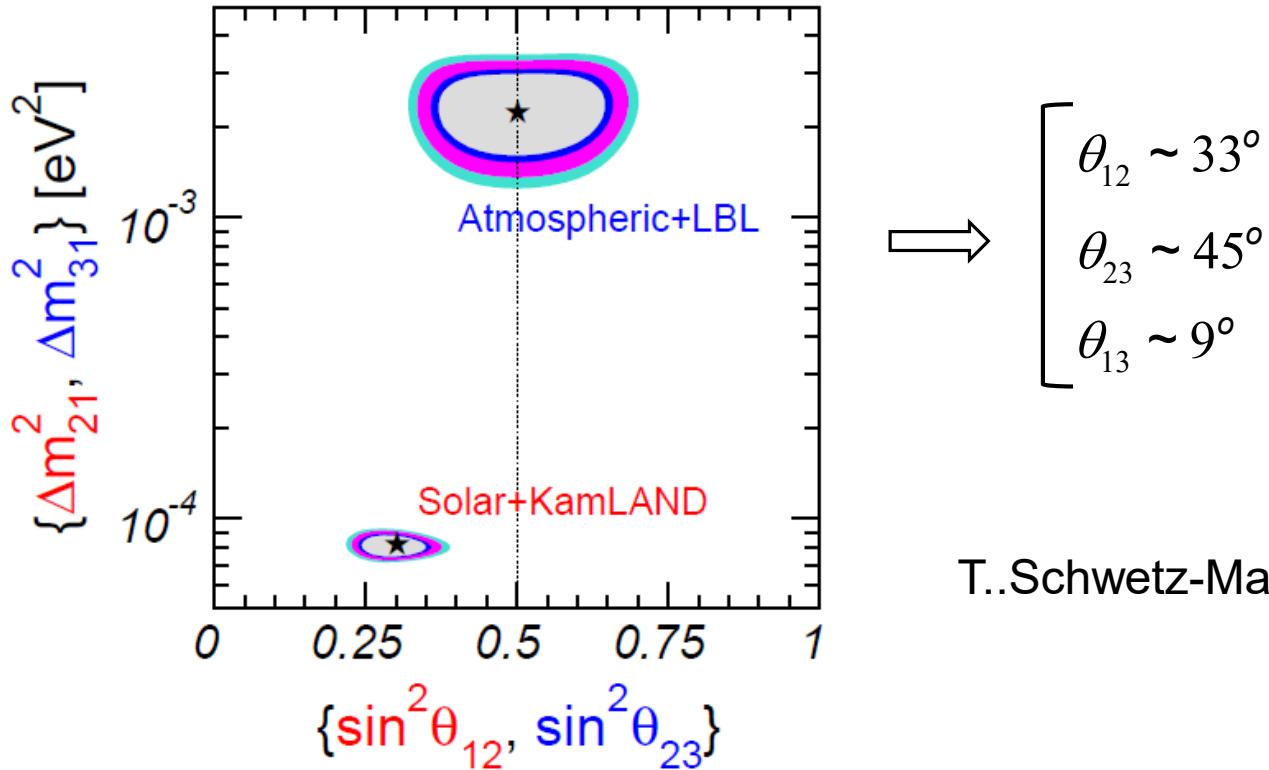
All experiments have a “near” detector to monitor the neutrino flux and a “far” (typ. Distance 1.5 km) to measure the deficit.

(South Korea)

The 3 reactor neutrino experiments published first results in 2012: [Double Chooz](#) reported an indication of electron antineutrino disappearance with the ratio of observed to expected events of $R = 0.944 \pm 0.016 \pm 0.04$ ruling out the no-oscillation hypothesis at 94.6% CL. [Daya Bay](#) observed of $R = 0.940 \pm 0.011 \pm 0.004$ corresponding to 5.2σ of a non-zero value of θ_{13} . [RENO](#) reported $R = 0.920 \pm 0.000 \pm 0.014$ indicating a non-zero value of θ_{13} with a significance of 4.9σ .



Summary: Neutrino Mixing



T..Schwetz-Mangold

$$|U_{PMNS}| \approx \begin{pmatrix} 0.82 & 0.58 & > 0 \\ 0.64 & 0.58 & 0.71 \\ 0.64 & 0.58 & 0.71 \end{pmatrix}$$

Summary: Neutrino masses

