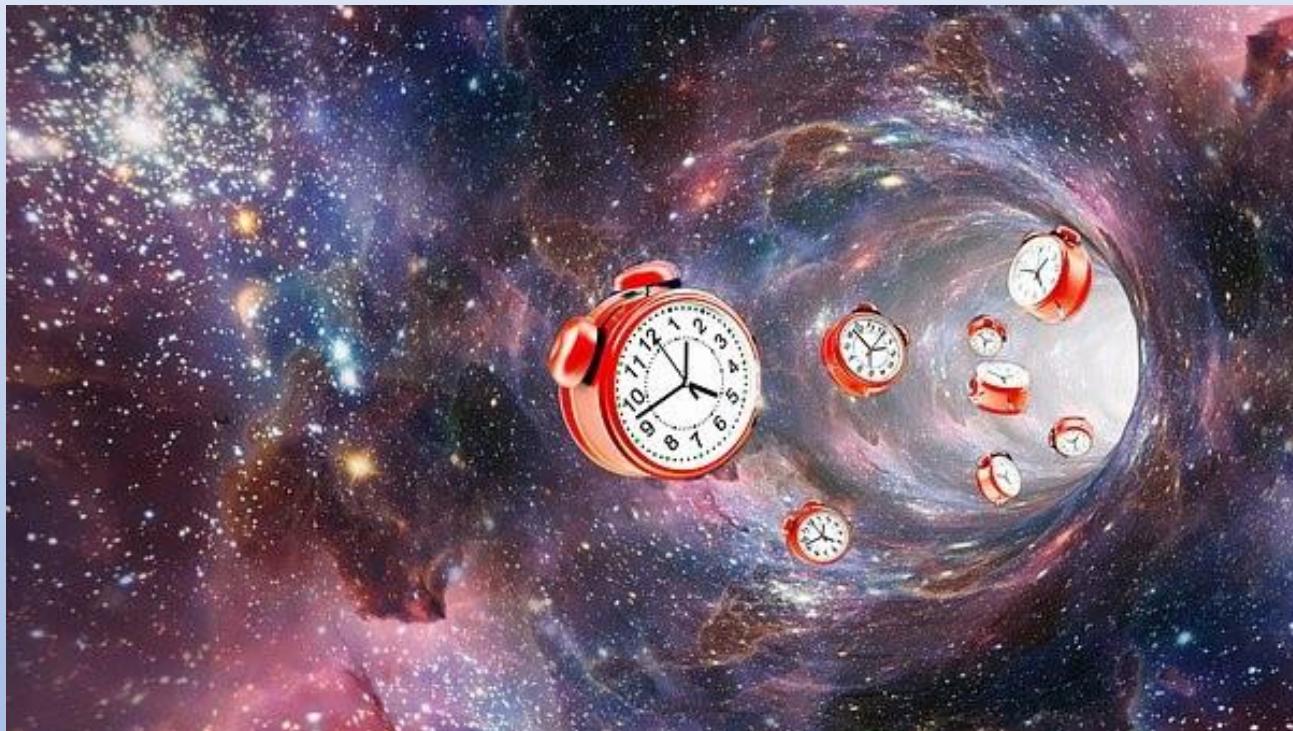


Atomic Clocks - How well can we measure time?

A presentation as part of the
Master Seminar „Your passion for
AMO-physics“ given by Lasse Kundy



Motivation – What is time?



[2, KIDPID...]

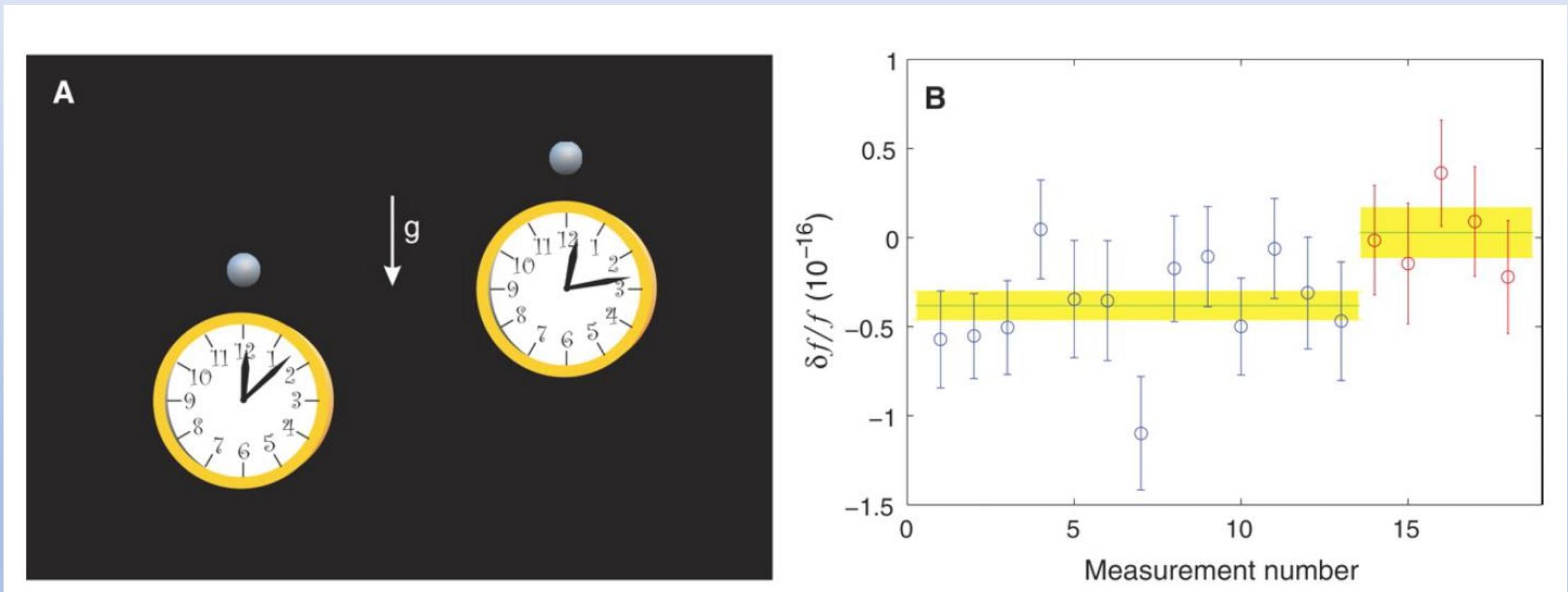
Height difference of
 $h = 33\text{cm}$

$$\Delta E = mgh = \frac{E}{c^2} gh$$

$$\frac{\Delta E}{E} = \frac{gh}{c^2} \rightarrow \frac{\Delta f}{f}$$

$$\approx 4 * 10^{-17}$$

Motivation

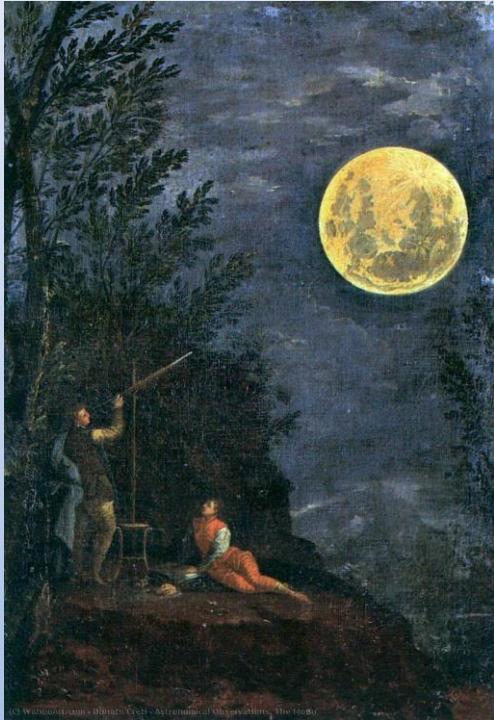


[3, C.W. Chou et al, Optical Clocks and Relativity]

Structure

- History of timekeeping
 - How does an atomic clock work?
 - Example: CSF1 atomic clock
 - Discussion
-
- Optical Clocks
 - CryPTEx-2 at MPIK
 - Applications
 - Summary
 - Discussion

History of timekeeping



[4, Usuem by Creti]
Astronomical observations



[5, Uhren-Hidding]
Pendulum Clock

$\sim 10^{-5}$

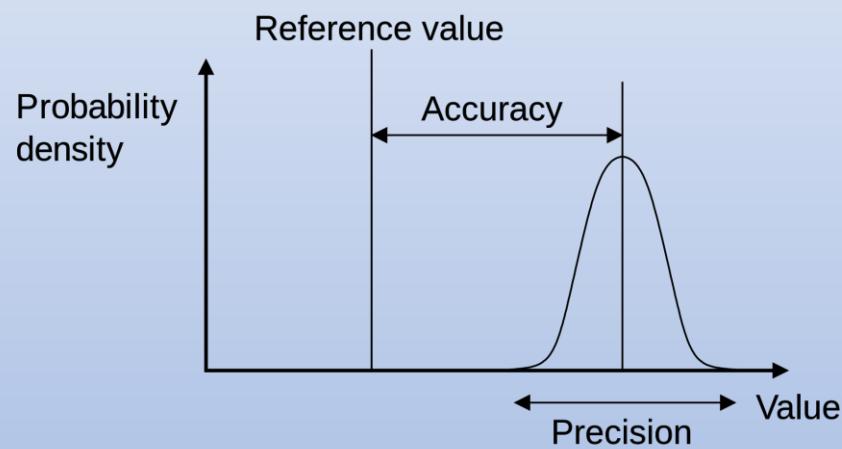


[6, Wikipedia Quartz Clock]

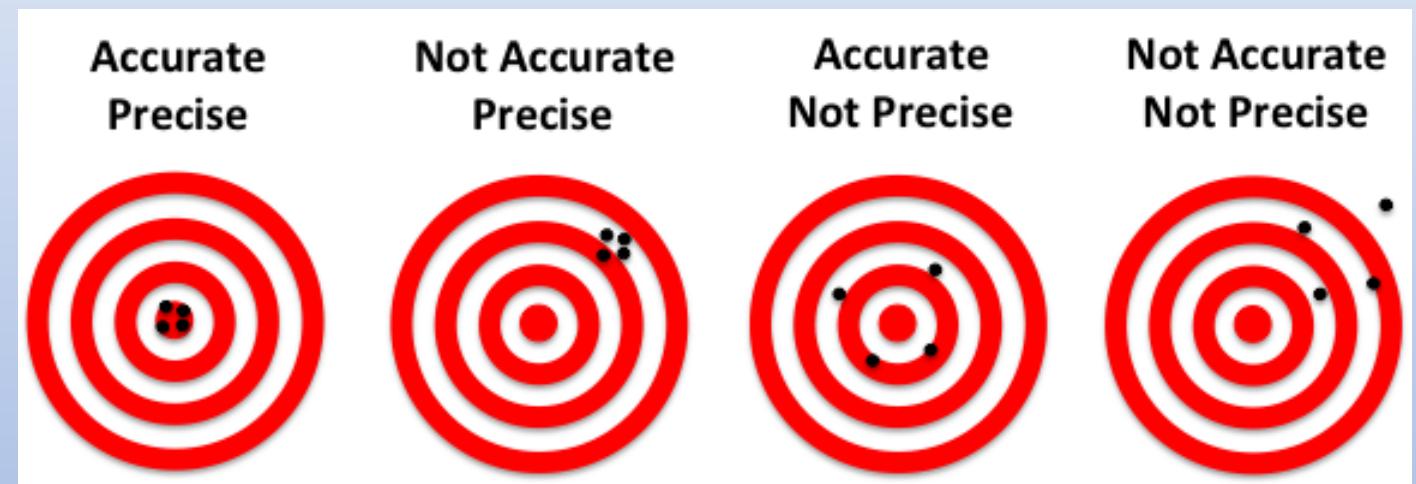
$\sim 10^{-8}$

$$\rightarrow \text{Relative uncertainty} = \frac{\Delta t}{t}$$

Accuracy vs. Precision



[7, Wikipedia, Accuracy and Precision]



[8, dnsoftwae]

Clock instability \sim relative uncertainty

spectroscopic linewidth of the clock system

$$\sigma_y(\tau) \approx \frac{\Delta\nu}{\nu_0 \sqrt{N}} \sqrt{\frac{T_c}{\tau}}$$

the time required for a single measurement cycle

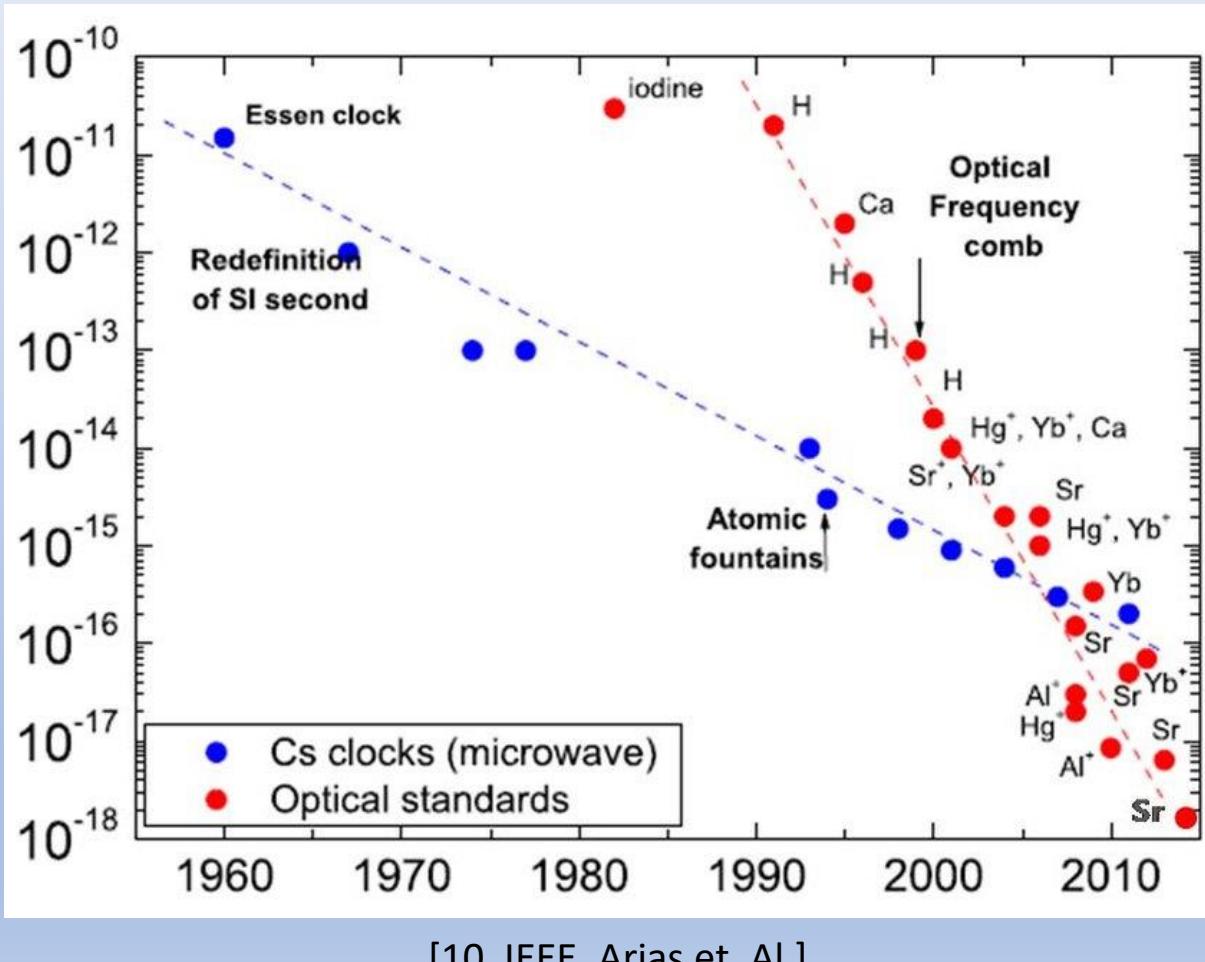
the averaging period

clock transition frequency

the number of atoms or ions used in a single measurement

[9, Safronova]

History of timekeeping



"The second is defined as being equal to the time duration of 9 192 631 770 periods of the radiation corresponding to the transition between the two hyperfine-levels of the fundamental unperturbed ground-state of the caesium-133 atom"

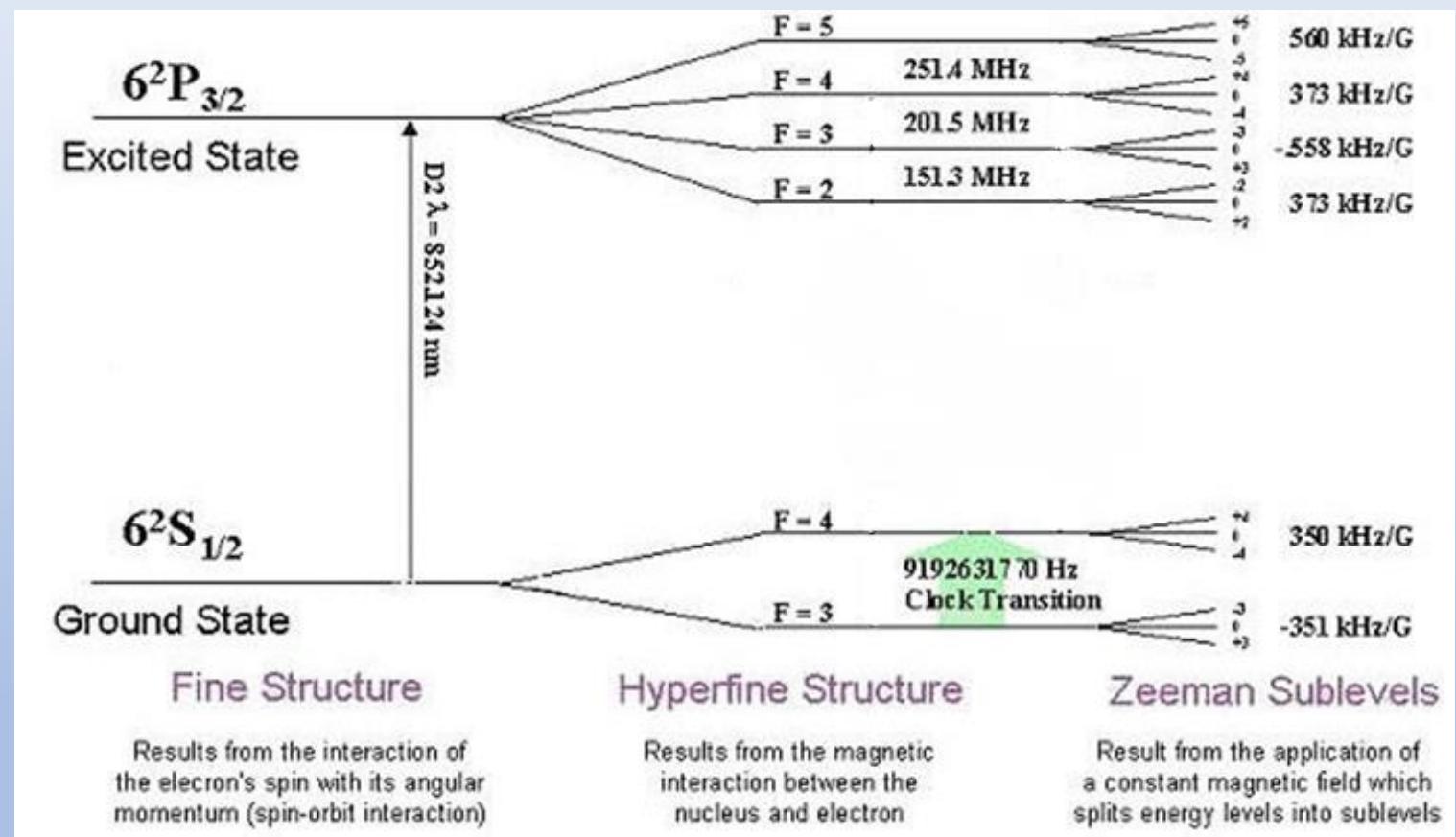
- International Bureau of Weights and Measures



2019, NIST, Al⁺

How does an atomic clock work?

- Interaction between light and internal electronic states of an atom
- In the case of Cs-133: hyperfine-transition is probed by microwaves
- $J = 1/2$
- $I = 7/2$



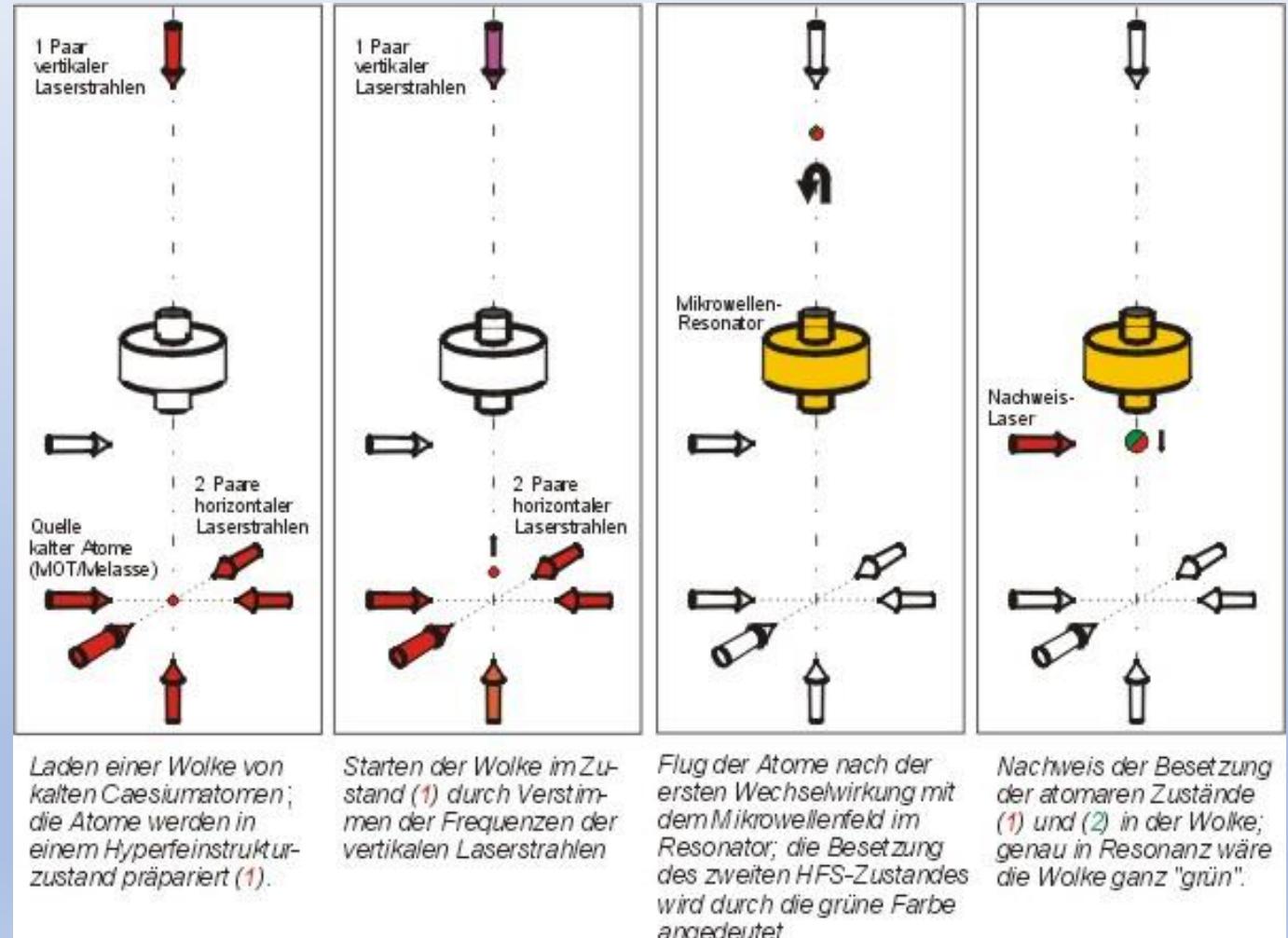
[11, PHARAO, Moric et.al.]

Example: CSF1 clock of PTB



[12, PTB, CSF1 and CSF2]

"9.192.631.770 oscillations"

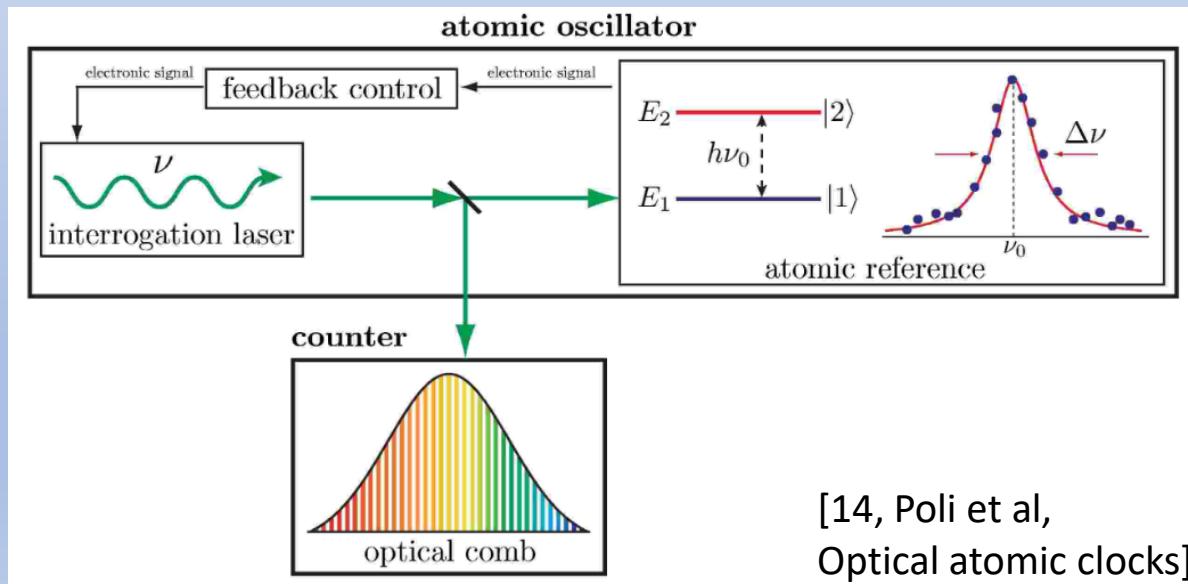


[13, PTB]

Discussion

Optical Clocks

- Transitions with optical frequencies $\sim 10^{15}$ Hz
- Only measurable by **frequency comb**



$$\sigma_y(\tau) \approx \frac{\Delta\nu}{\nu_0 \sqrt{N}} \sqrt{\frac{T_c}{\tau}}$$

spectroscopic linewidth of the clock system

the time required for a single measurement cycle

the averaging period

clock transition frequency

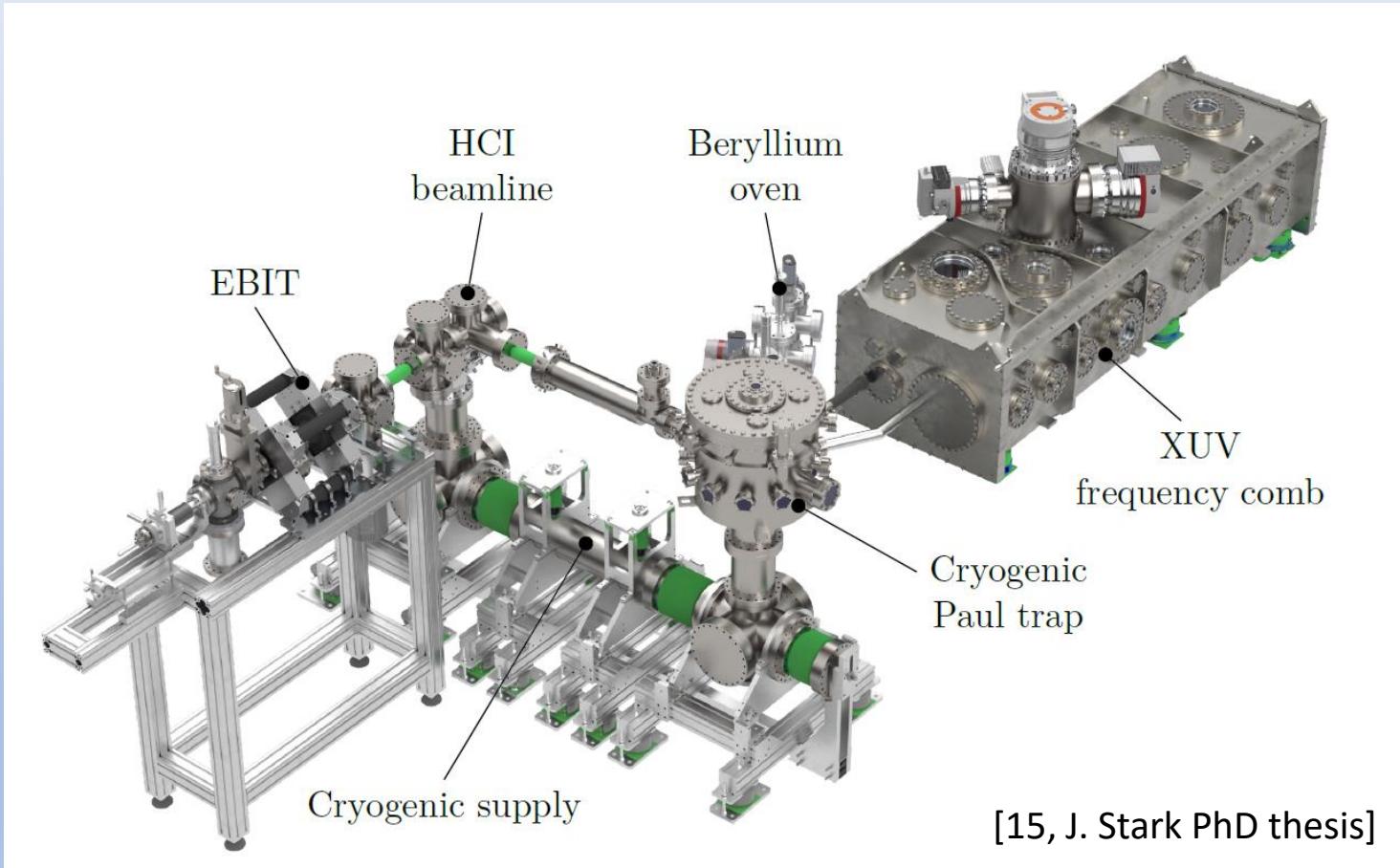
the number of atoms or ions used in a single measurement

[9, Safronova]

Highly Charged Ions (HCI)

- Less sensitive for perturbations
- Dipole forbidden transitions in the optical regime
 - Fine and Hyperfinetransitions
 - levelcrossings
- Very sensitive for possible α -variation
- Relative Change of $\frac{\dot{\alpha}}{\alpha} \sim 10^{-19}$ per year ?

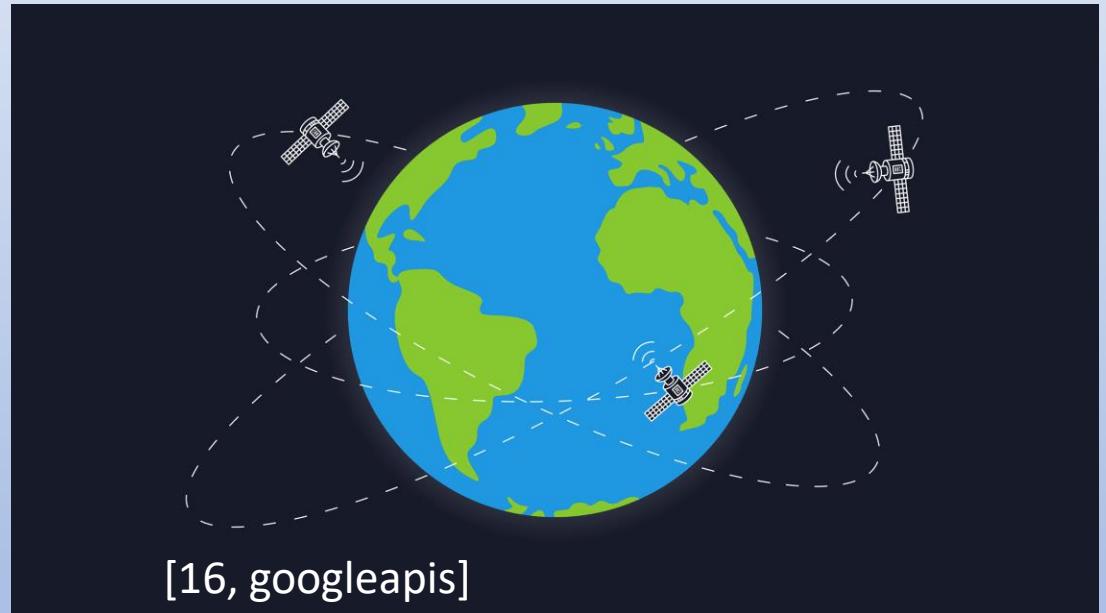
CryPTEEx-2 at MPIK



- Spectroscopy of cold HCl in the XUV
- Candidate for new frequency standards
- Testing QED/SM

Applications

- International Atomic Time (TAI)
- Coordinated Universal Time (UTC)
- Global Positioning System (GPS)
- Geodesy
- PHARAO
- Goal: smaller, cheaper, portable, energy efficient and more stable



Summary

- We can measure time very well
→ achieved **relative uncertainty** $\sim 10^{-19}$
- Definition of 1s is based on a hyperfinetransition of Caesium
- Next generation of **optical clocks**
- Many applications e.g. navigation systems
- Related experiments such CryPTEx-2
- Testing **Standard Model, Special and General Relativity**

Atomic Clocks - How well can we measure time?

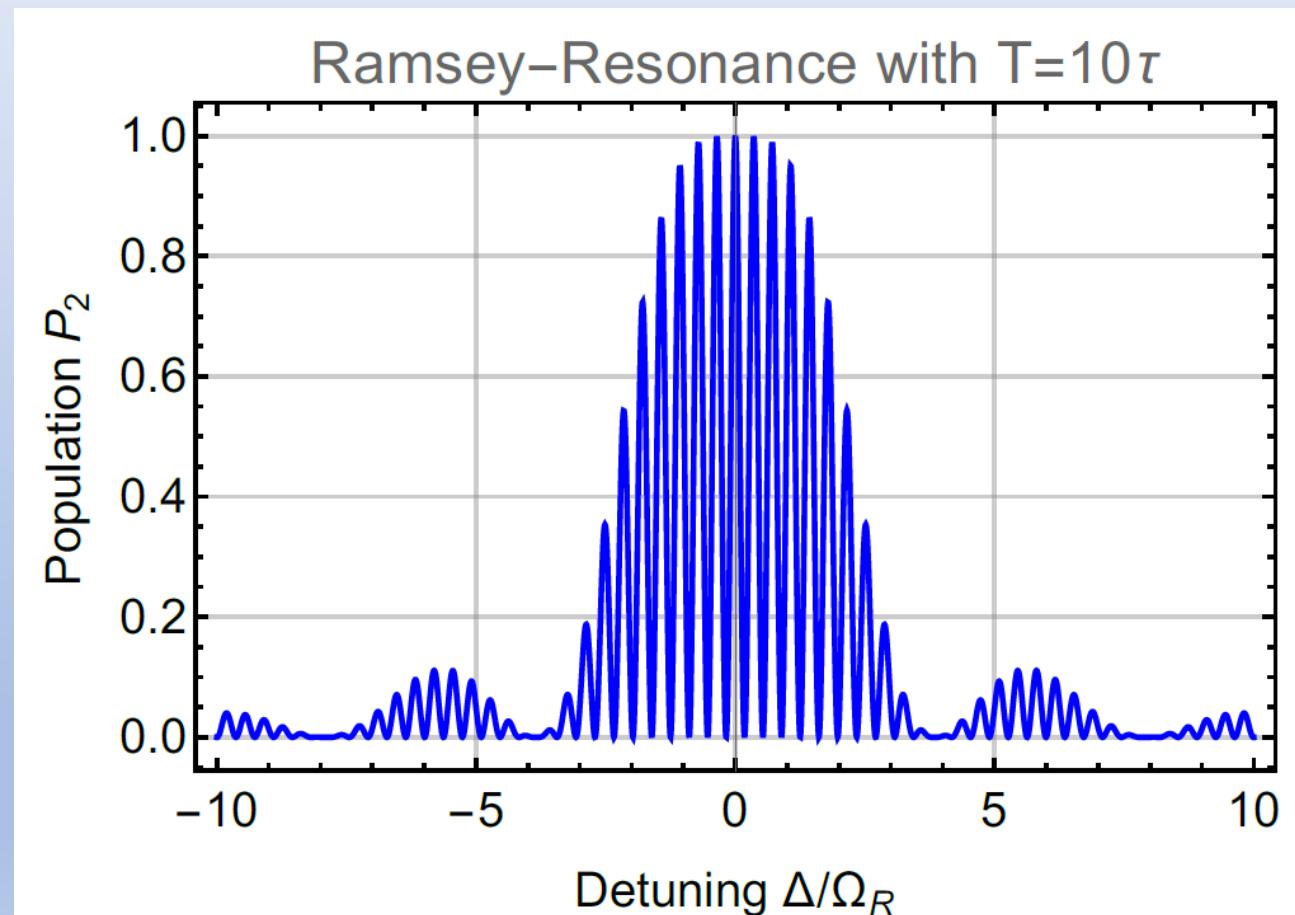
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Sources of figures

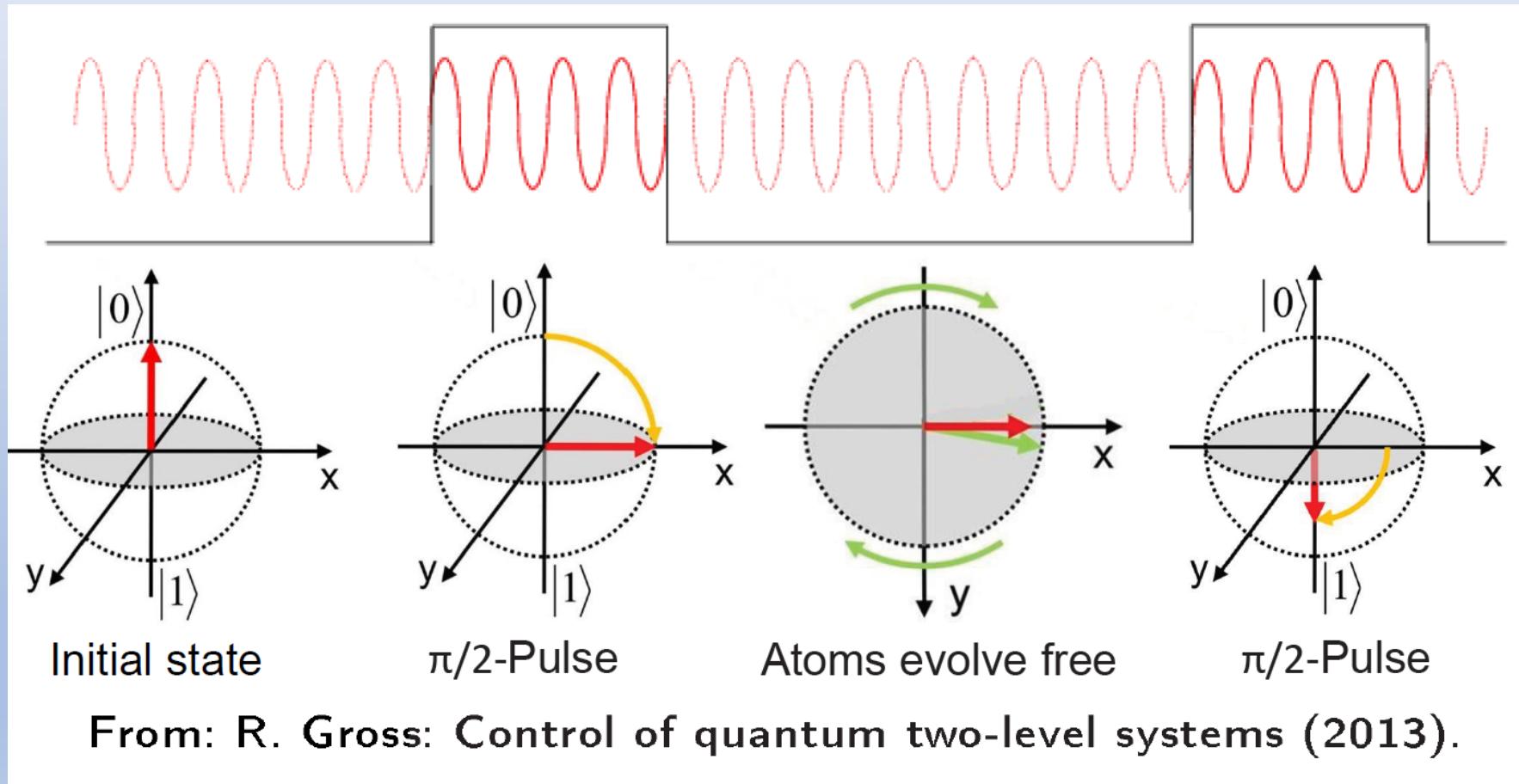
- [1] https://www.pyramidtimesystems.com/media/wysiwyg/atomic_clock_1.jpg
- [2] <https://www.kidpid.com/what-is-time-travel-is-it-possible/>
- [3] Chou CW, Hume DB, Rosenband T, Wineland DJ. Optical clocks and relativity. *Science*. 2010 Sep 24;329(5999):1630-3. doi: 10.1126/science.1192720. PMID: 20929843.
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- [5] <https://uhren-hidding.de/en/startseite/258-riefler-precision-pendulum-clock.html>
- [6] https://upload.wikimedia.org/wikipedia/commons/thumb/0/03/Clock_lock.jpg/1024px-Clock_lock.jpg
- [7] https://en.wikipedia.org/wiki/Accuracy_and_precision#/media/File:Accuracy_and_precision.svg
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- [9] Atomic Clock, presentation by Marianna Safronova, University of Delaware
- [10] The 50th Anniversary of the Atomic Second - Scientific Figure on ResearchGate. Available from: https://www.researchgate.net/figure/Reported-accuracy-of-atomic-transitions-from-BIPM-website_fig1_324253222 [accessed 10 May, 2021]
- [11] On-ground characterization of the cold atoms space clock PHARAO - Scientific Figure on ResearchGate. Available from: https://www.researchgate.net/figure/The-energy-levels-of-cesium-energy-level-used-for-clock-transition-and-cooling_fig5_281534634 [accessed 30 Apr, 2021]
- [12] https://www.ptb.de/cms/fileadmin/_processed/_csm_4_-_Uhren_13bfebd041.jpg
- [13] https://www.ptb.de/cms/fileadmin/internet/fachabteilungen/abteilung_4/4.4_zeit_und_frequenz/4.41/sequcsf1.jpg
- [14] Poli, Nicola, et al. "Optical atomic clocks." *La Rivista del Nuovo Cimento* 36 (2013): 555-624.
- [15] Julian Stark. "An Ultralow-Noise Superconducting Radio-Frequency Ion Trap for Frequency Metrology with Highly Charged Ions". Diss. Ruprecht-Karls-Universität Heidelberg, 2020.
- [16] https://storage.googleapis.com/geotab_wfm_production_cms_storage/CMS-Images-production/Blog/NA/_2020/May/GPS-update/blog-what-is-gps-hero@2x.png

Appendix A – Ramsey Fringe Pattern

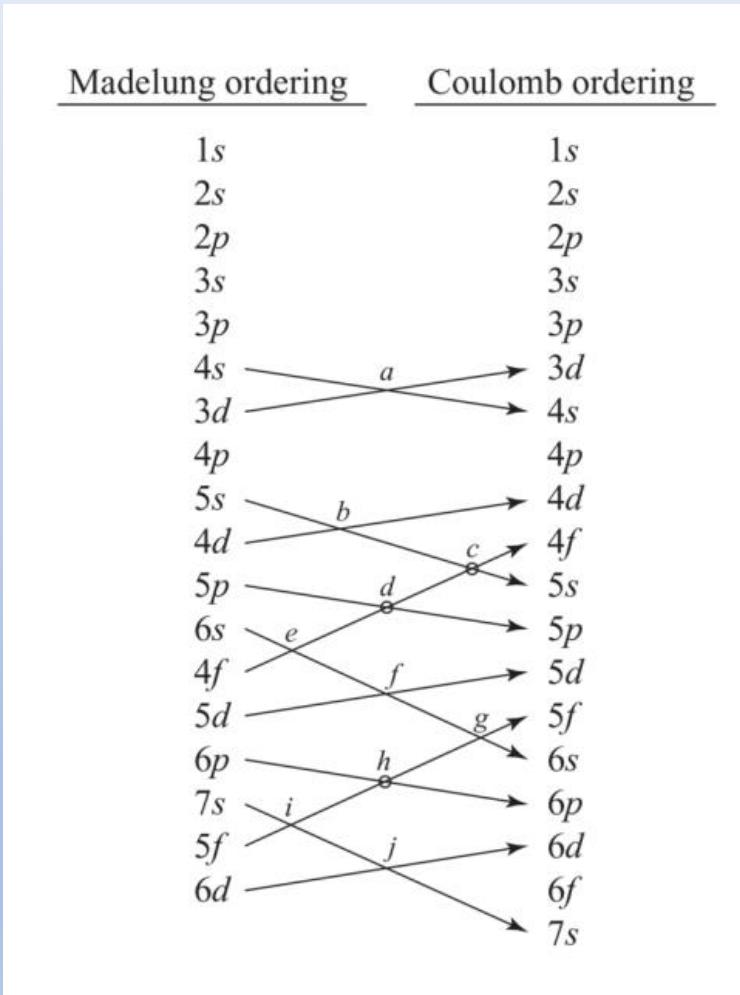


http://www.phys.cwru.edu/events/mppl/Hanneke/MPPL_clocks.pdf

Appendix B – Ramsey Resonance method



Appendix C - Levelcrossings



https://www.quantummetrology.de/fileadmin/quest/quest_institute/Projects/HCI/level_crossing.png